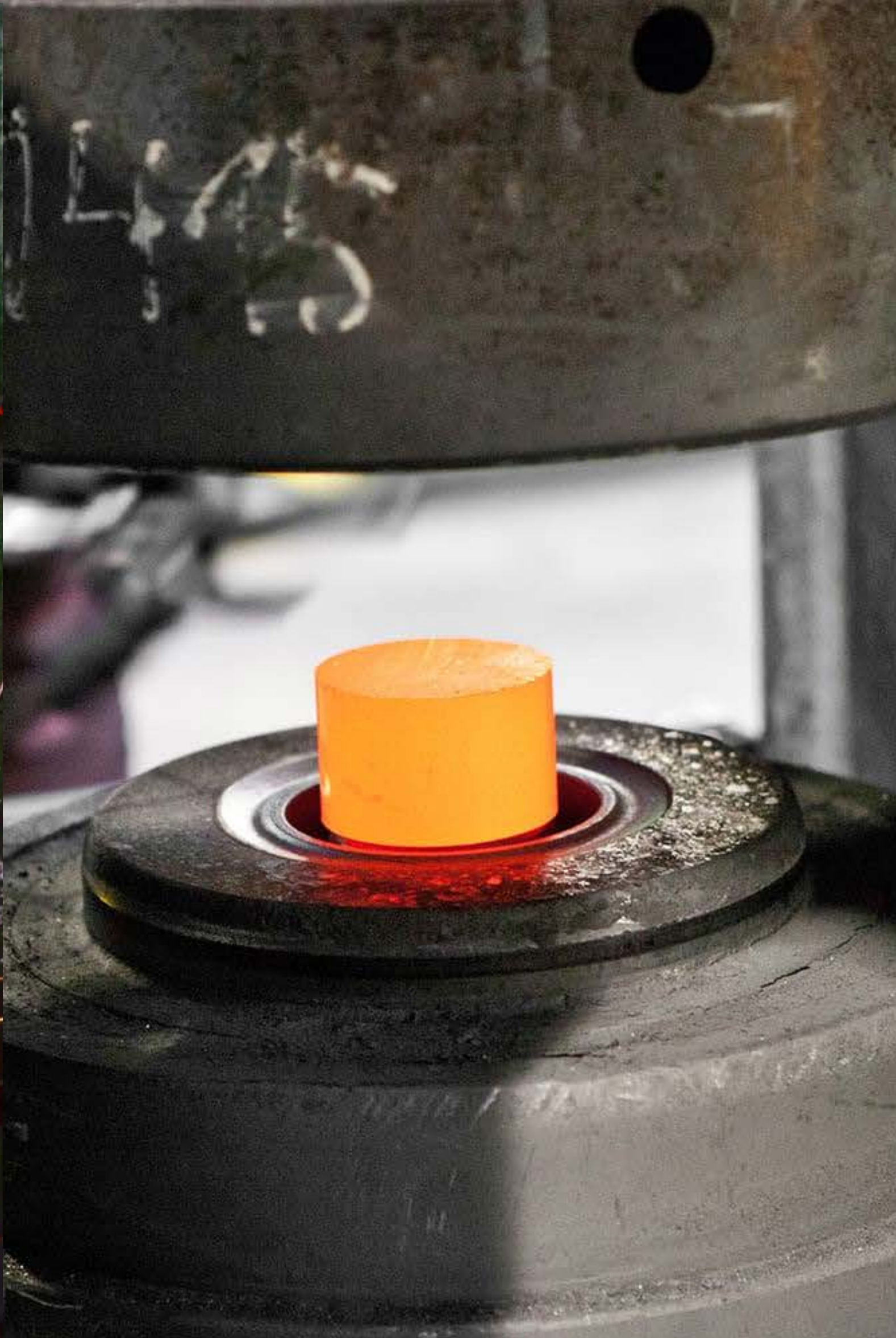


Deforming

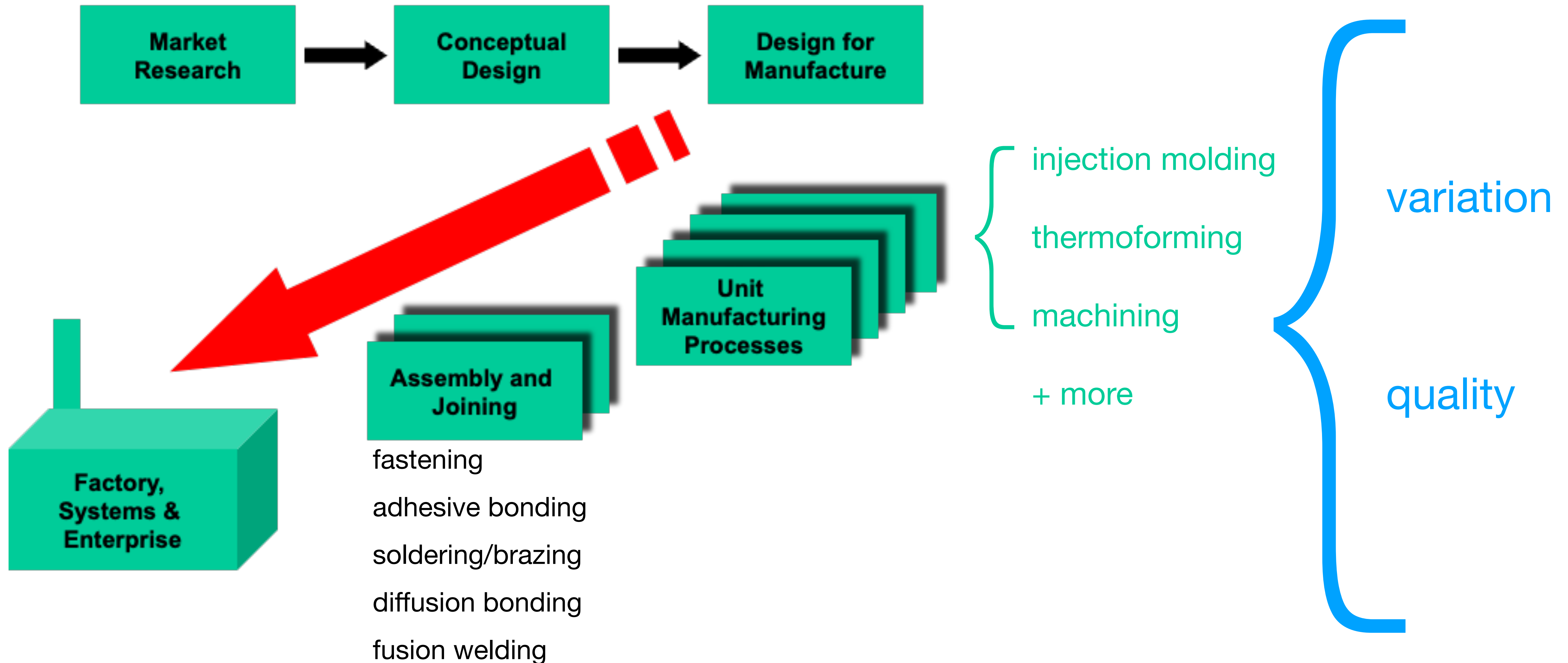
Forging, Extrusion, Sheet Metal: Processes and Equipment



Deforming

Forging, Extrusion, Sheet Metal: Processes and Equipment

2



Deforming

Forging, Extrusion, Sheet Metal: Processes and Equipment

3

2.008 Topic Coverage

Deformation process characteristics

Deformation physics

Common deformation processes

DFM

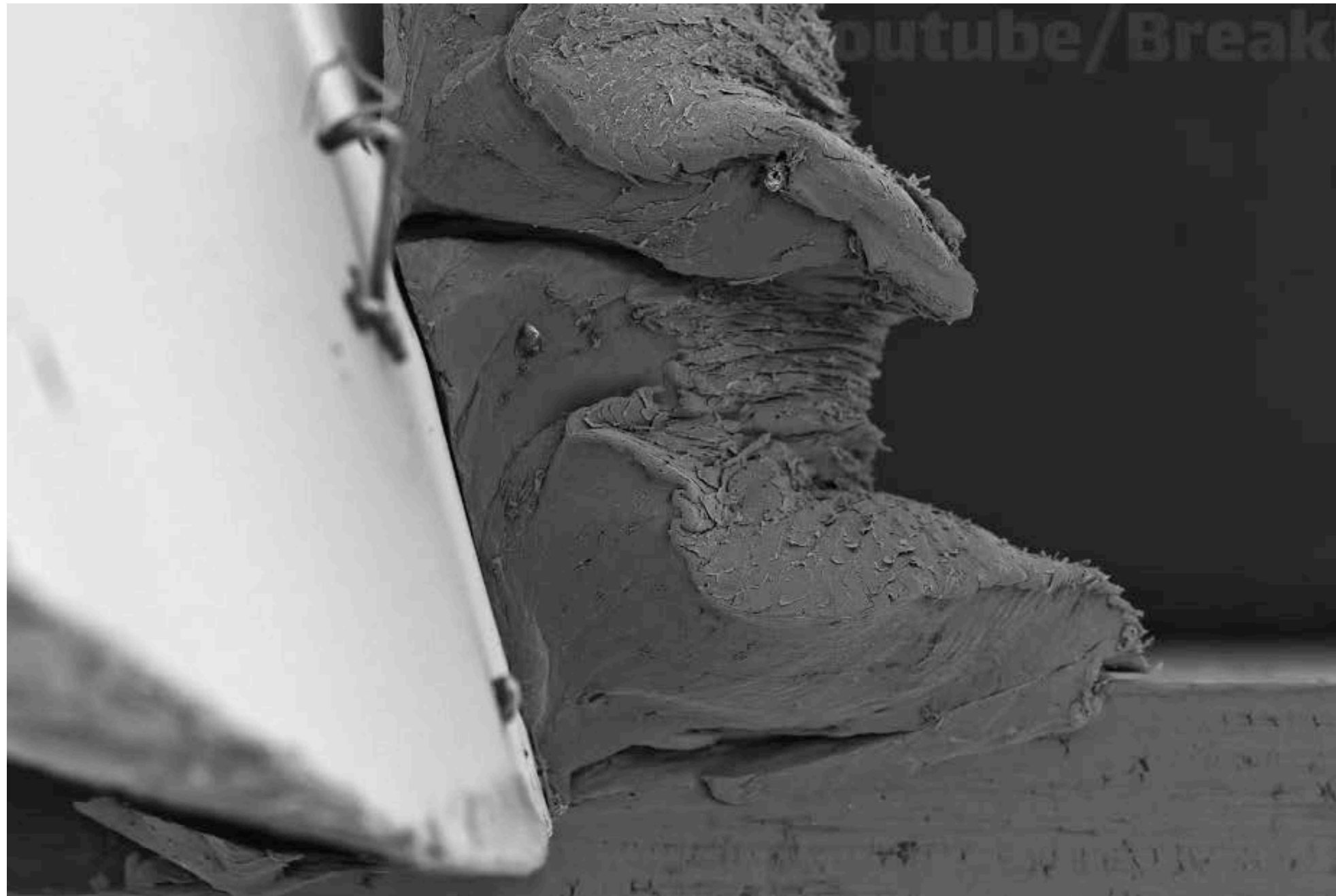


Deforming

Forging, Extrusion, Sheet Metal: Processes and Equipment

4

Deforming vs Machining



Machining:

- 10s-100s of **lbs**
- concentrated shear zone: **break material**



Deforming:

- 10s-100s of **tons**
- across large volumes: **do not want separation (cracks)**

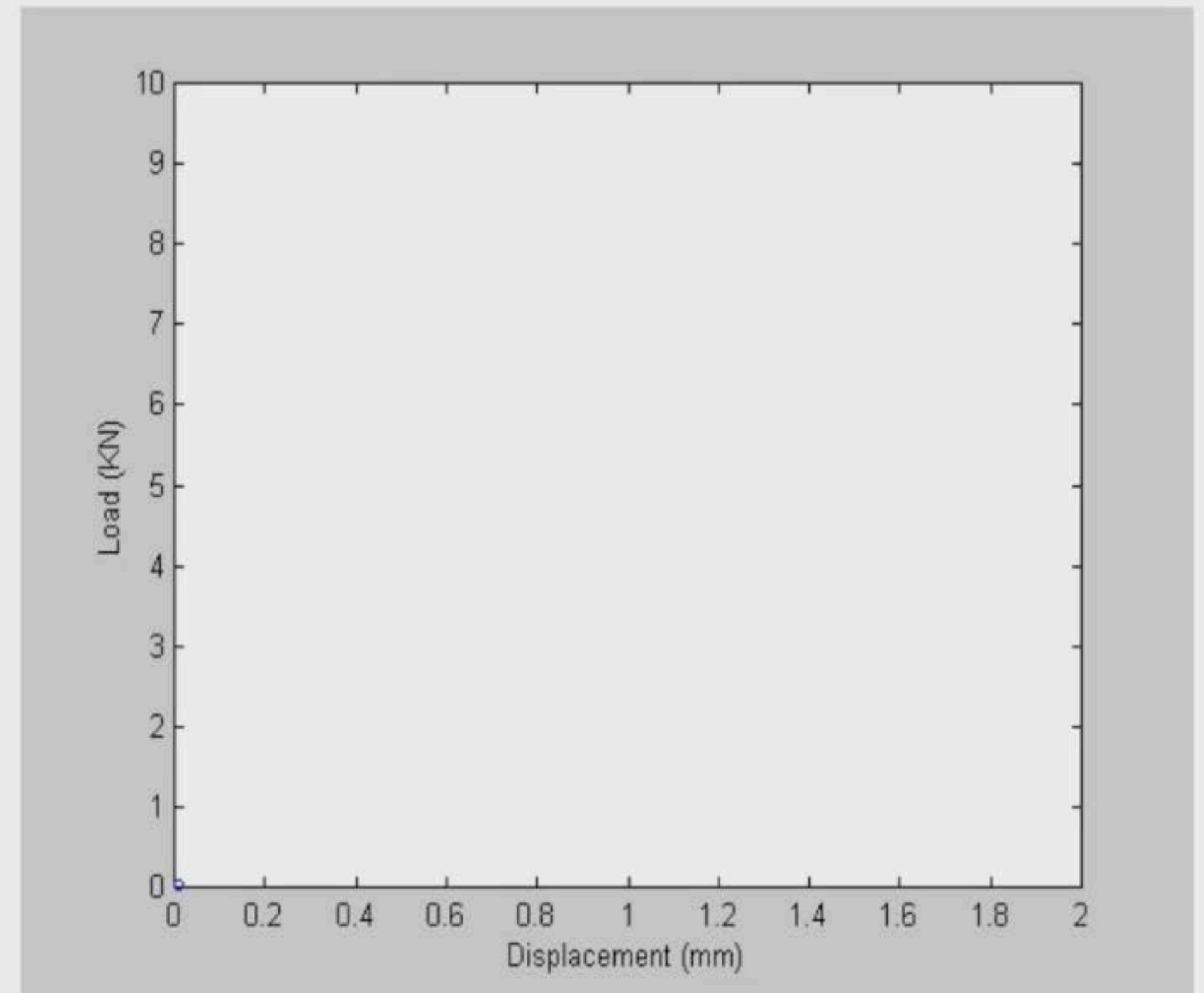
- any ductile material
- shape: limited by strain/plastic flow characteristics
- size: limited by equipment

Deforming

Forging, Extrusion, Sheet Metal: Processes and Equipment

5

Tensile Testing: Al 6061



Deforming

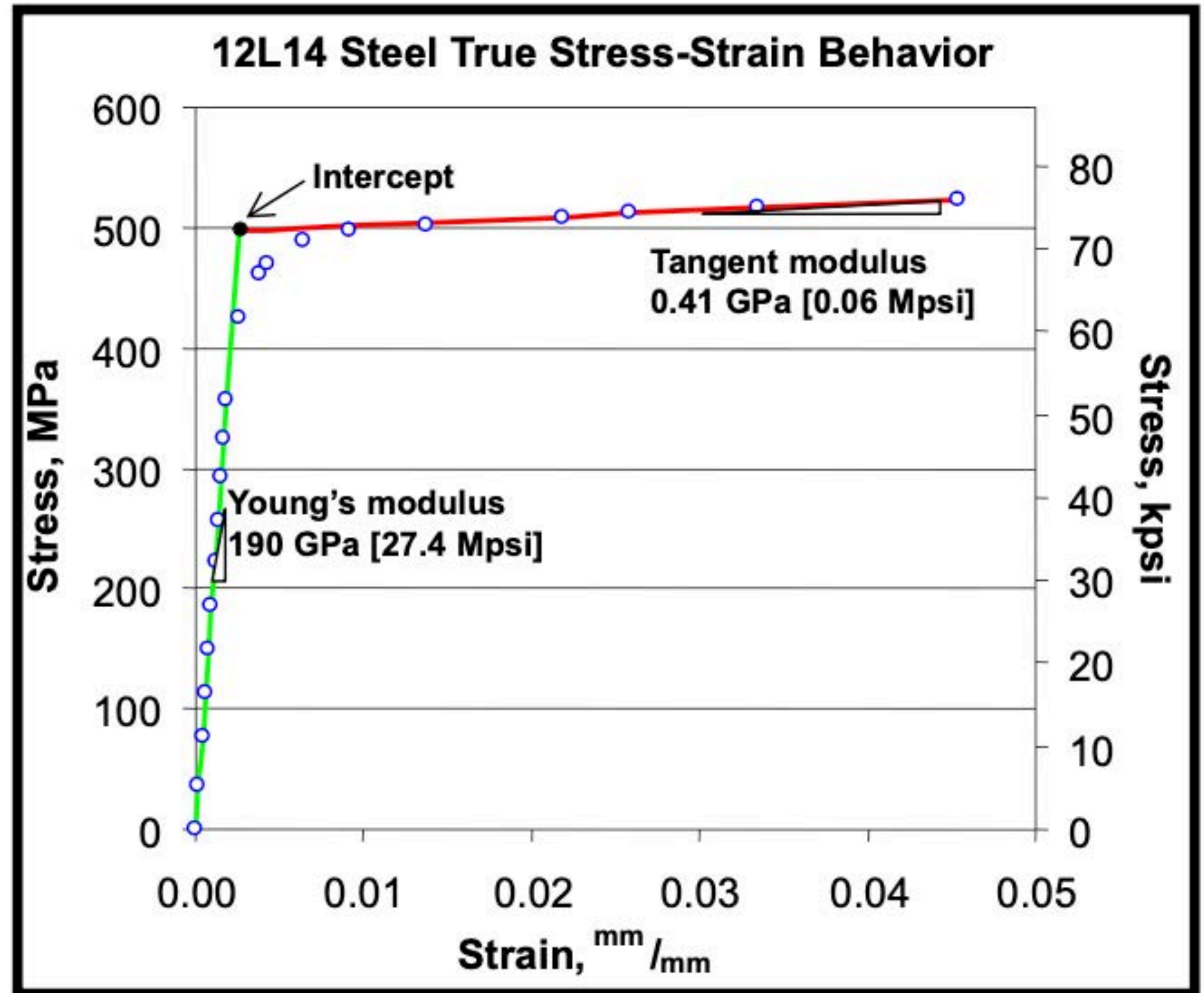
Forging, Extrusion, Sheet Metal: Processes and Equipment

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Steel: 12L14

elastic → plastic deformation to form part

- we **do not want** elastic - that undoes our work!
- bulk deformation: forging/rolling/extrusion - so much plastic deformation that elastic is not significant
- sheet forming: plastic deformation is not much bigger than elastic
- elevated temperature: easier to deform

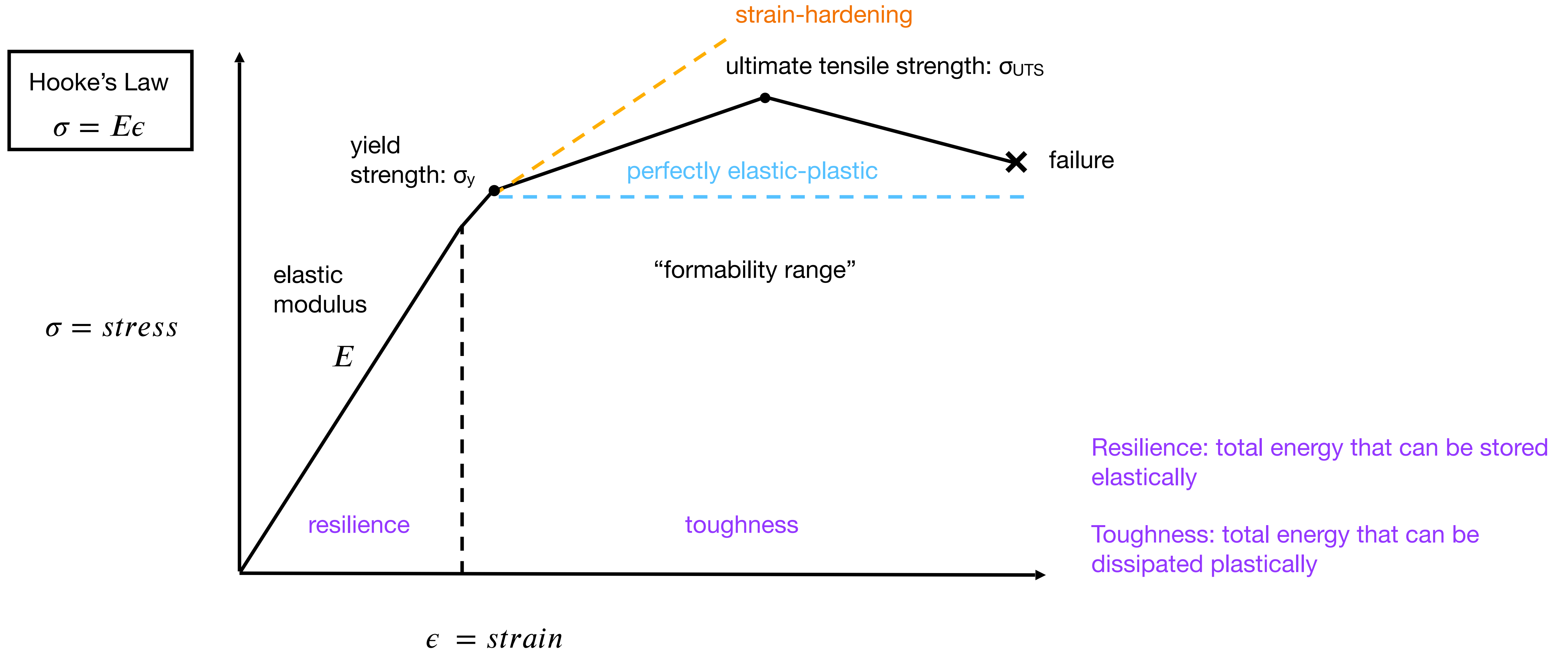


Deforming

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Stress-Strain Curve++



Deforming

Forging, Extrusion, Sheet Metal: Processes and Equipment

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2.008 Attributes

Internalize the **rate**, **quality**, **cost**, and **flexibility** as manufacturing attributes

Apply physics to understand the factors that influence the **rate**, **quality**, **cost**, and **flexibility** of processes

Apply an understanding of variation to the factor that influence **rate**, **quality**, **cost**, and **flexibility** of processes and systems

Understand the impact of manufacturing constraints on product design and process planning



Stress/Strain → deformation force

- force dictates equipment and energy requirements

Friction → energy requirements, lubrication, quality (**friction is not repeatable, coefficient is not constant**)

BETA

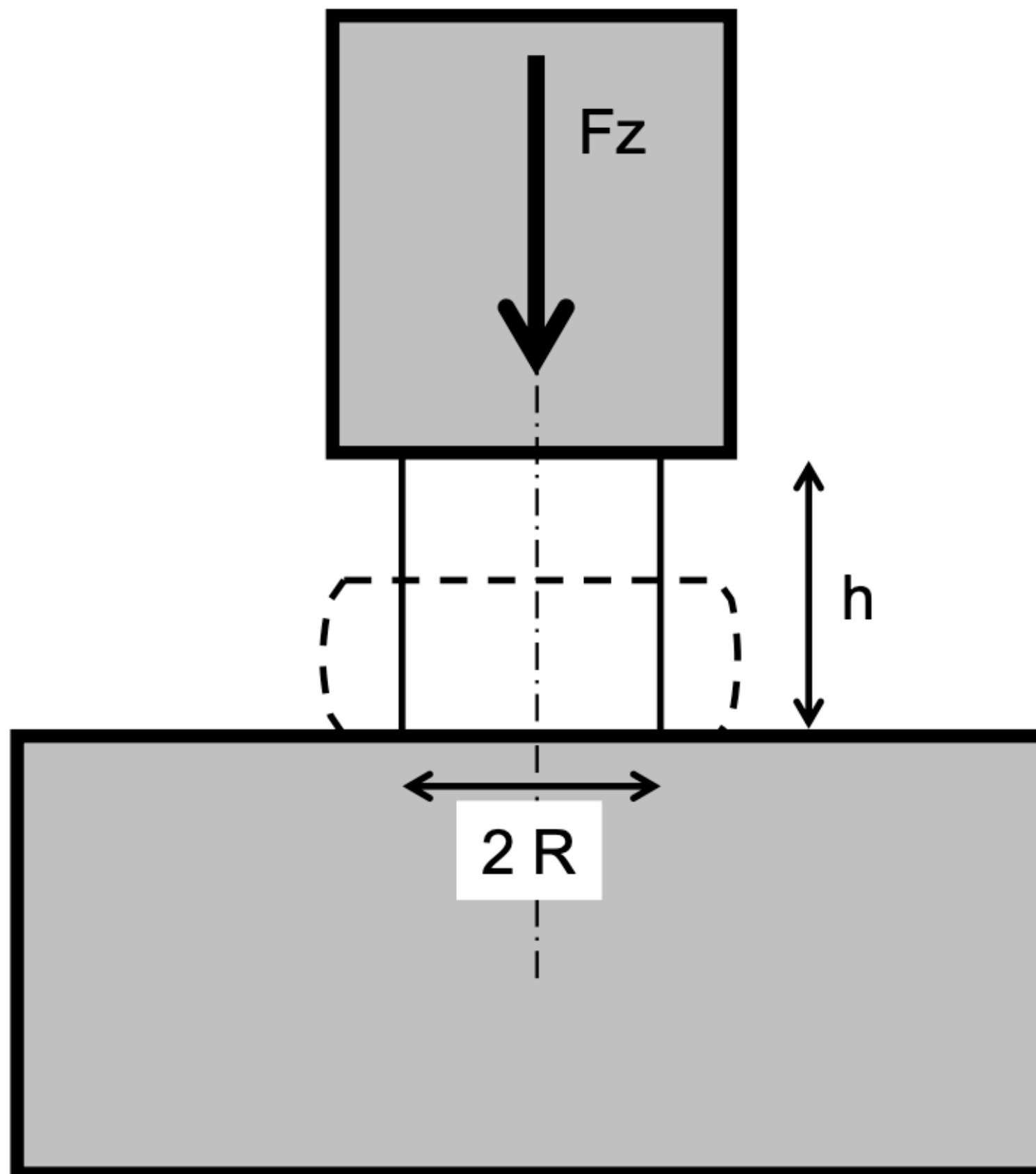


Deforming

Forging, Extrusion, Sheet Metal: Processes and Equipment

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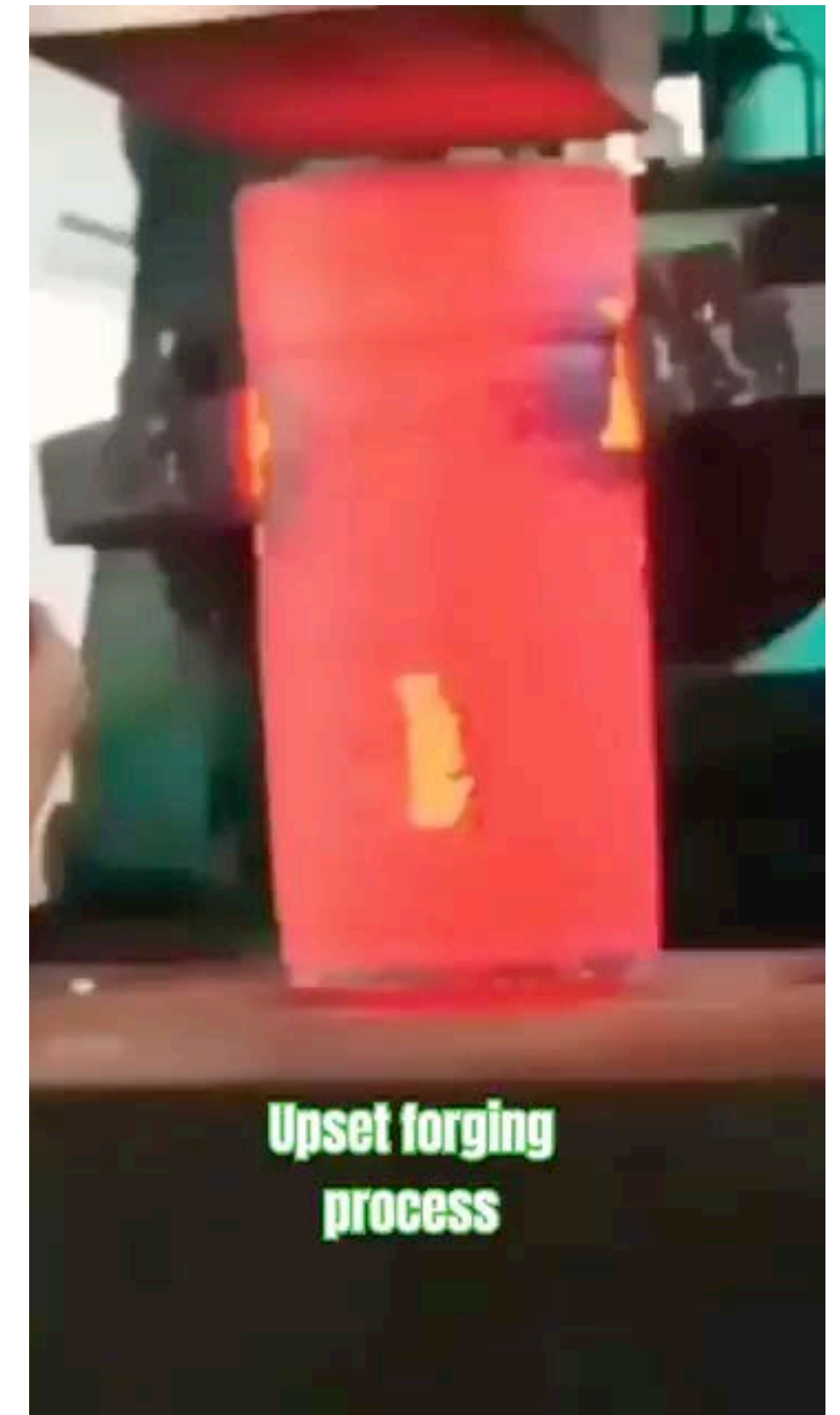
Forging Force and Friction



Axi-symmetric Upsetting

Assumptions:

- Tresca yield \rightarrow plastic deformation \rightarrow flow
- constant friction coefficient
- no “barreling”

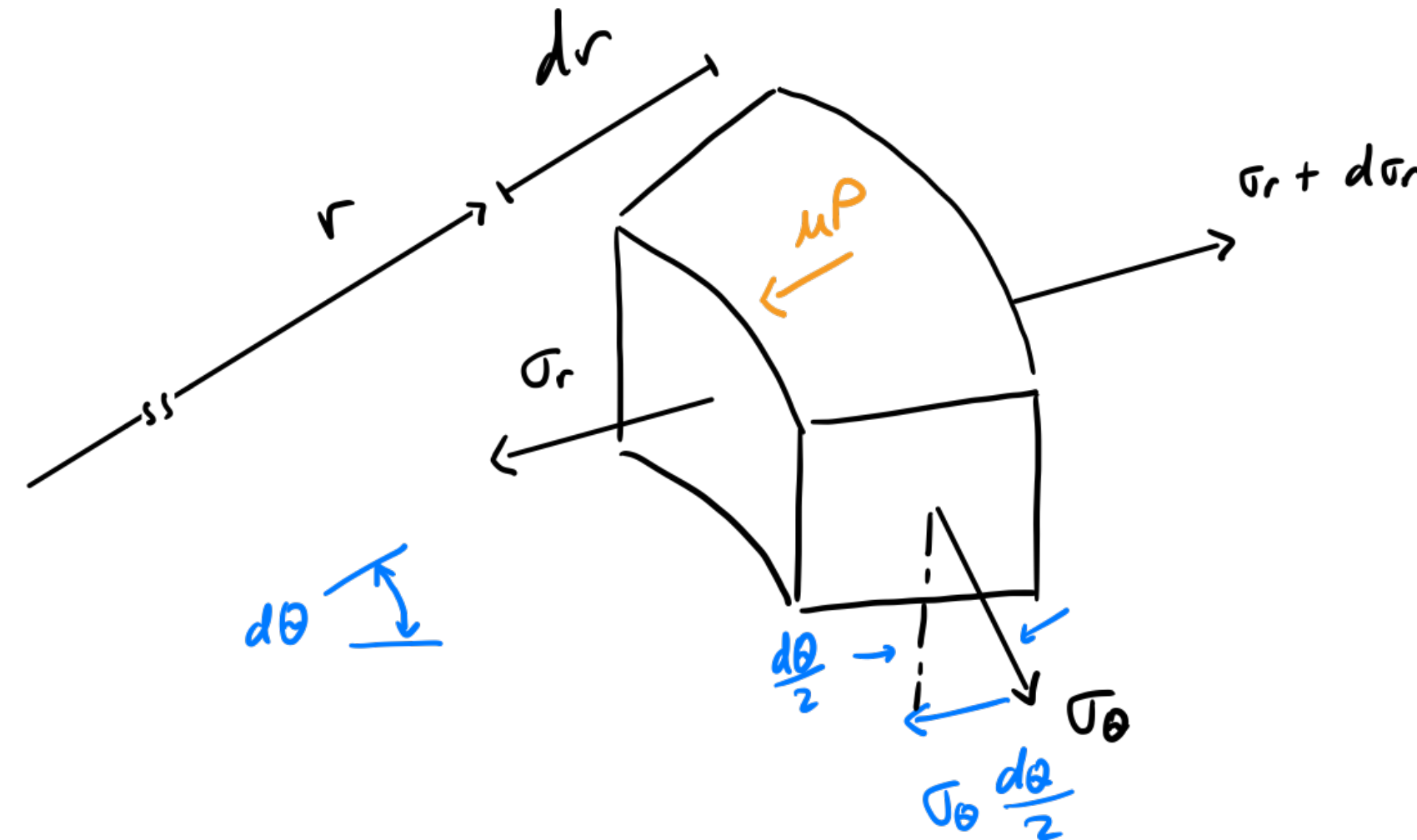
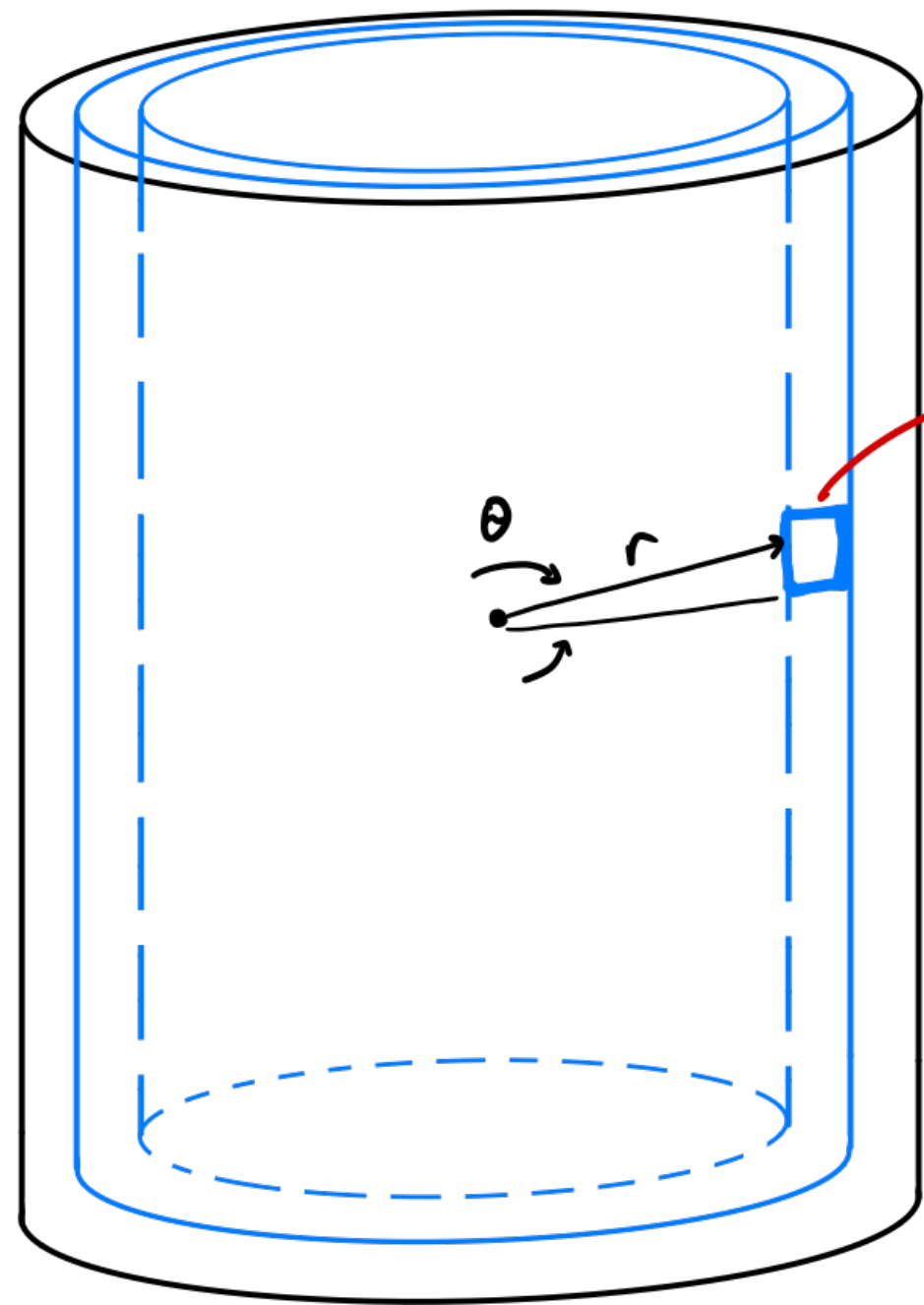


Deforming

Forging, Extrusion, Sheet Metal: Processes and Equipment

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Forging Force and Friction



Eq. A: Equilibrium in the r direction

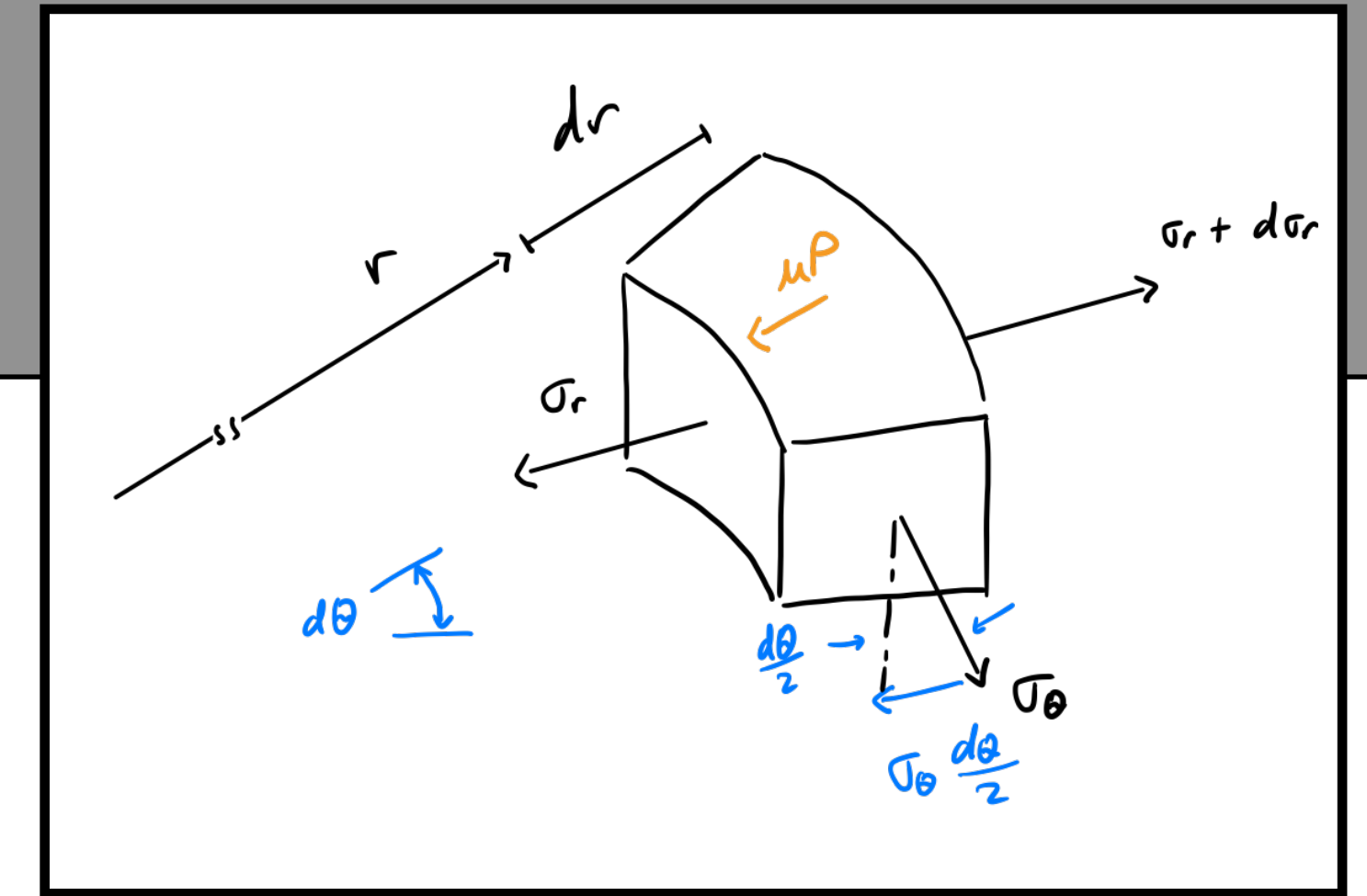
$$\sum dF_r = 0 = \underbrace{\sigma_r \cdot h \cdot r \cdot d\theta}_{\text{inner arc}} - \underbrace{2 \cdot \mu \cdot P \cdot r \cdot d\theta \cdot dr}_{\text{friction top and bottom}} - \underbrace{2 \cdot \sigma_\theta \cdot h \cdot dr \cdot \frac{d\theta}{2}}_{\text{hoop}} + \underbrace{(\sigma_r + d\sigma_r) \cdot (r + dr) \cdot h \cdot d\theta}_{\text{outer arc}}$$

$$\frac{d\sigma_r}{r} = \frac{2\mu P}{h} = -\frac{2\mu\sigma_z}{h}$$

Deforming

Forging, Extrusion, Sheet Metal: Processes and Equipment

Forging Force and Friction



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Eq. A: Equilibrium in the r direction

$$\sum dF_r = 0 = \underbrace{\sigma_r \cdot h \cdot r \cdot d\theta}_{\text{inner arc}} - \underbrace{2 \cdot \mu \cdot P \cdot r \cdot d\theta \cdot dr}_{\text{friction top and bottom}} - \underbrace{2 \cdot \sigma_\theta \cdot h \cdot dr \cdot \frac{d\theta}{2}}_{\text{hoop}} + \underbrace{(\sigma_r + d\sigma_r) \cdot (r + dr) \cdot h \cdot d\theta}_{\text{outer arc}}$$

$$\frac{d\sigma_r}{r} = \frac{2\mu P}{h} = -\frac{2\mu\sigma_z}{h}$$

Eq. B: Tresca Yield Criterion

$$\sigma_r - \sigma_z = Y \quad \rightarrow \quad \frac{d\sigma_z}{dr} = \frac{d\sigma_r}{dr}$$

$$\sigma_z = -Y \cdot e^{\frac{2\mu}{h}(R-r)}$$

Deforming

Forging, Extrusion, Sheet Metal: Processes and Equipment

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Forging Force and Friction

$$F_z = \int_0^R \sigma_z \cdot 2 \cdot \pi \cdot r \cdot dr = (\pi \cdot R^2) \cdot \frac{1}{2} \cdot \left(\frac{h}{\mu R} \right)^2 \cdot Y \cdot \left(e^{\frac{2\mu R}{h}} - \frac{2\mu R}{h} - 1 \right)$$

Use Taylor's series expansion to approximate the exponential and expand about 0 (valid for small $2\mu R/h$)

$$|F_z| = (\pi R^2) \cdot Y \cdot \left(1 + \frac{2\mu R}{3h} \right)$$

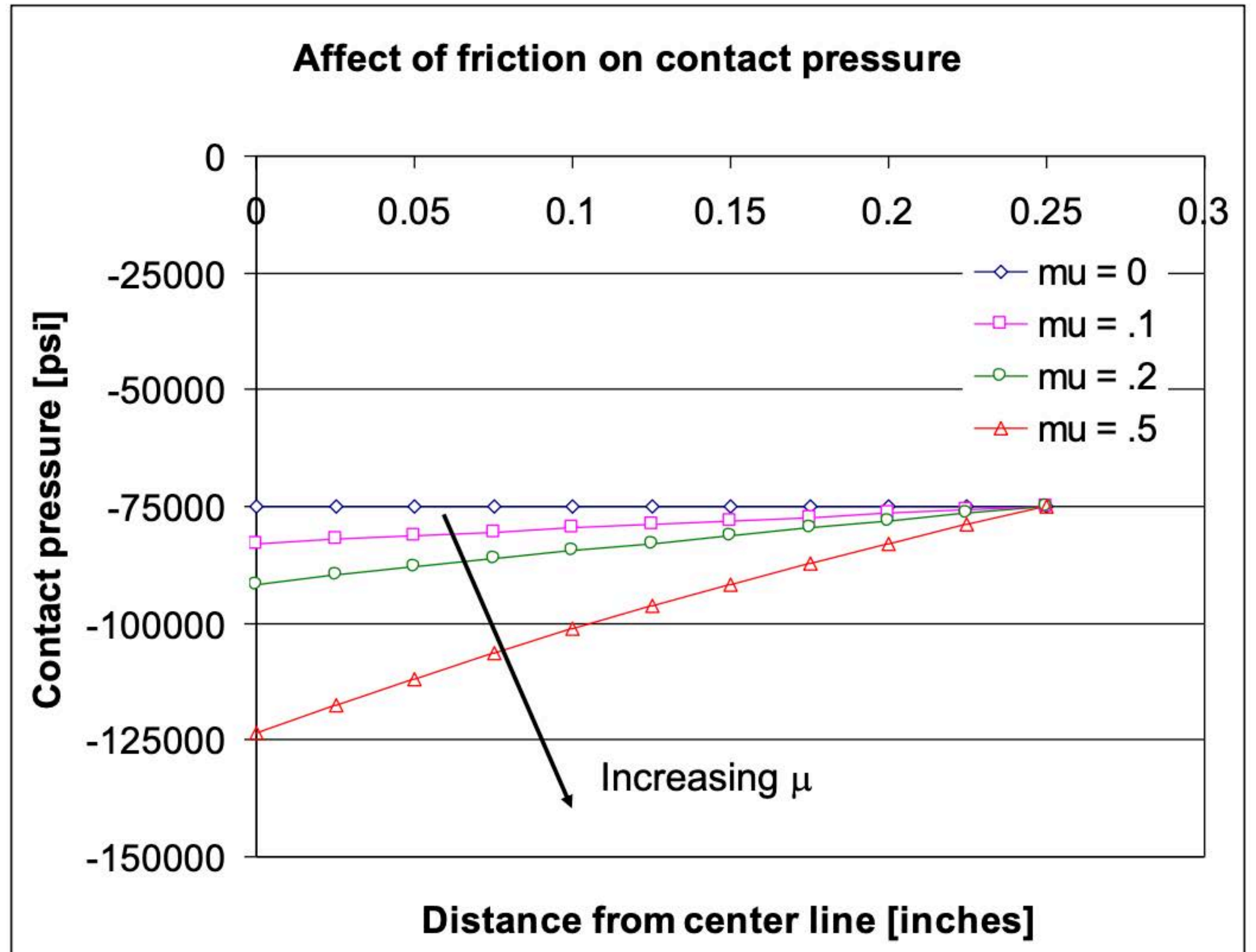
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Forging Force and Friction

$Y = 75000 \text{ psi}$
 $h = \frac{1}{2} \text{ inch}$

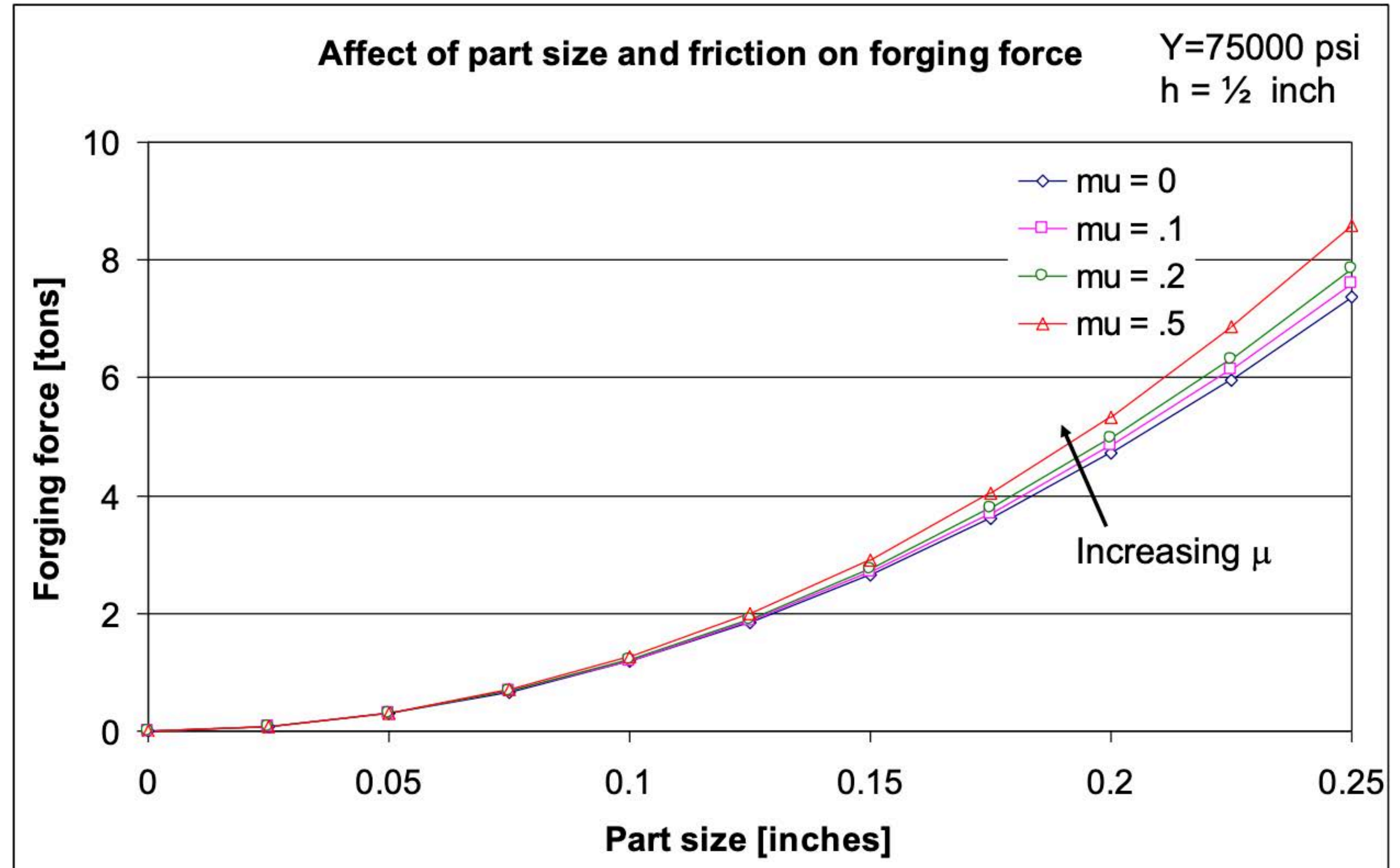


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Forging Force and Friction

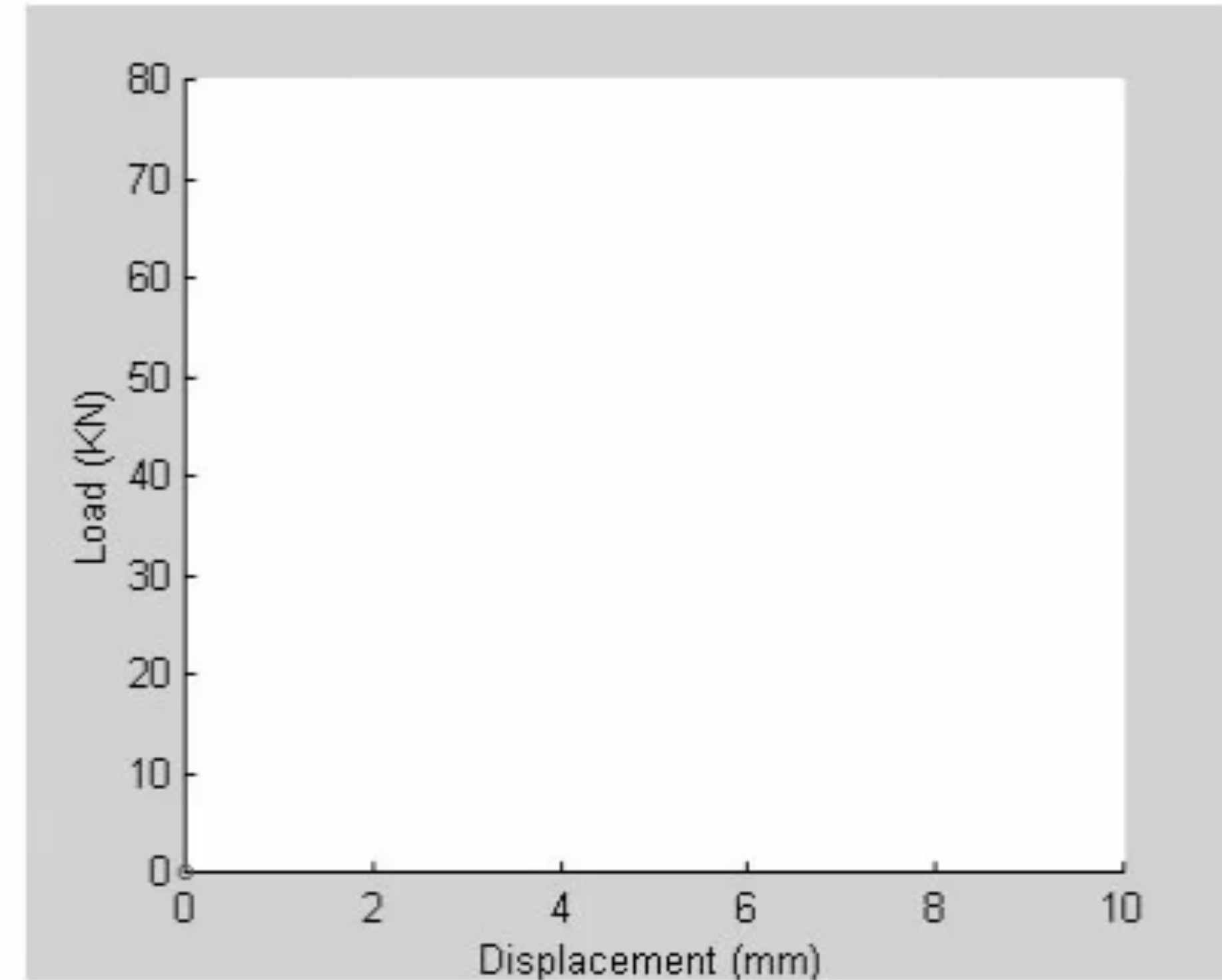
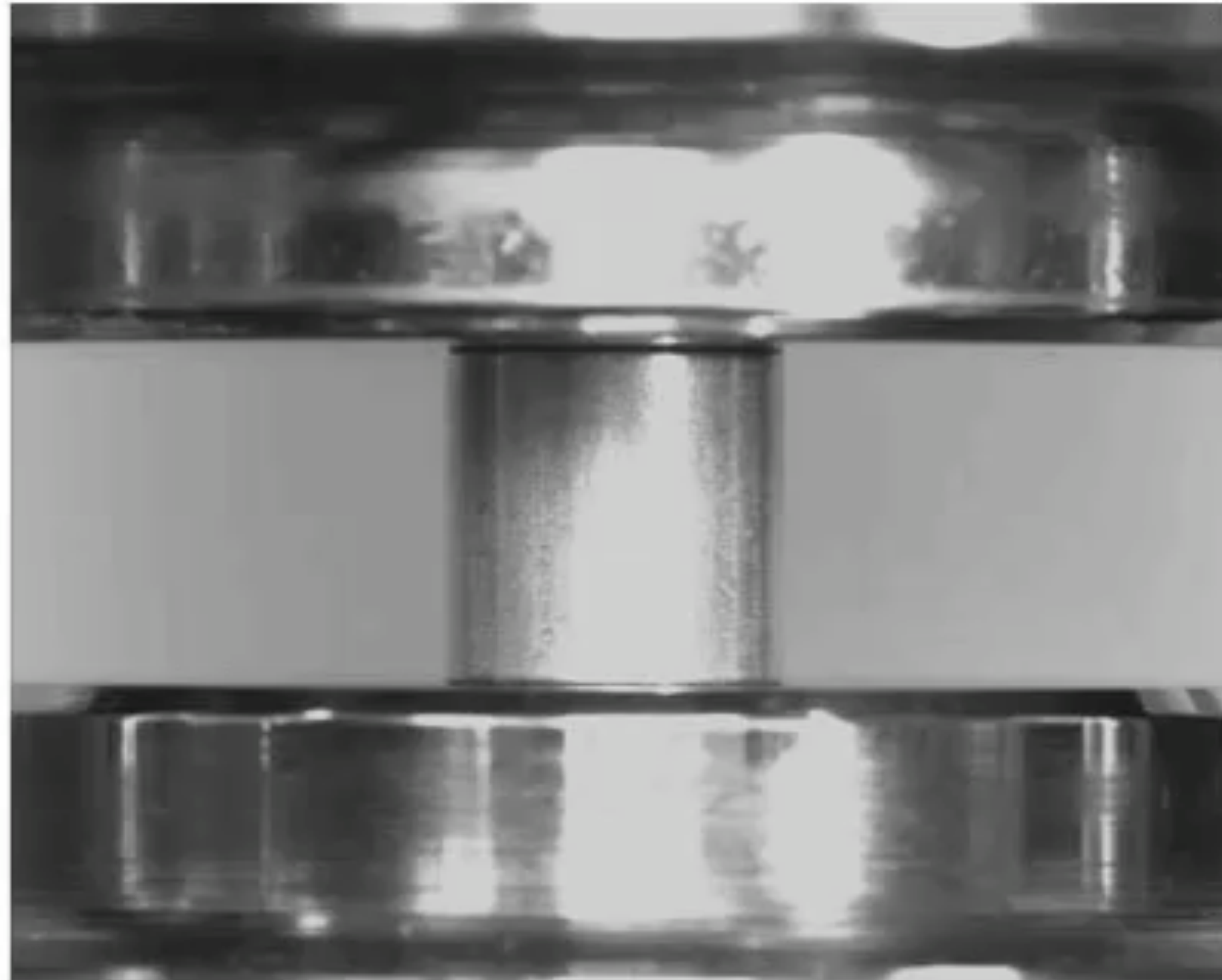


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Upsetting with Friction

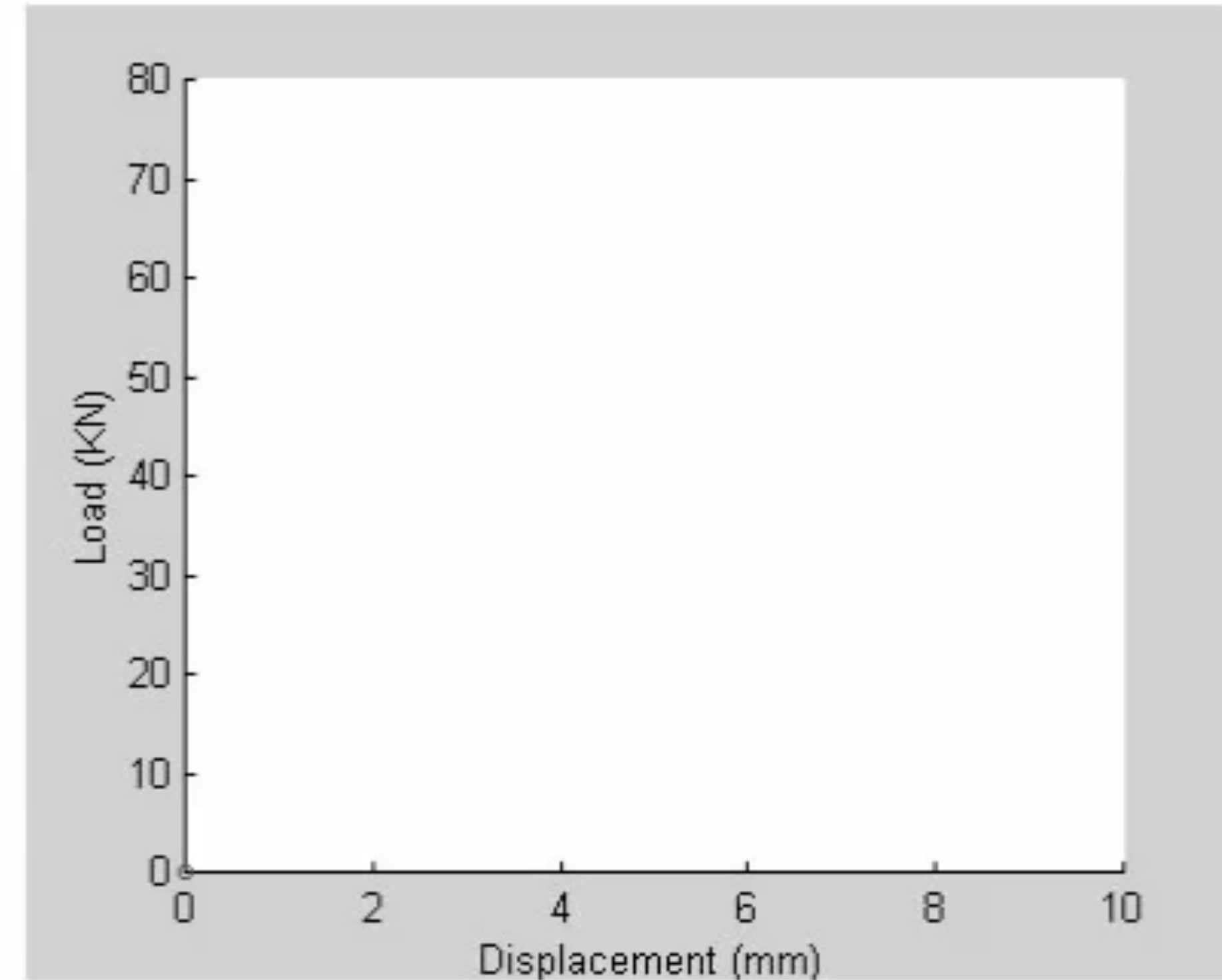
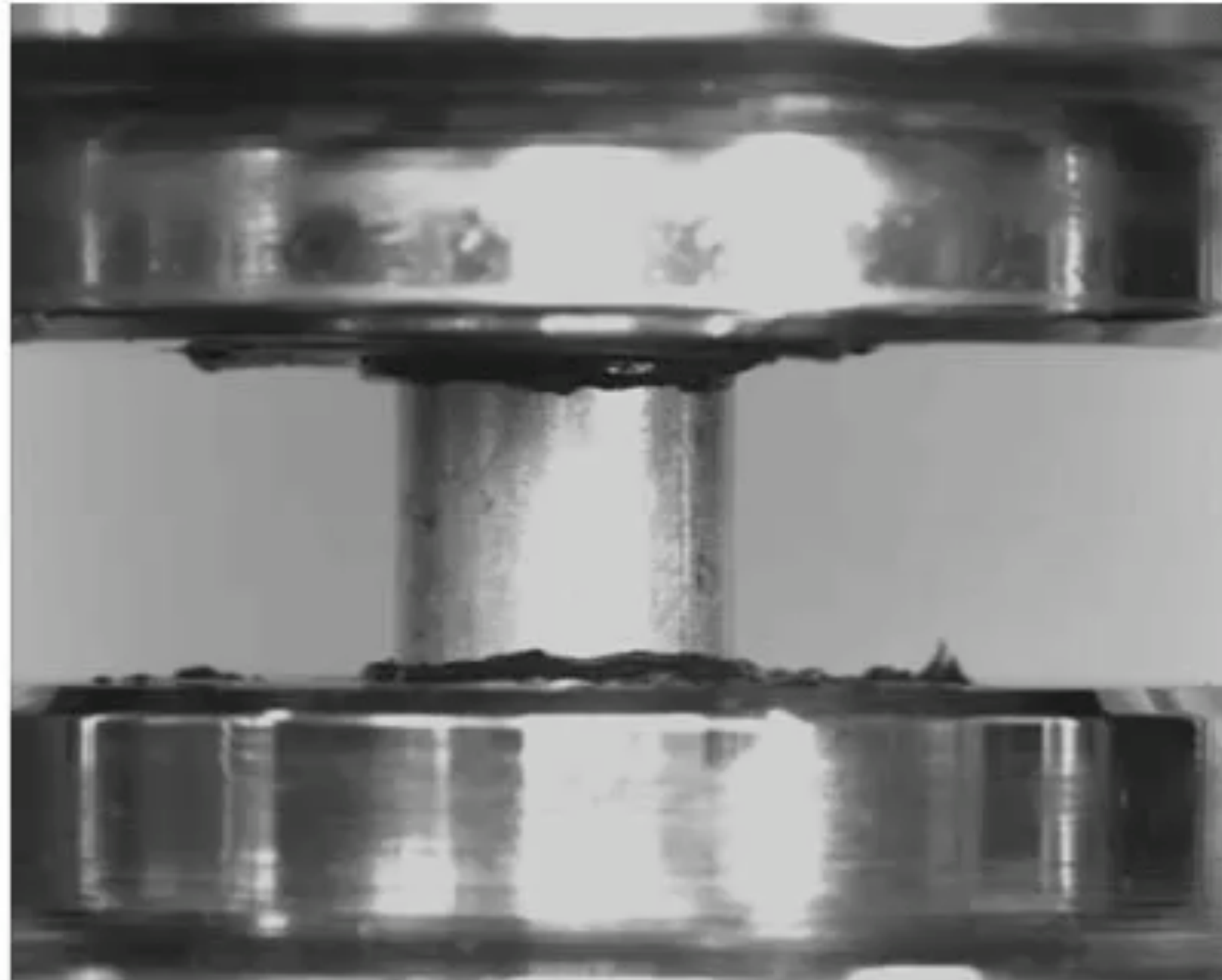


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Upsetting without Friction

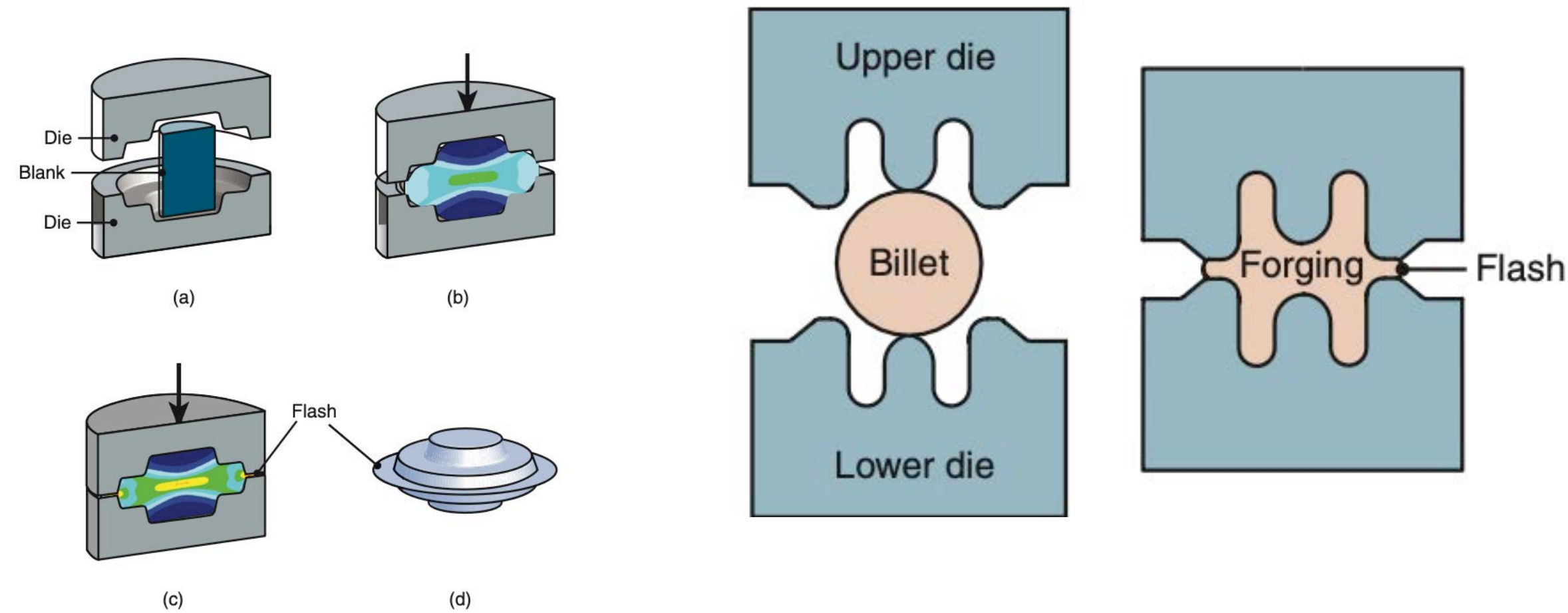


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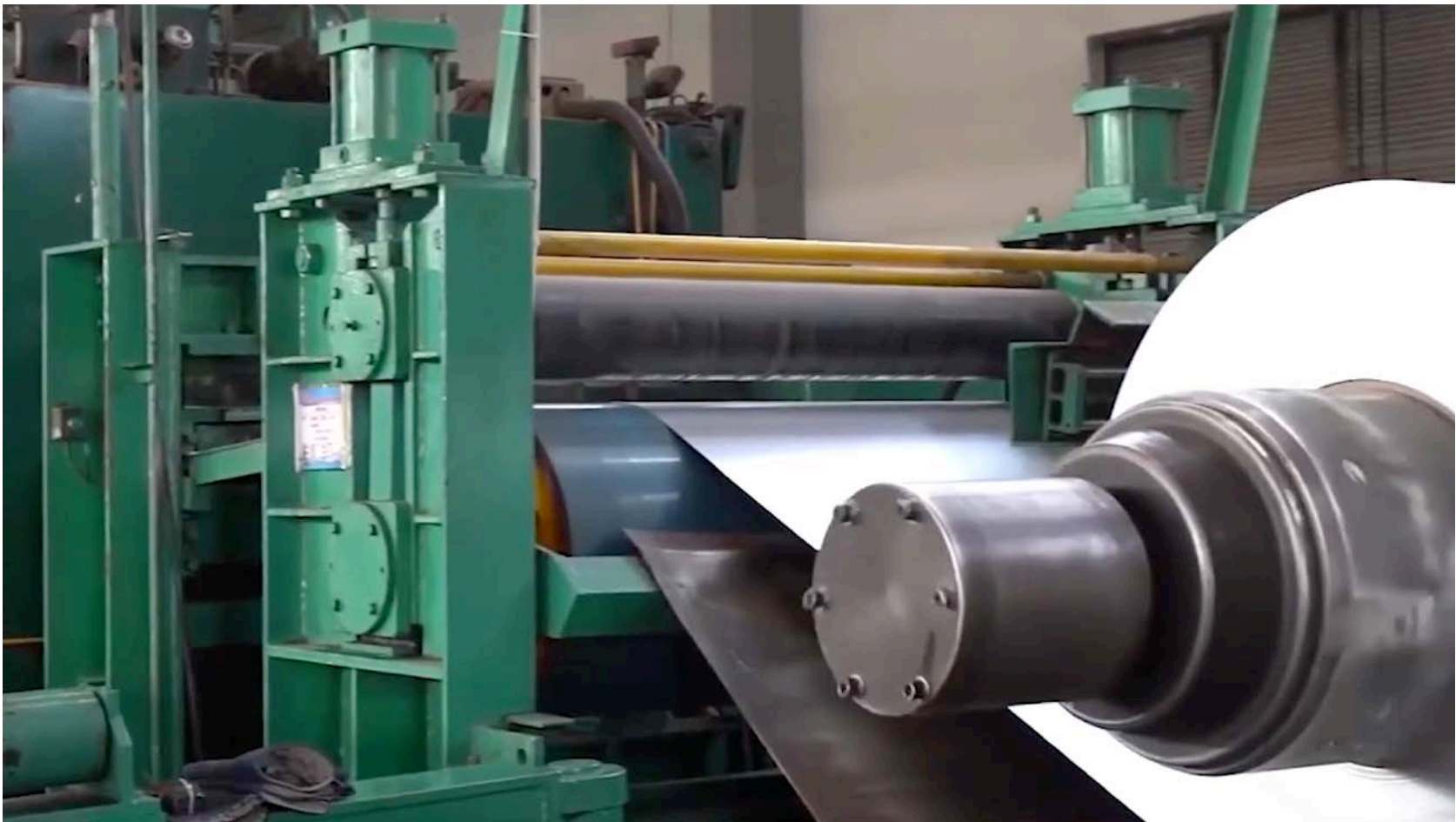
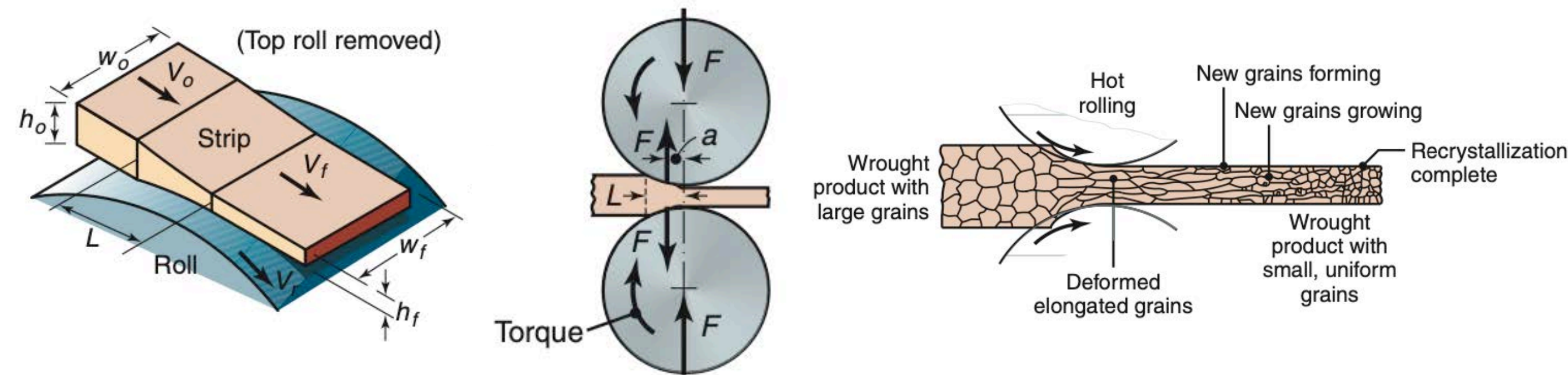
Forging, Extrusion, Sheet Metal: Processes and Equipment

Common Bulk Processes

Forging



Rolling



Deforming

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Microstructure: Grain Size

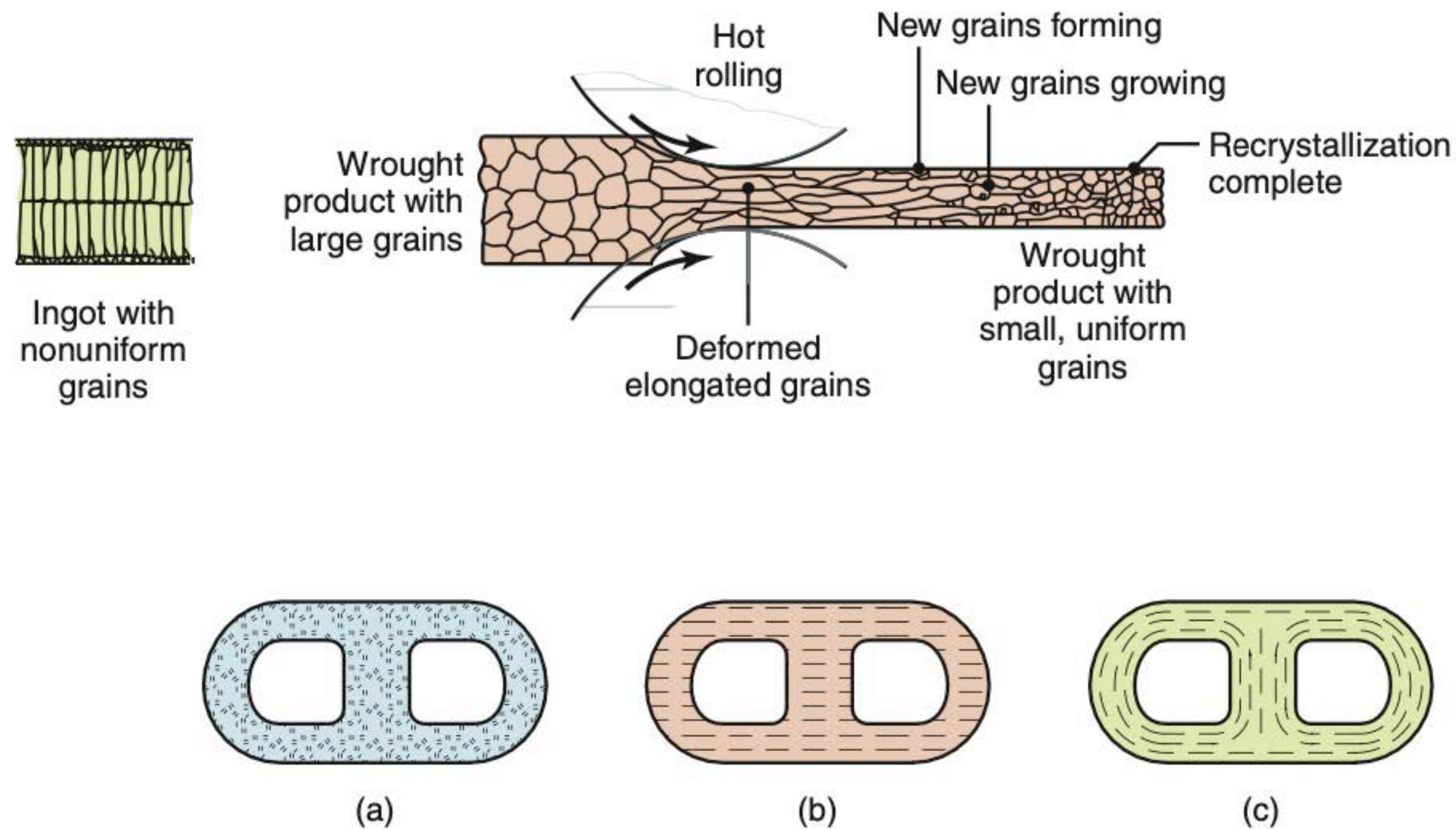


Figure 14.2: Schematic illustration of a part (dragline chain link, approximately 2-m long) made by three different processes and showing grain flow. (a) Casting by the processes described in Chapter 11. (b) Machining from a blank, described in Part IV of this book, and (c) forging. Each process has its own advantages and limitations regarding external and internal characteristics, material properties, dimensional accuracy, surface finish, and the economics of production. *Source:* Courtesy of the Forging Industry Association.

material properties affected by grain size:

- strength
- hardness
- ductility

Hall-Petch model: smaller grains give higher strength

σ_0 = stress to start dislocation movement

k_y = material hardening constant

d = grain size

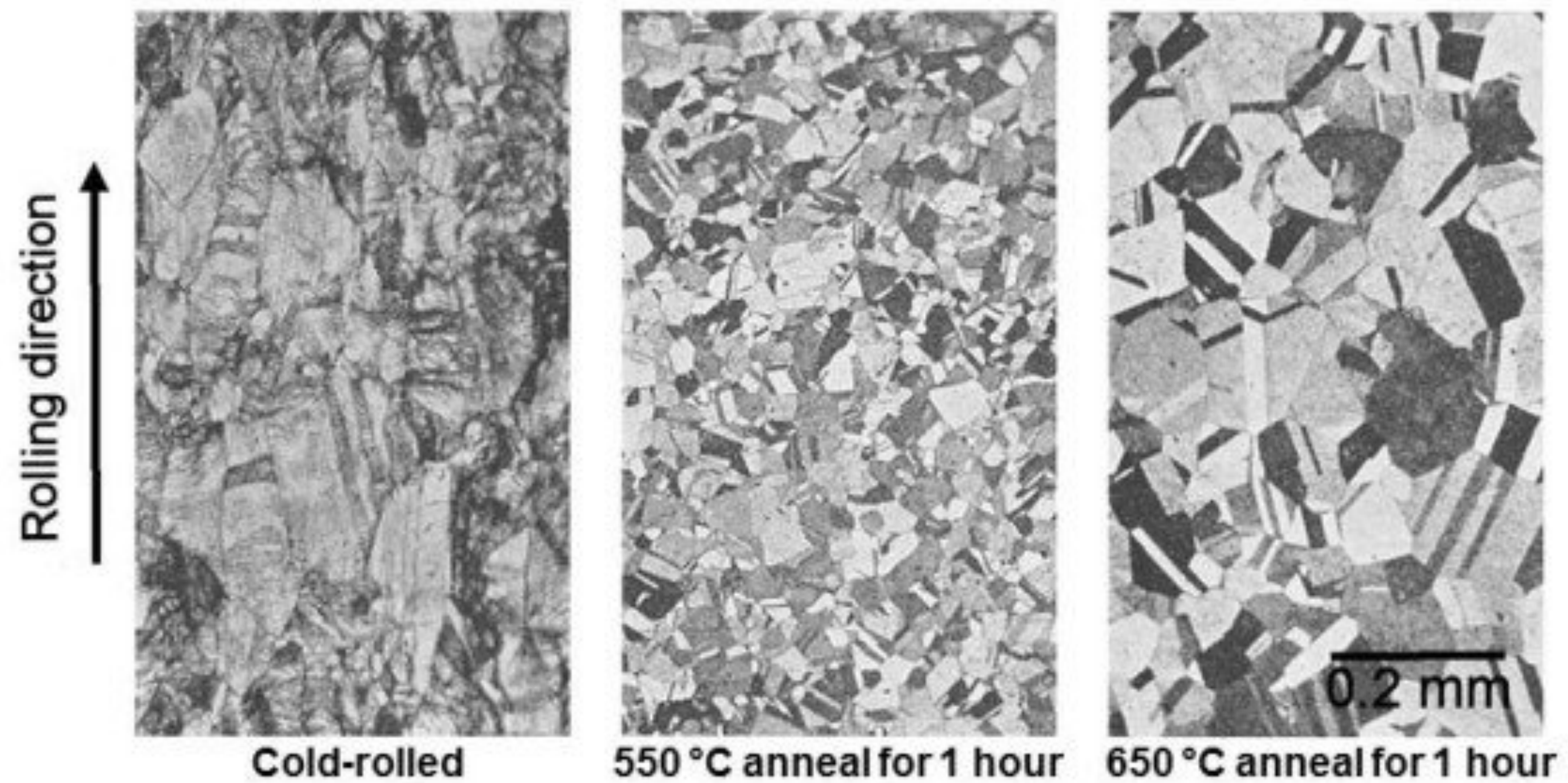
$$\sigma_y = \sigma_o + \frac{k_y}{\sqrt{d_{\text{grain}}}}$$

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Recrystallization



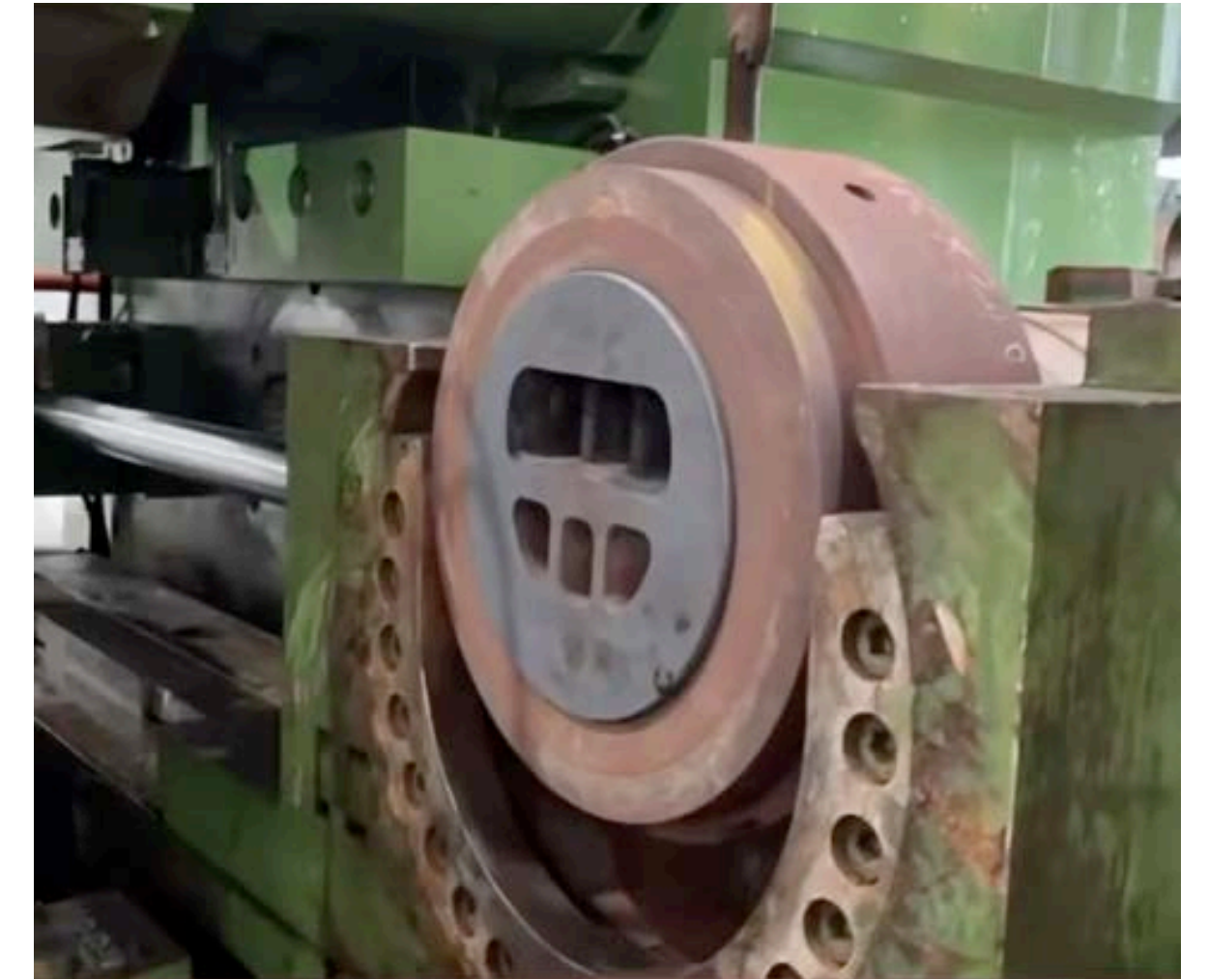
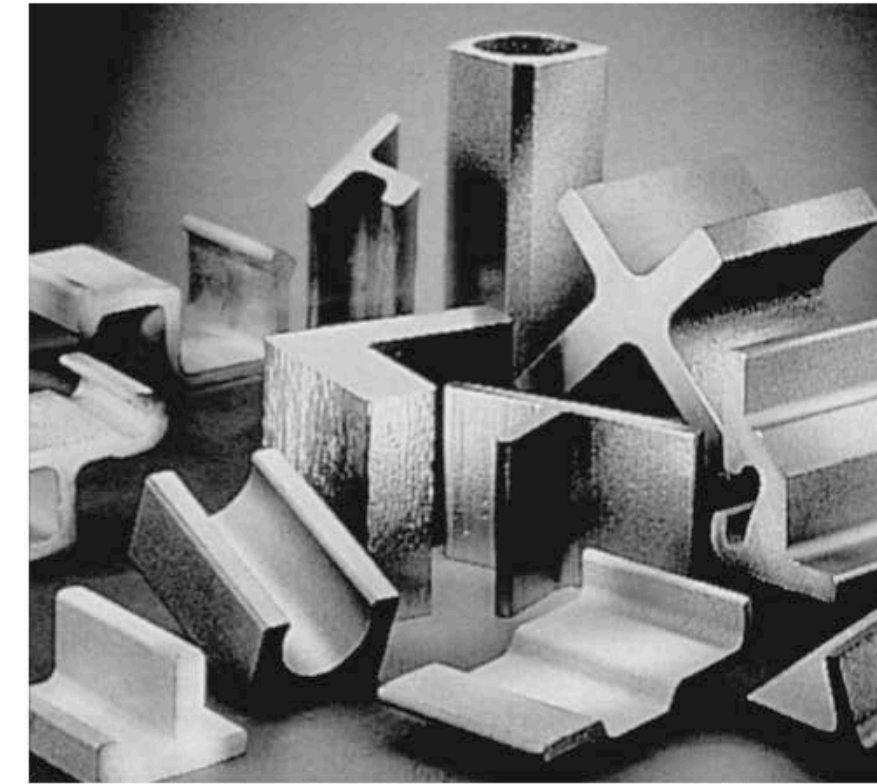
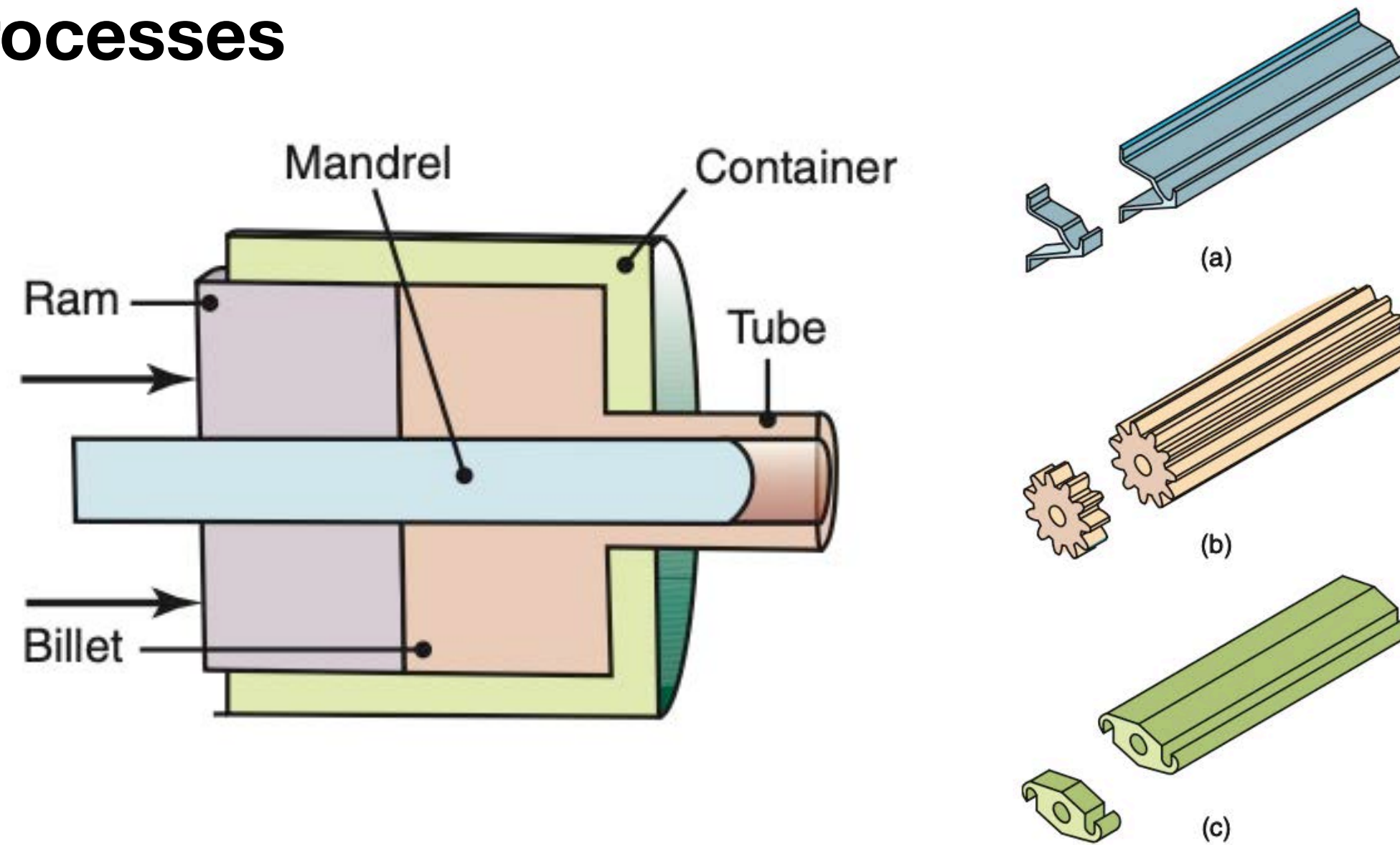
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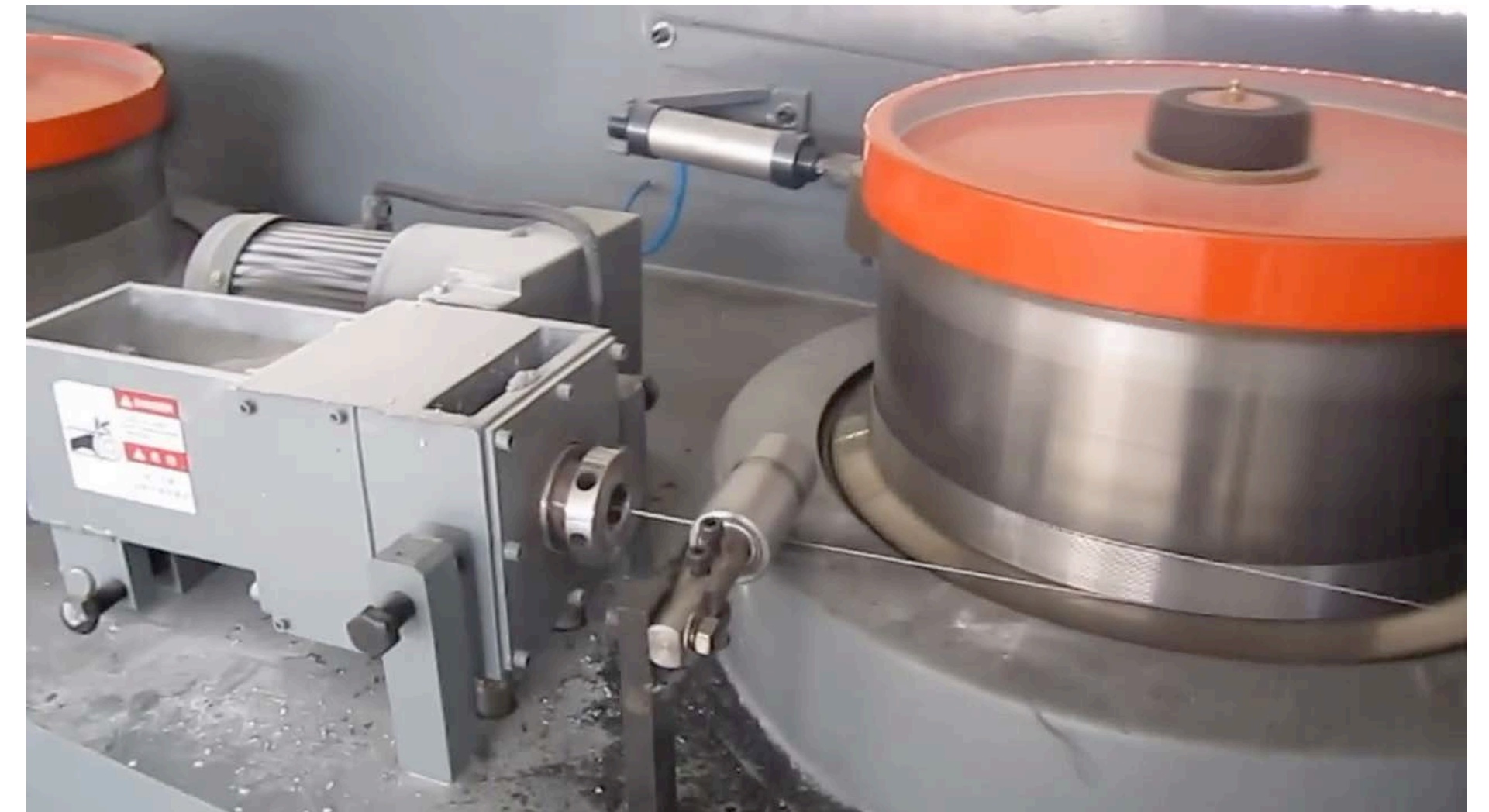
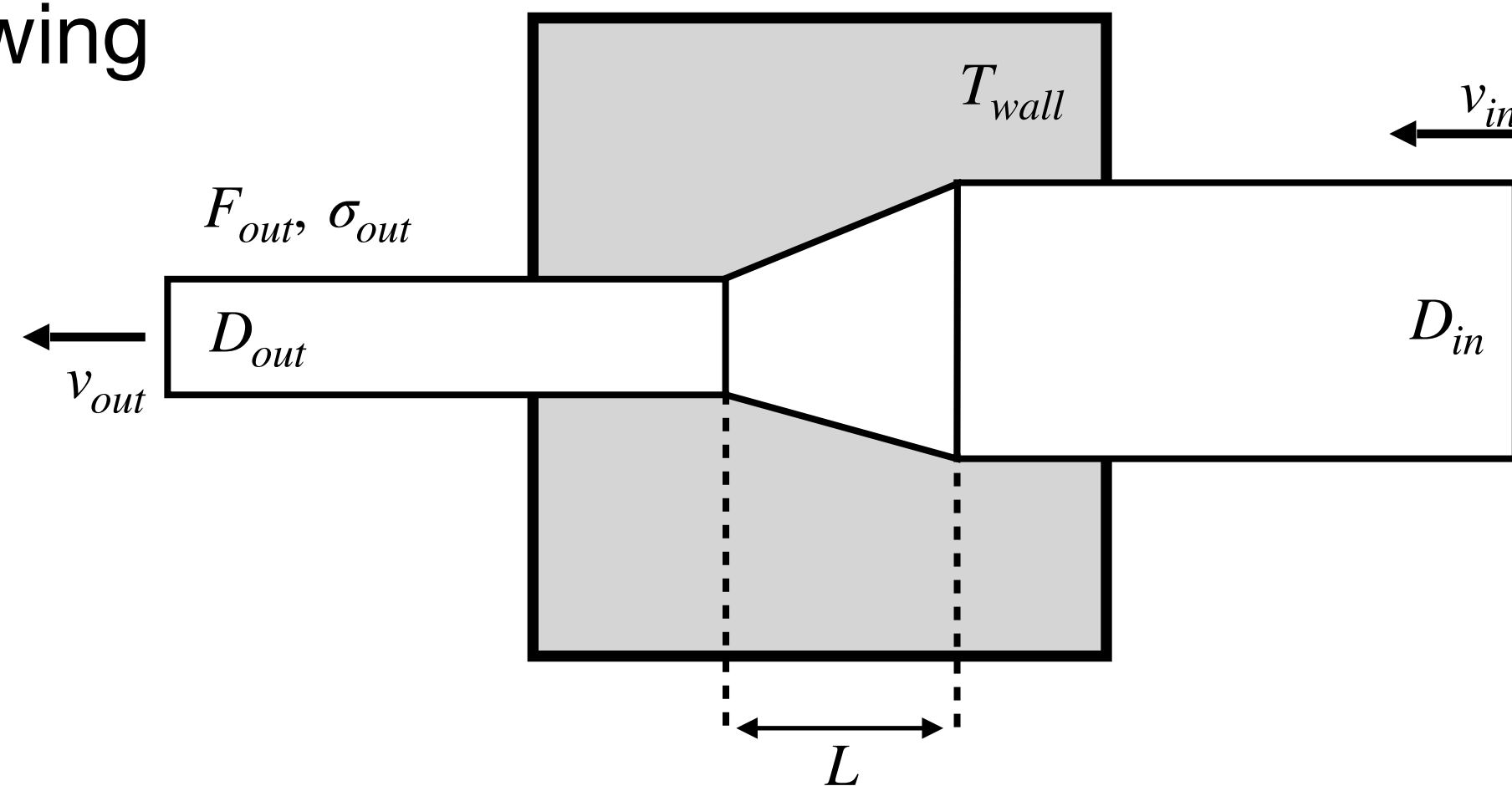
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Common Processes

Extrusion



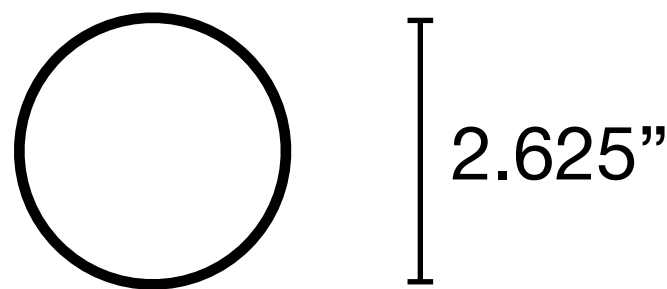
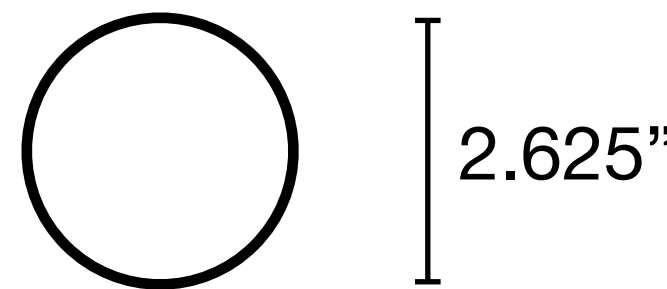
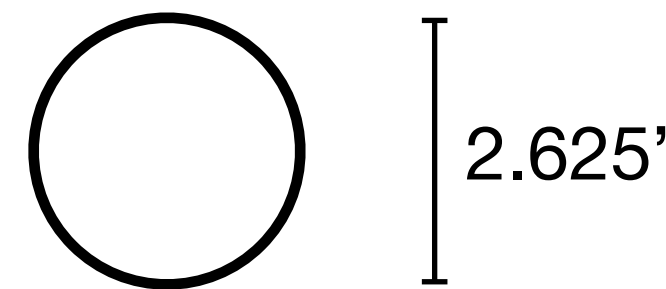
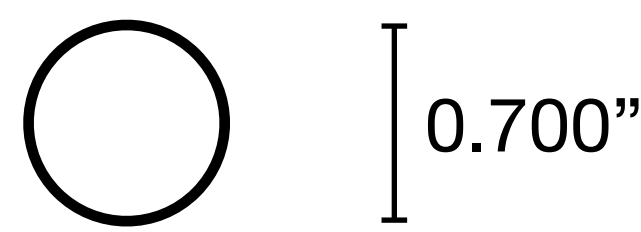
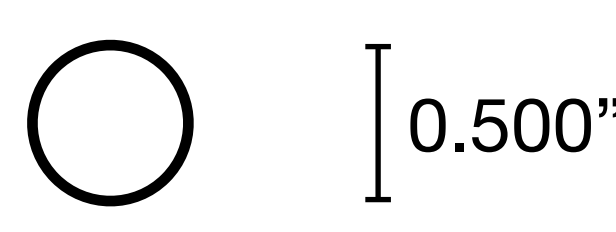
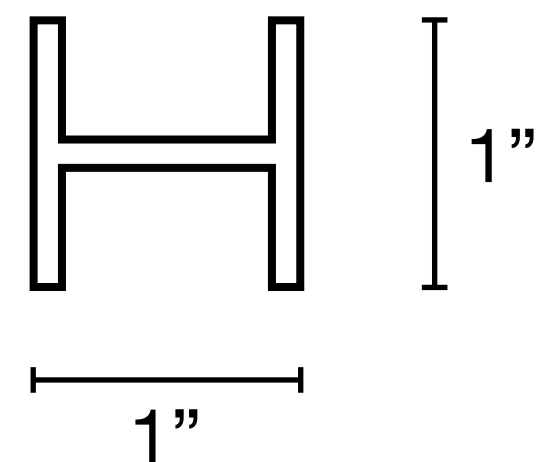
Drawing



Deforming

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Extrusion Demo

	Trial #1	Trial #2	Trial #3
Initial Shape			
Final Shape			
Final Area	0.4 in ²	0.2 in ²	~0.2 in ²



Deforming

Forging, Extrusion, Sheet Metal: Processes and Equipment

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DFM for Deforming

parting line + flash handling

draft angles to eject part

avoid sharp corners to fill appropriately

lubrication

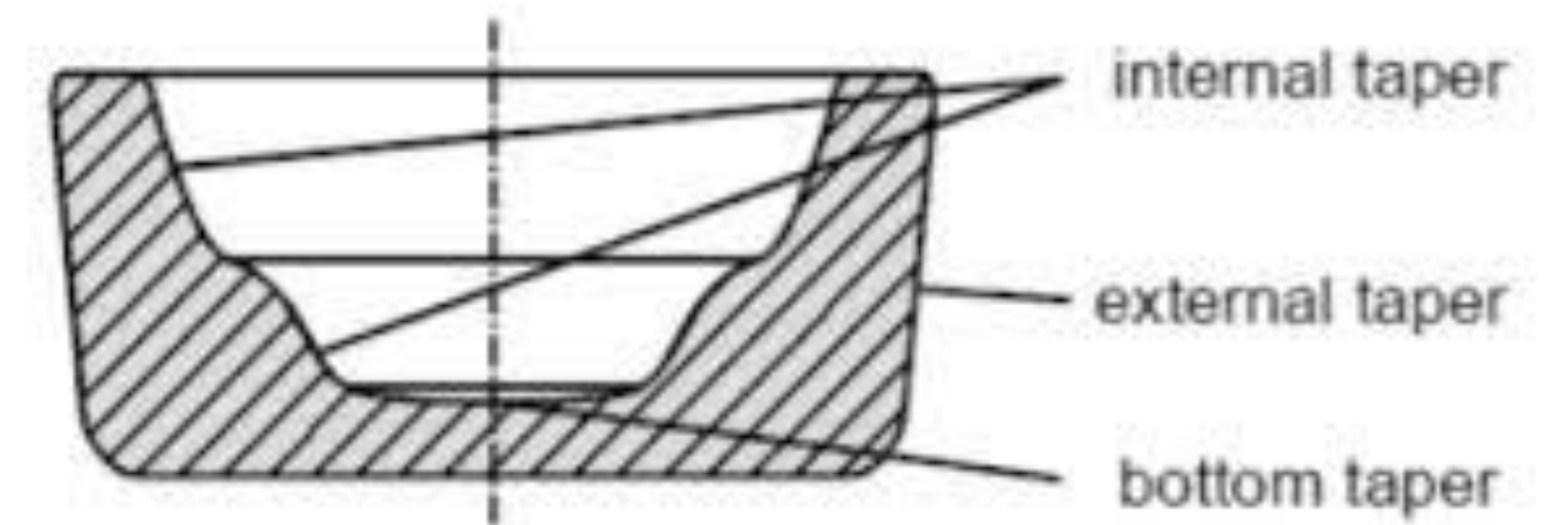
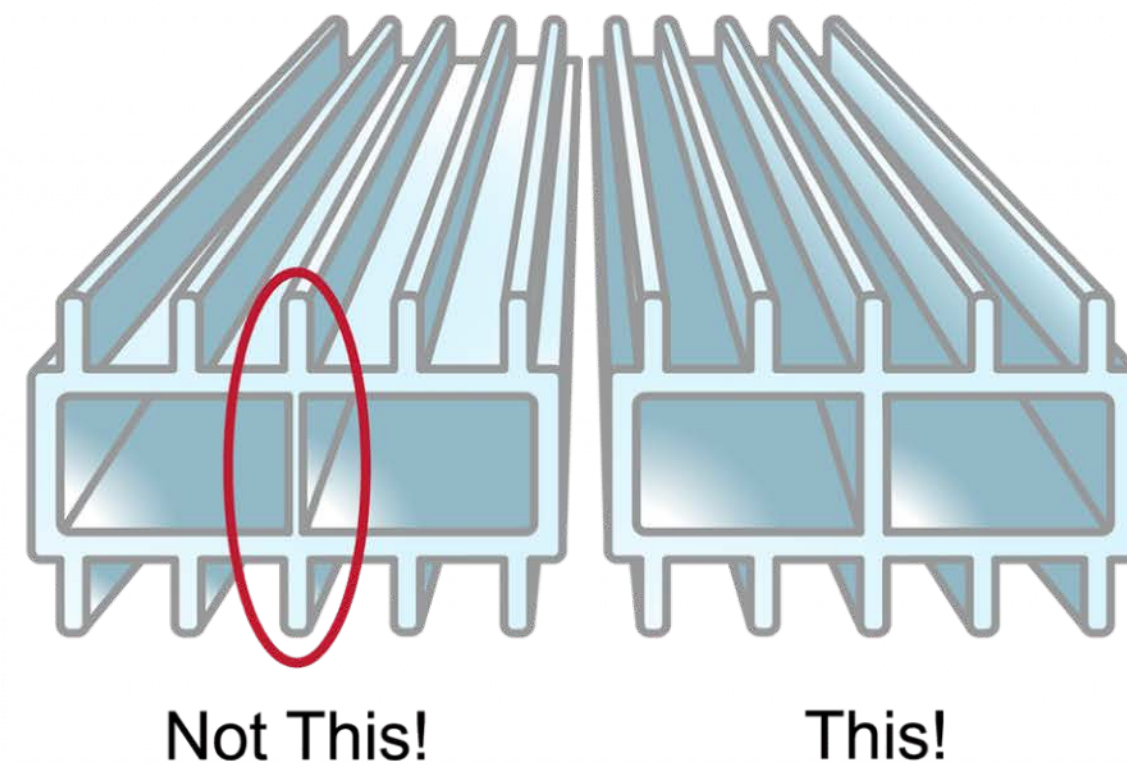
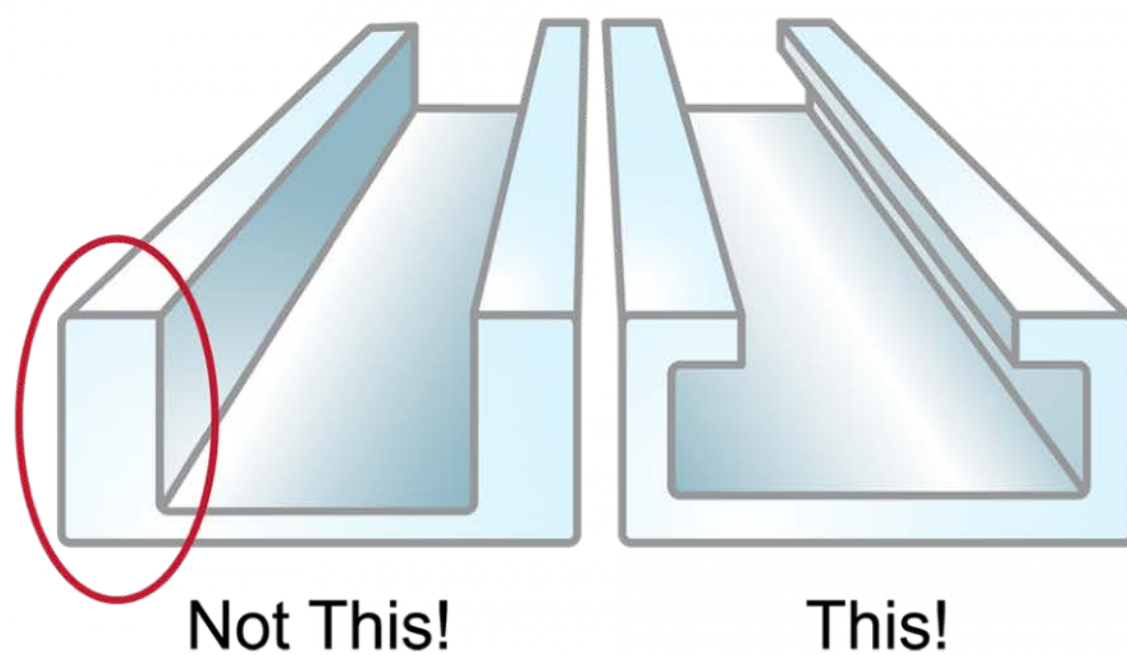
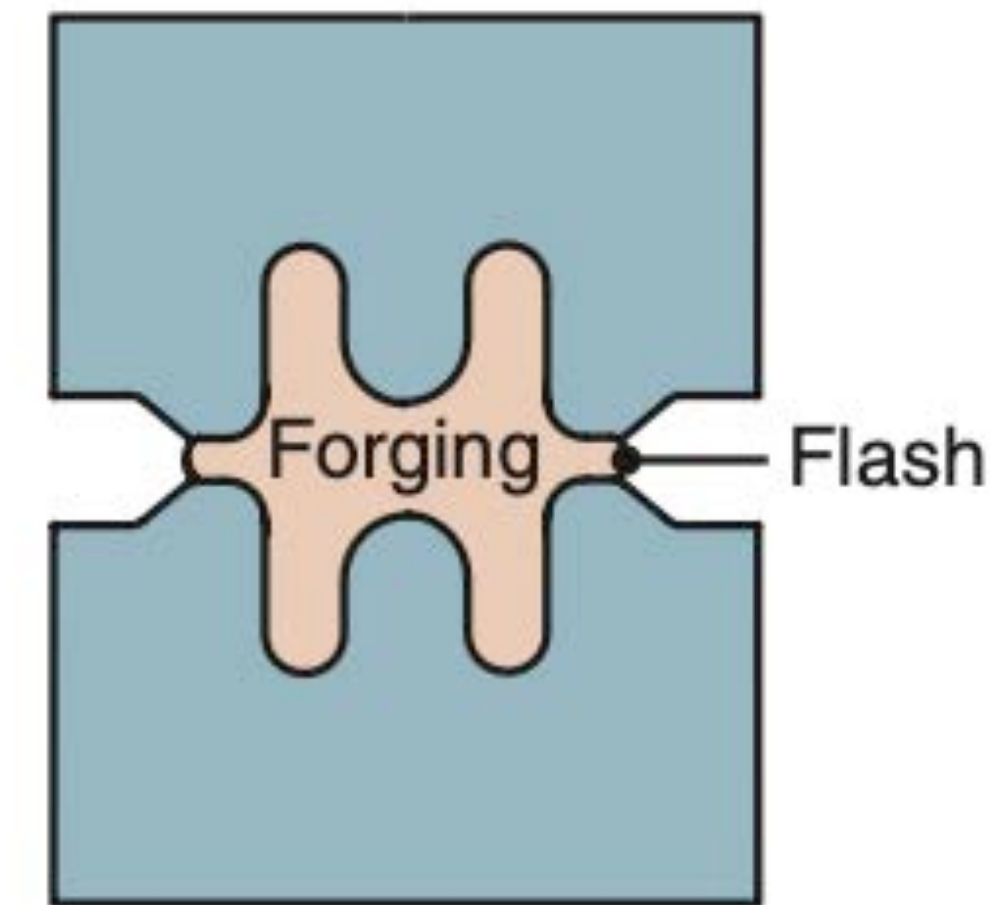
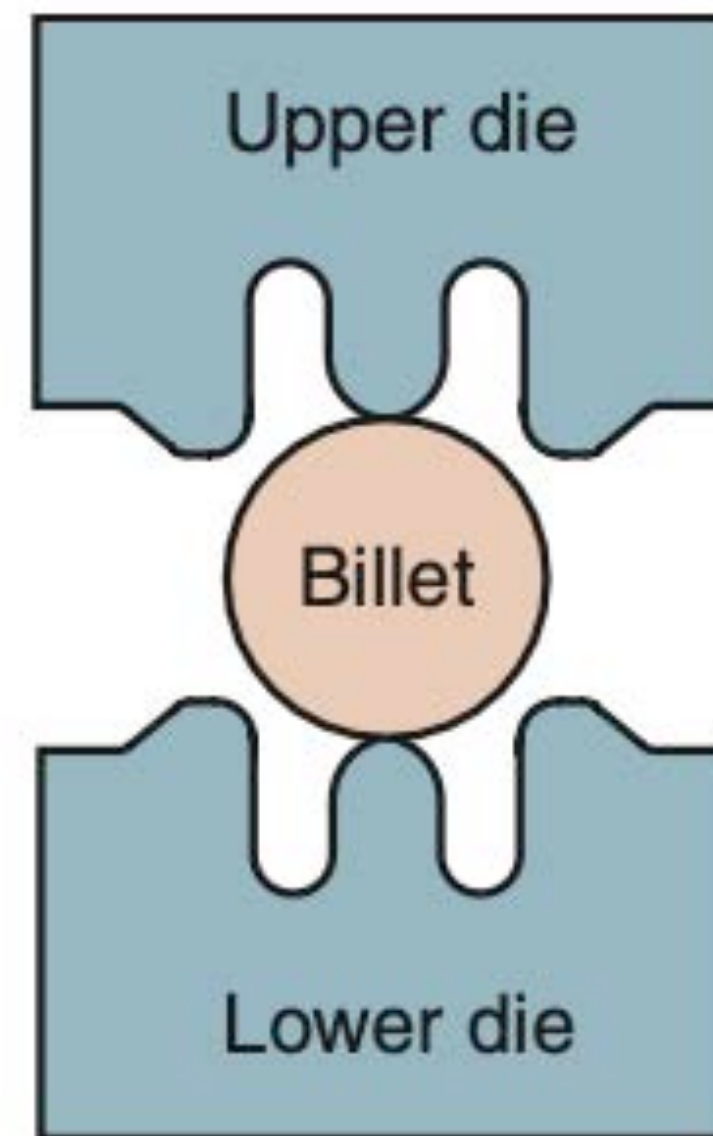


Illustration of Draft

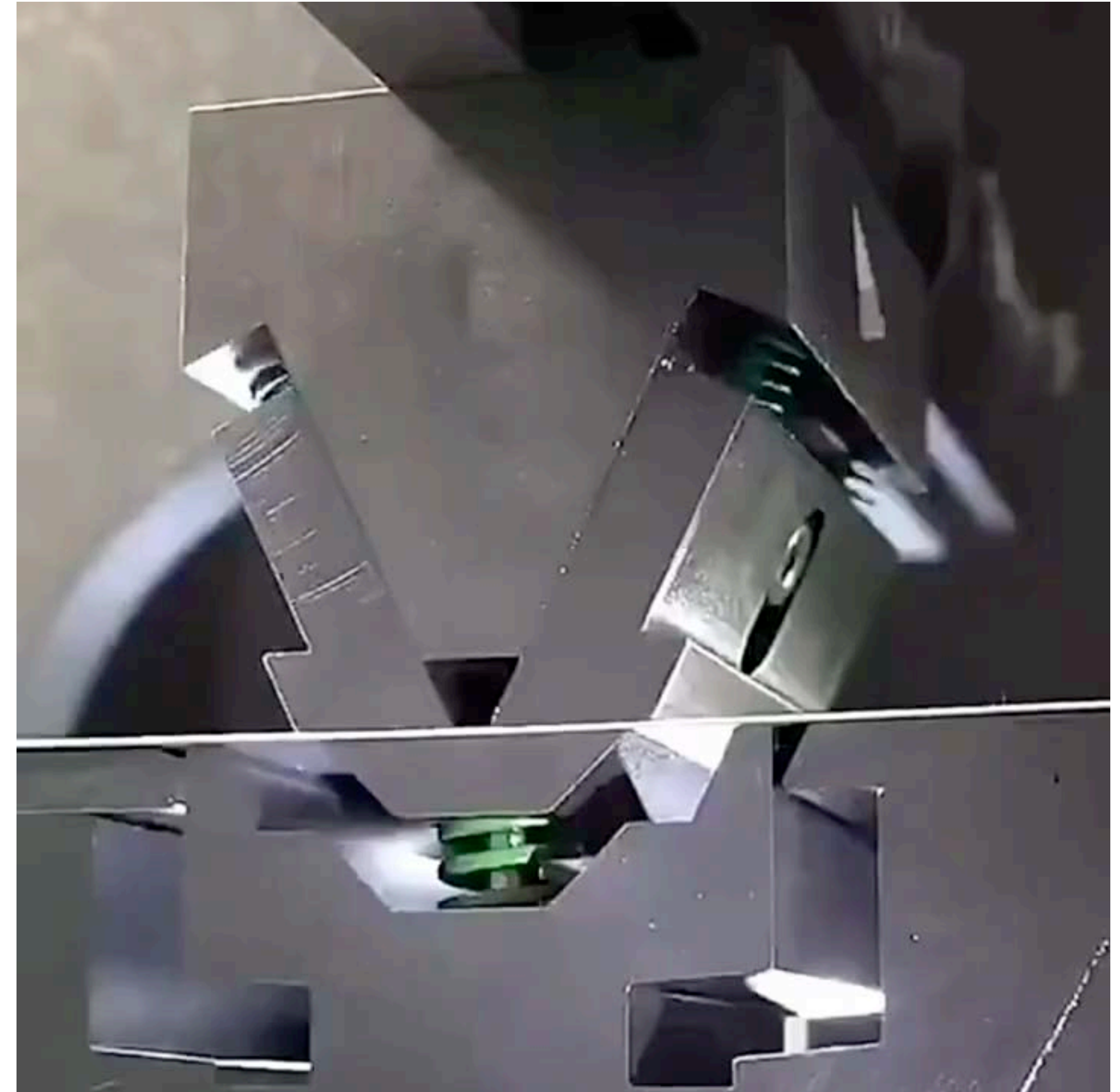
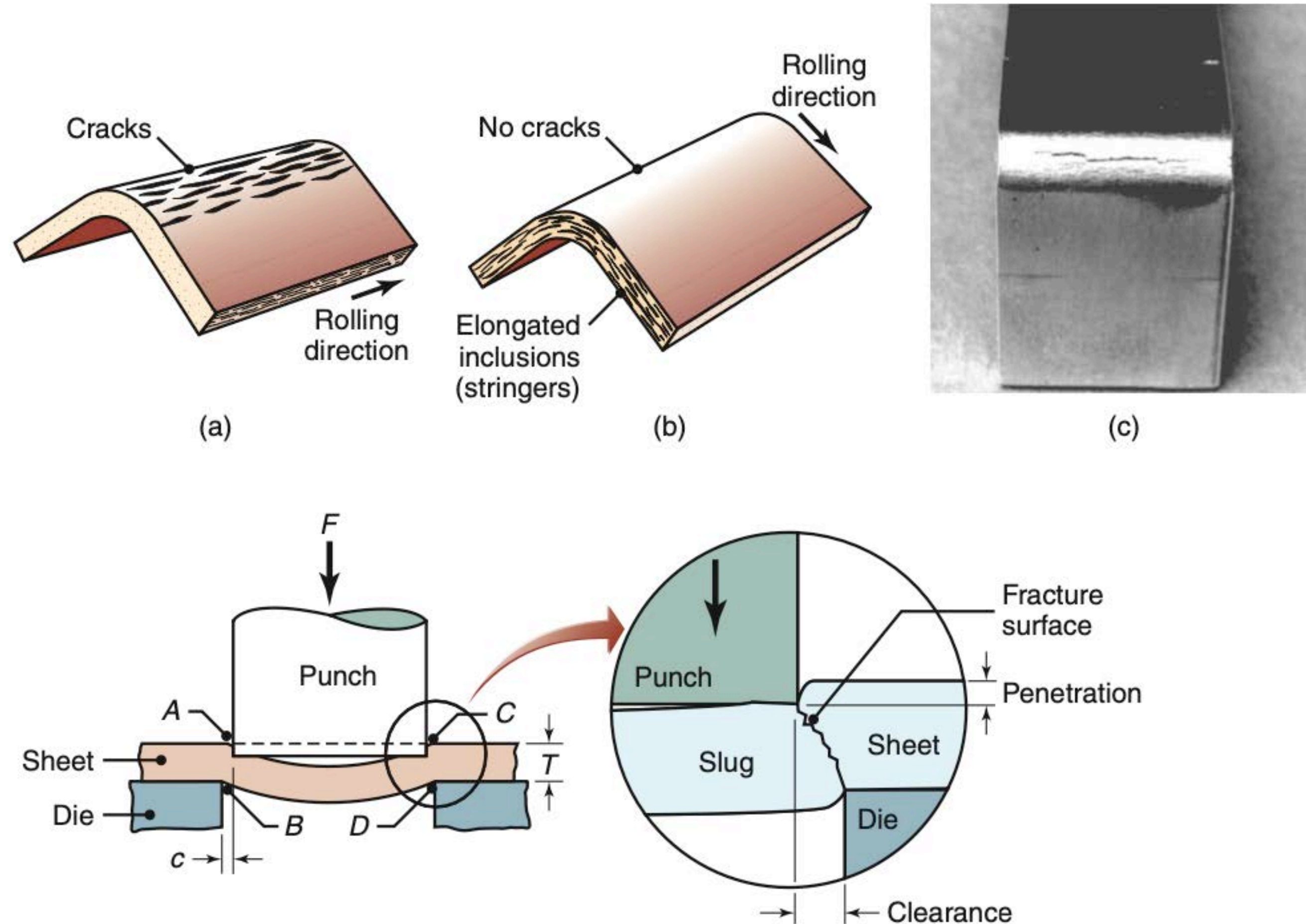
Deforming

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Common Sheet Forming Processes

Sheet Metal Bending/Stamping



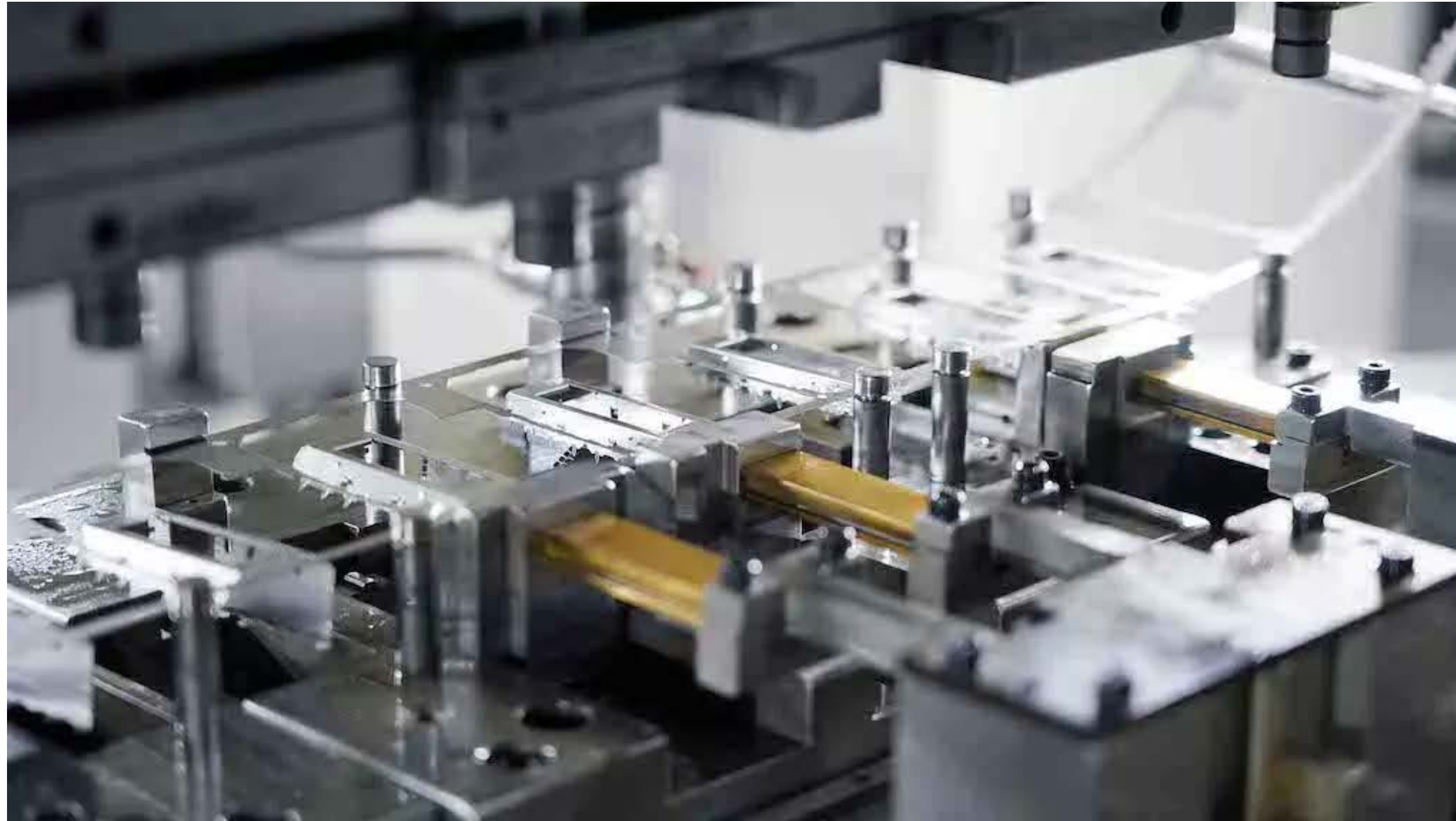


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Sheet Metal Forming



Sheet metal concerns

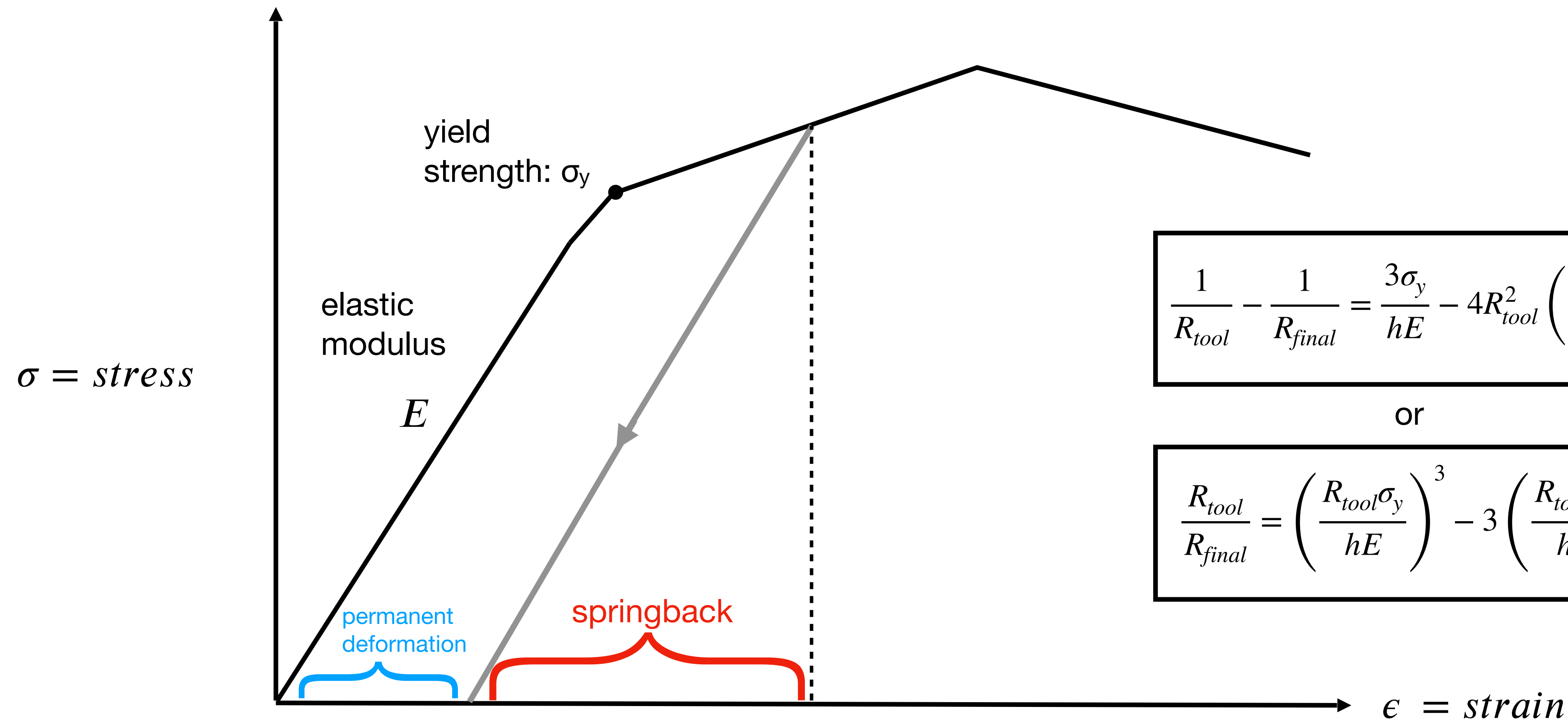
- springback
- cracking

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Forging, Extrusion, Sheet Metal: Processes and Equipment

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Sheet Metal Bending



$$\frac{1}{R_{tool}} - \frac{1}{R_{final}} = \frac{3\sigma_y}{hE} - 4R_{tool}^2 \left(\frac{\sigma_y}{hE} \right)^3$$

what will the springback amount be?
(evaluate it or eliminate it)

or

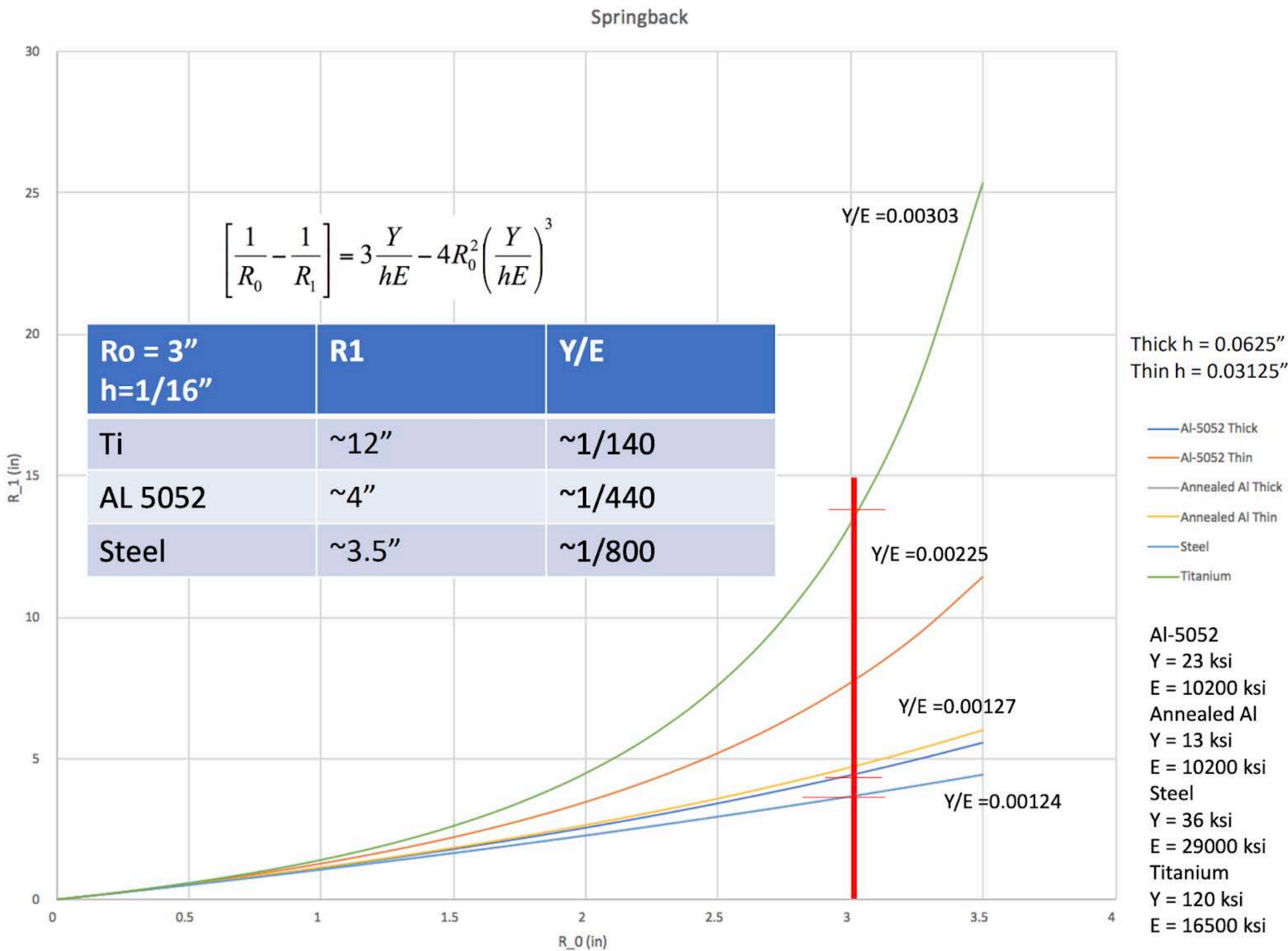
$$\frac{R_{tool}}{R_{final}} = \left(\frac{R_{tool}\sigma_y}{hE} \right)^3 - 3 \left(\frac{R_{tool}\sigma_y}{hE} \right) + 1$$

what will the final radius be?
(predict final part)

Deforming

Forging, Extrusion, Sheet Metal: Processes and Equipment

Sheet Metal Bending



$R_1 = R_{\text{final}} = R_{\text{unloaded}}$ for various metals, treatments, and thicknesses



$Y = \sigma_y$
 $R_0 = R_{\text{tool}} = R_{\text{loaded}}$
 $R_1 = R_{\text{final}} = R_{\text{unloaded}}$

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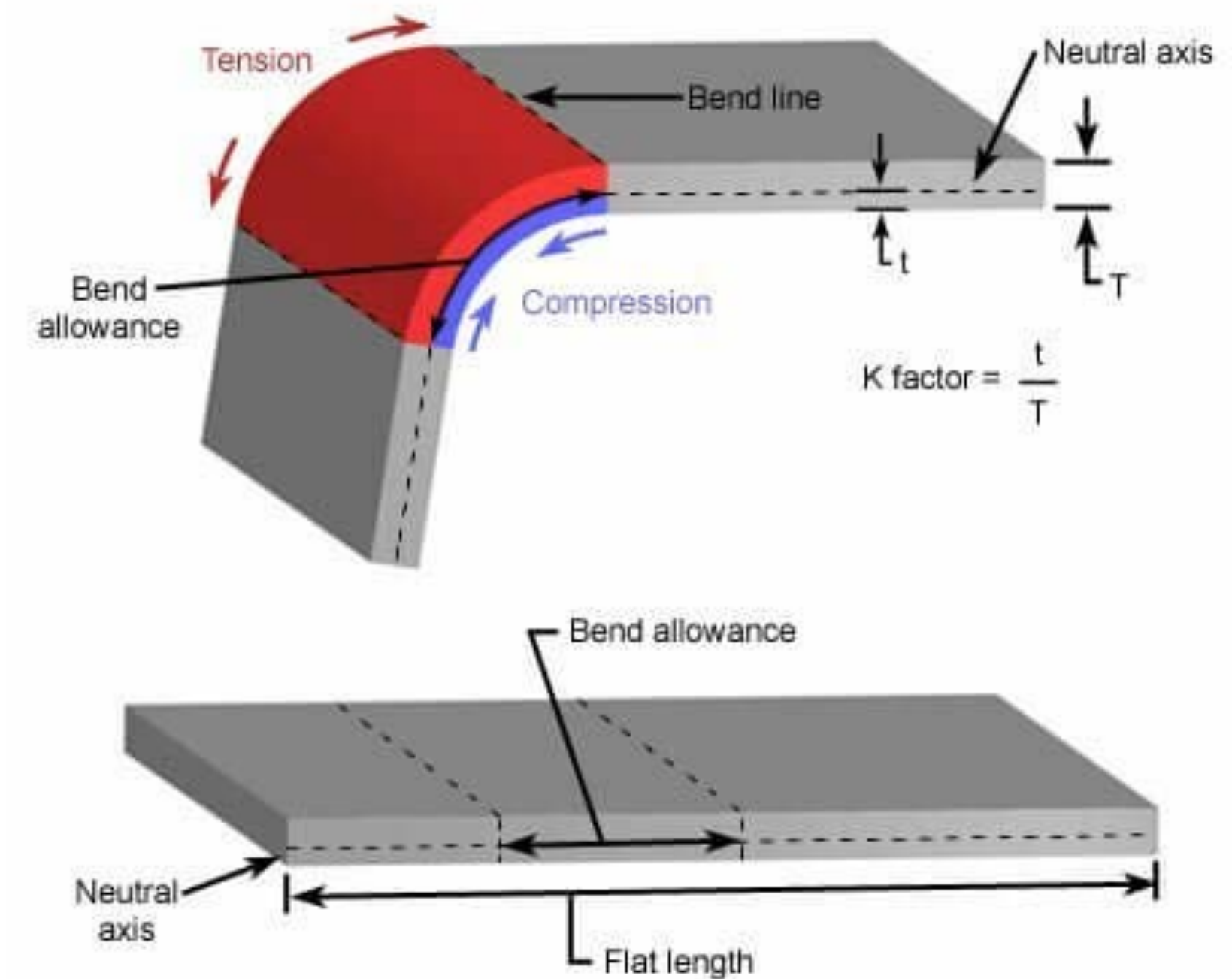
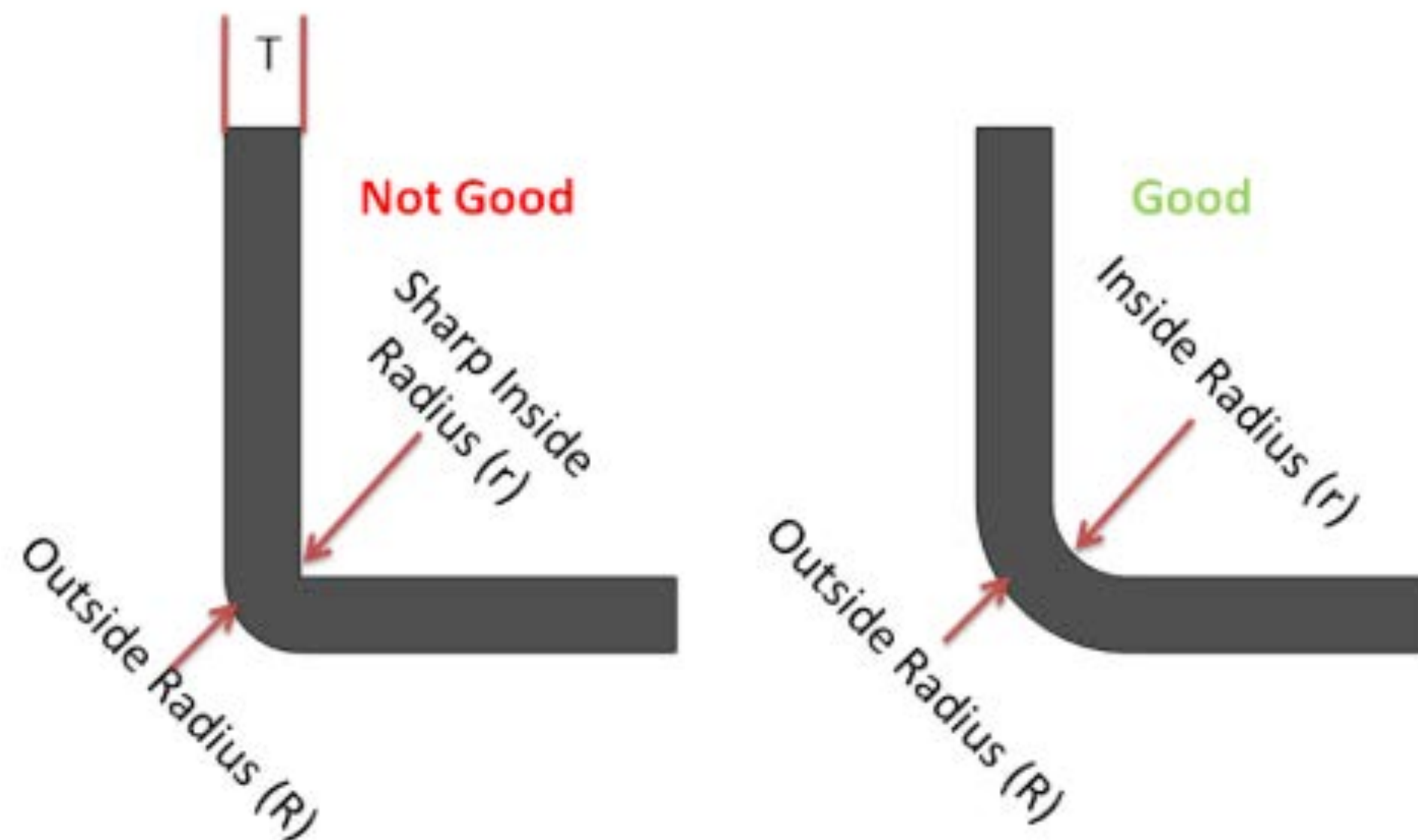
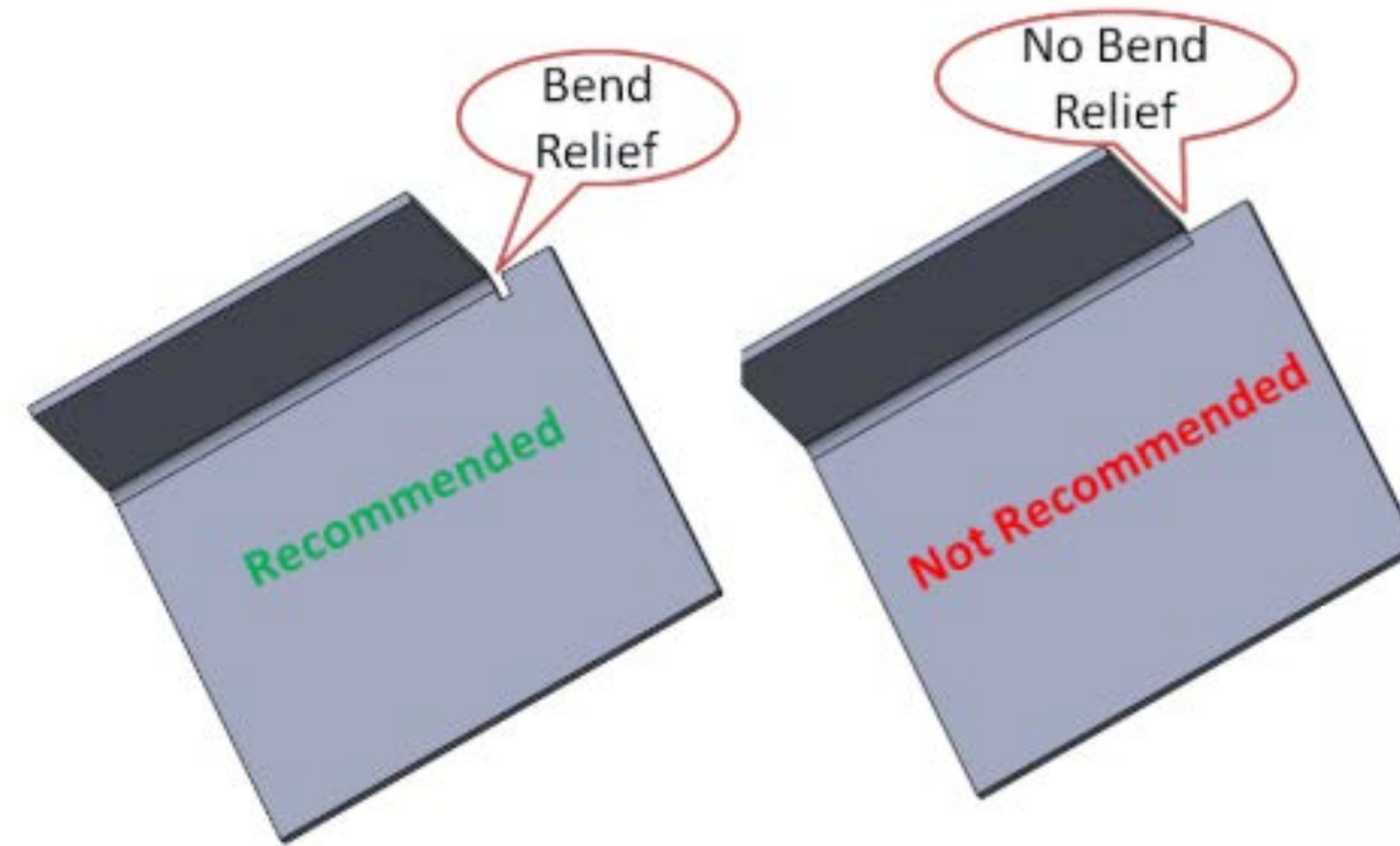
29

DFM for Sheet Metal

bending radii and allowances

springback: over-bend or stretch

bend reliefs

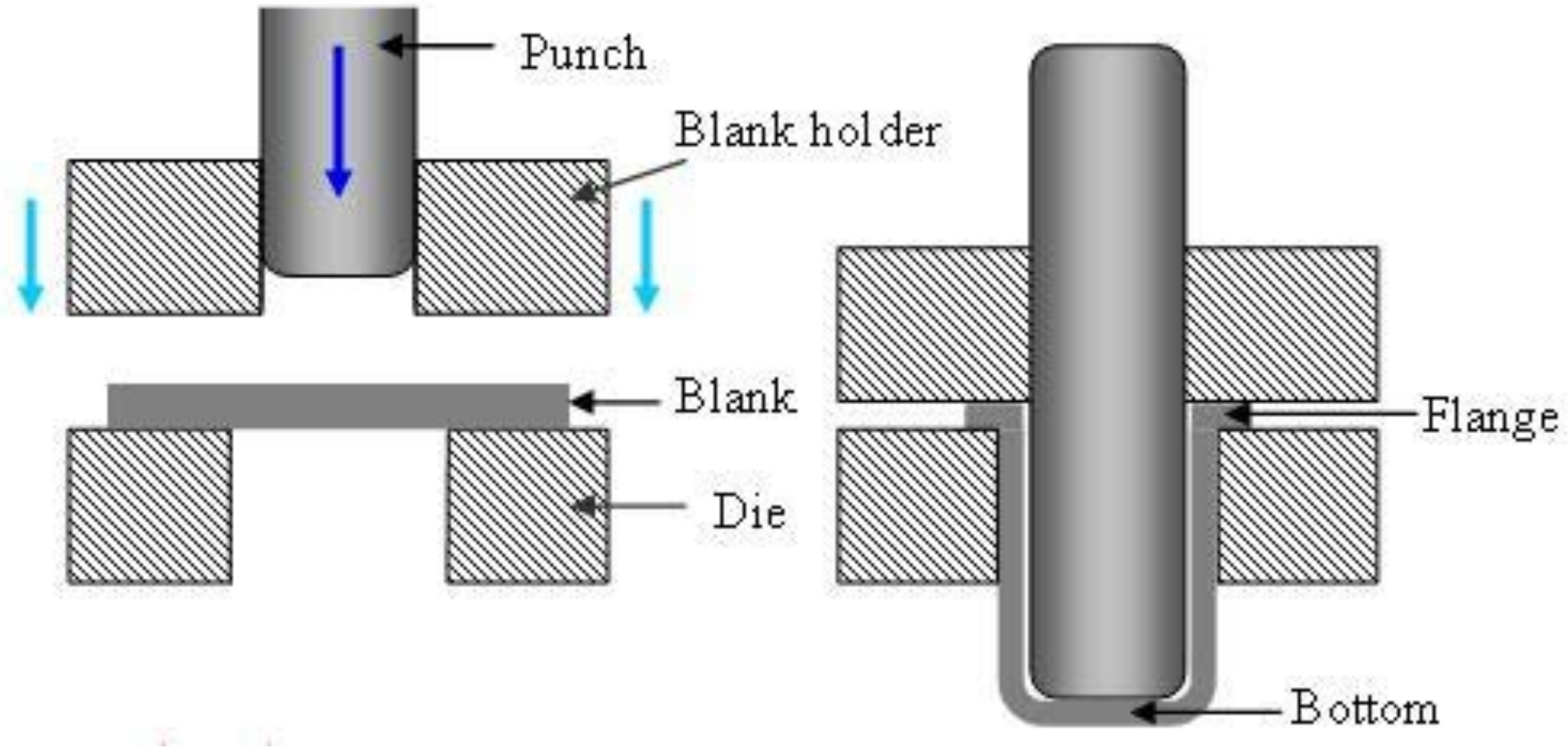


Deforming

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Stretching and Drawing



stretching: fix the flange and push down

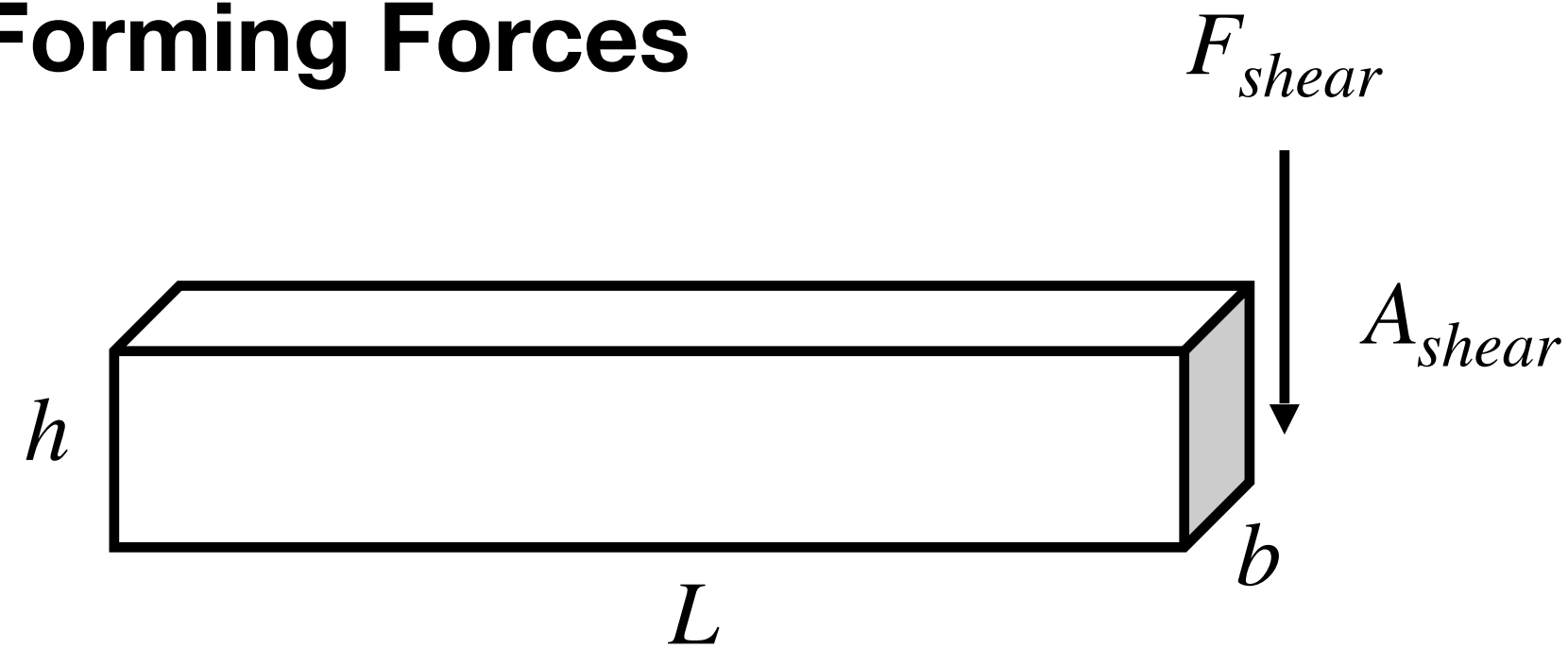
drawing: do not fix flange

Deforming

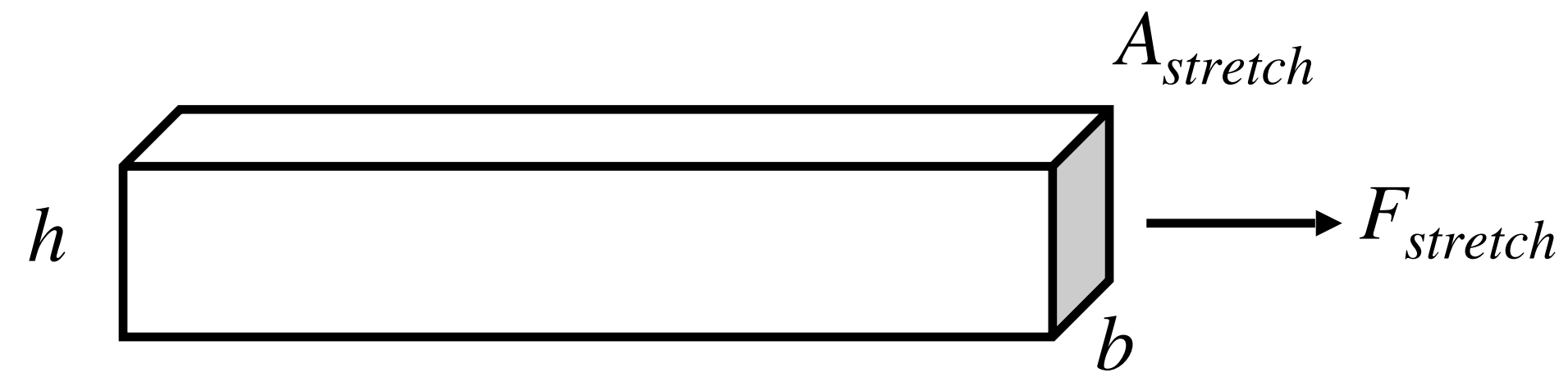
Forging, Extrusion, Sheet Metal: Processes and Equipment

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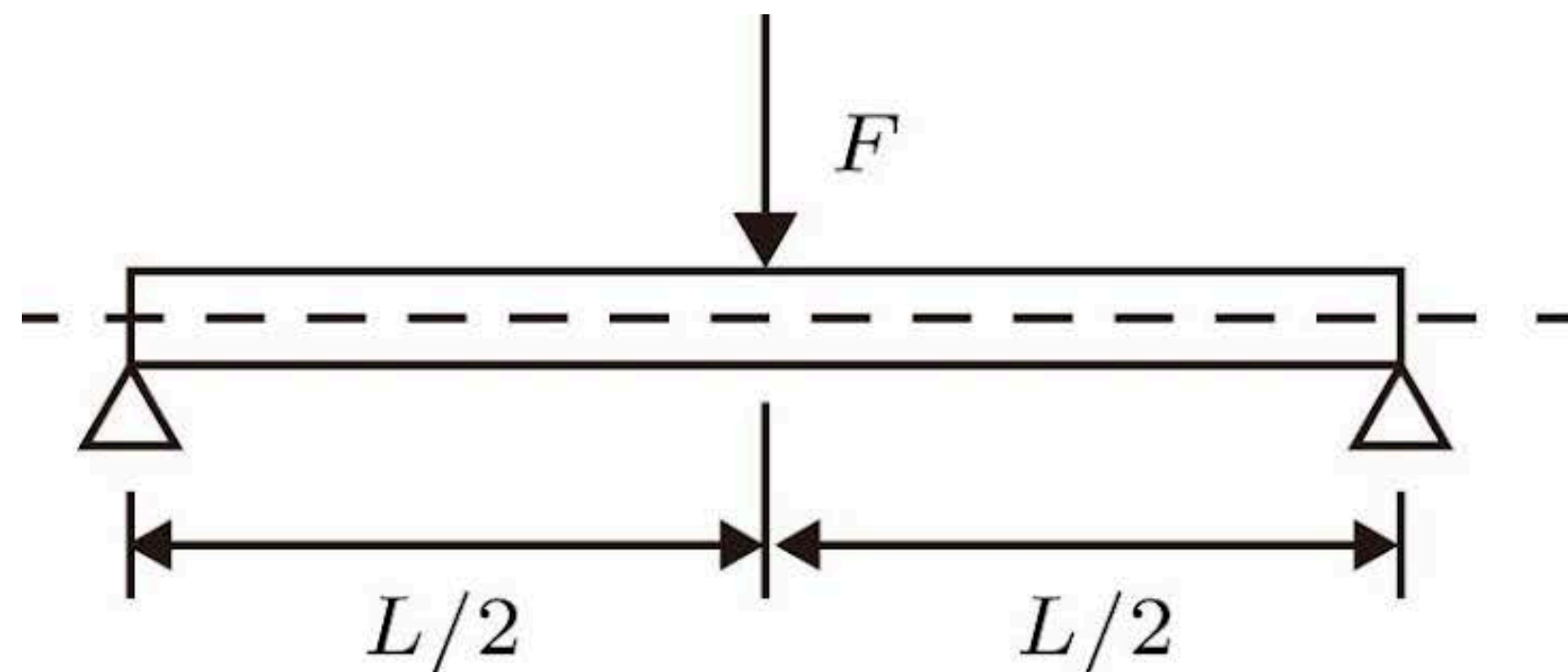
Forming Forces



$$F_{shear} = \sigma_{UTS} A_{shear} = \sigma_{UTS} b h$$



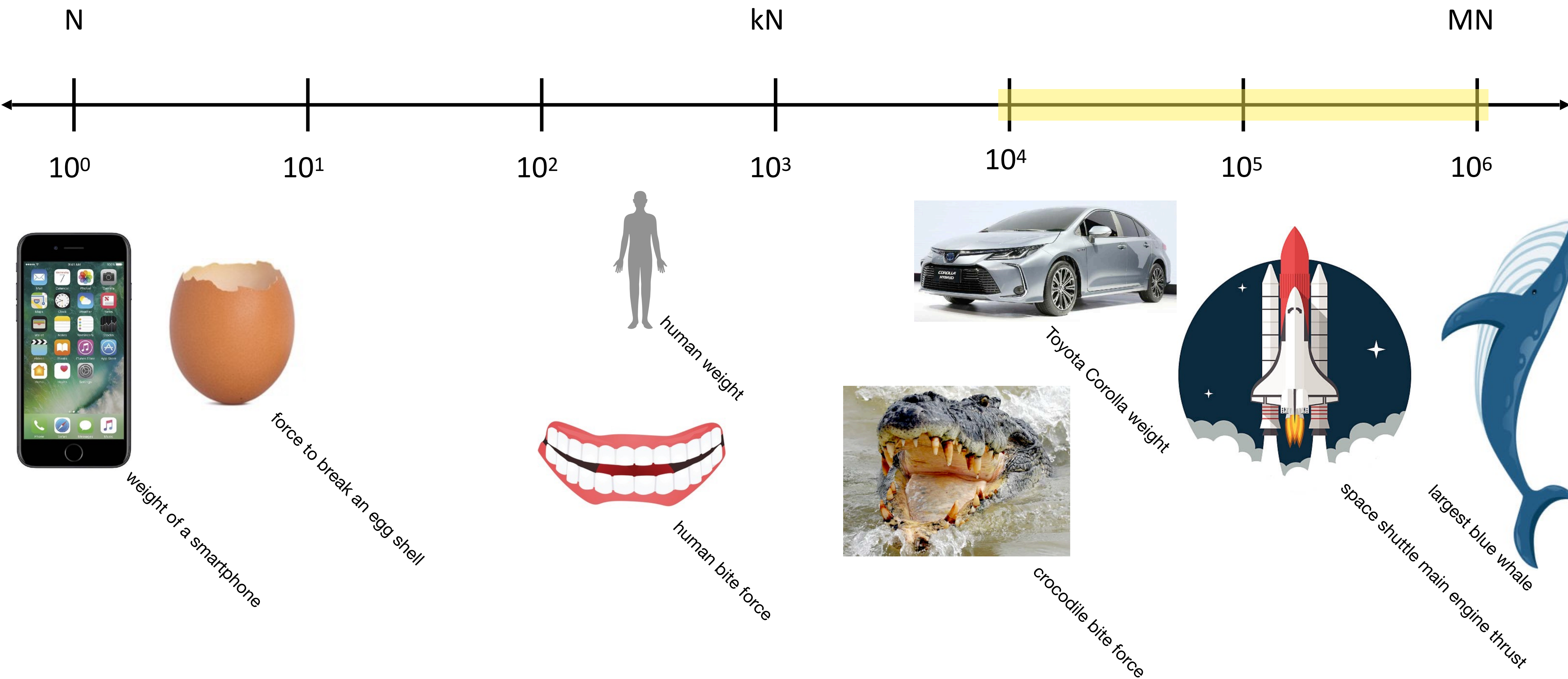
$$F_{stretch} = \text{"strength"} \cdot A_{stretch} = \frac{\sigma_{UTS} + \sigma_y}{2} b h$$



$$F_{bending} = \frac{\sigma_y b h^2}{L}$$

Deforming

Forging, Extrusion, Sheet Metal: Processes and Equipment



Deforming

Forging, Extrusion, Sheet Metal: Processes and Equipment

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Rate/Cost/Quality/Flexibility

Advantages

- net shape process: rapid formation of part
- material properties are improved

Disadvantages

- high cost of equipment and dies
- limited flexibility of shapes and sizes
- accuracy/repeatability



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