

2.76/2.760 Multiscale Systems Design & Manufacturing

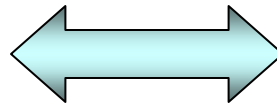
Fall 2004

Piezoelectric Transducers

What is Piezoelectricity ?

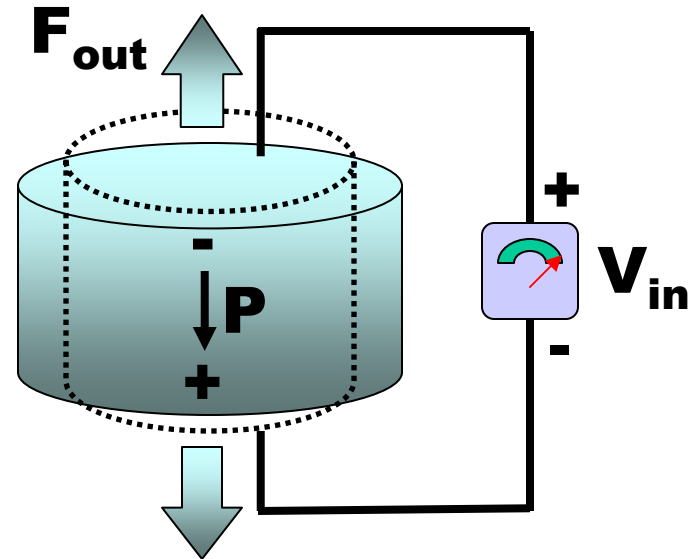
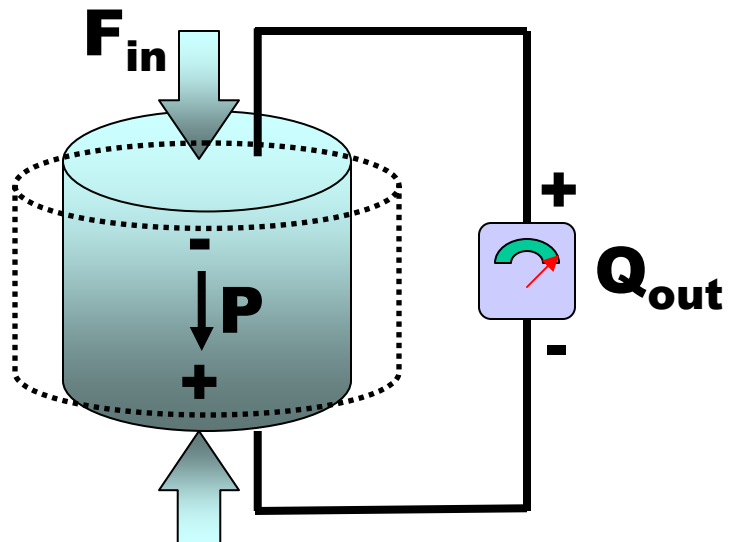
Jacques & Pierre Curie (1880)

**Electrical
Energy**



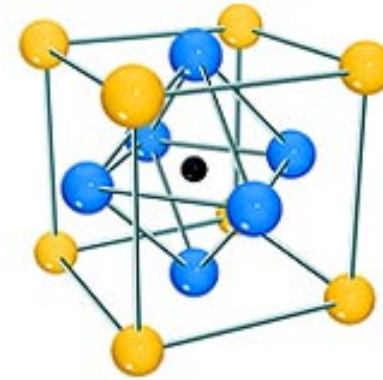
Lippmann (1881)

**Mechanical
Energy**



Piezoelectricity

- **Piezoelectric Ceramics**
- **Thin film fabrication**
- **Piezoelectric Transducers**

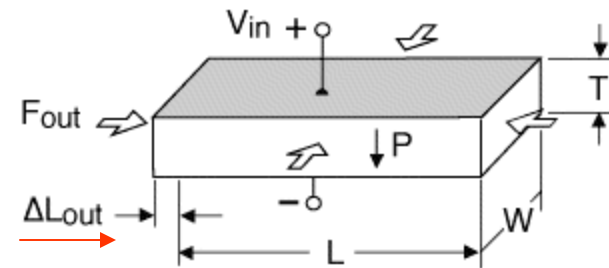
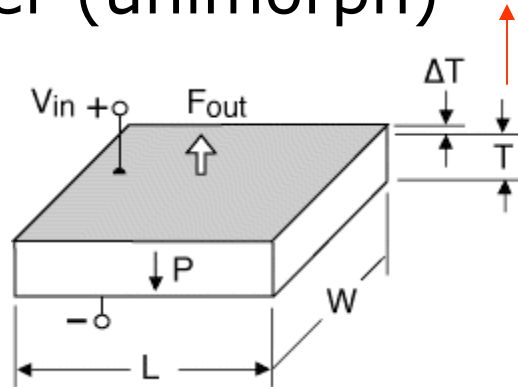


G. Binnig & H. Rohrer, Nobel Prize, 1986

Photos removed for copyright reasons.
Medical ultrasound, disk drive heads, naval submarine.

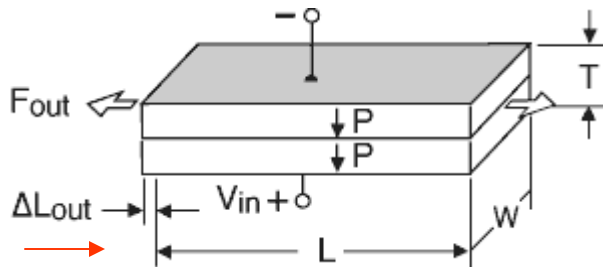
Piezoelectric Transducers

1-layer (unimorph)



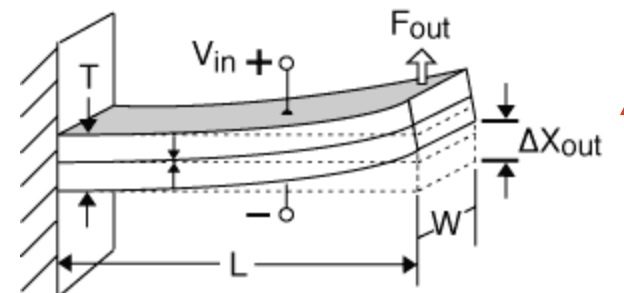
2-layer

extender



Y-poled

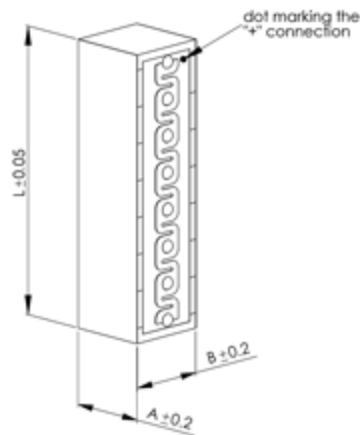
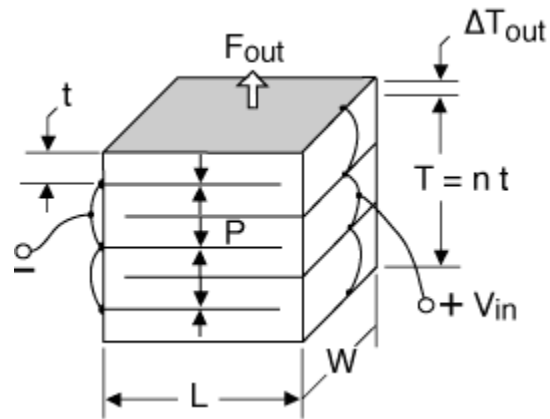
bender (bimorph)



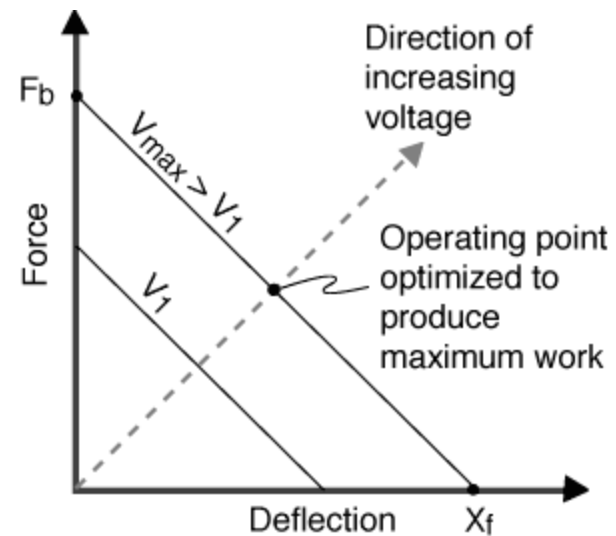
x-poled

Transducers

multi-layer (multimorph)



blocked
force



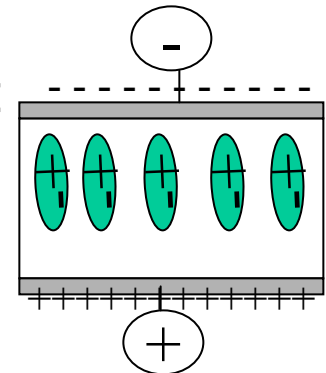
Dielectric Constant

- Dielectric materials, atoms are ionized, + and – charged, causing electric dipoles. – electric polarization
- Polarization, quantitatively,
electric dipoles/unit volume, C/m²
- Dielectric Displacement, D,
stored electric charge/unit area

$$D = \epsilon_0 + P = \epsilon E = K\epsilon_0 E$$

ϵ_0 : Vacuum permittivity (8.854×10^{-12} F/m)

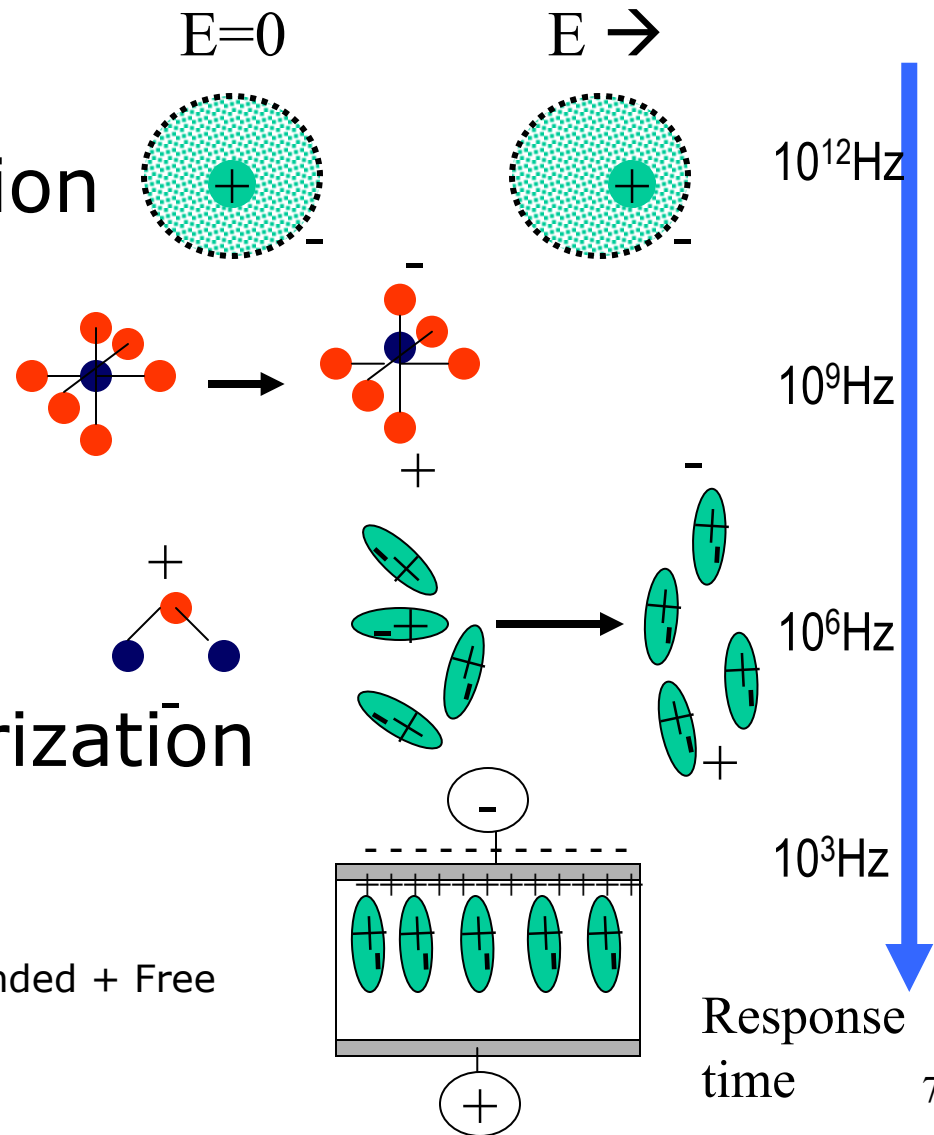
K : Relative Permittivity or dielectric constant



Origins of Polarization

- Electronic Polarization
- Ionic Polarization
 - Ionic crystals, NaCl..
- Dipolar Polarization
 - HCl
- Space Charge Polarization

Total Charge= bounded + Free

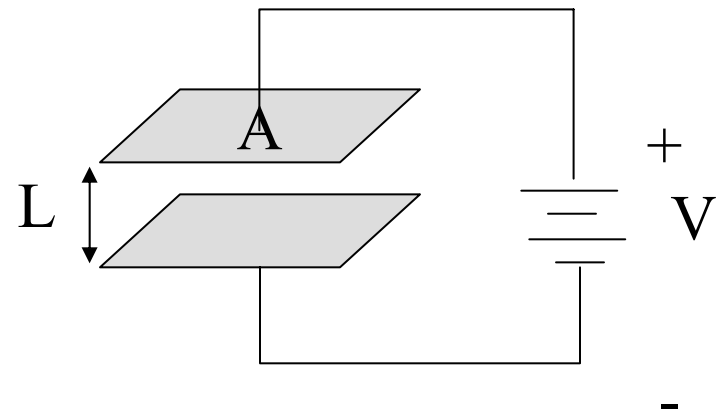


Capacitance

$$C = \frac{q}{V}$$

Capacitance of a parallel plate capacitor

$$C = \epsilon\epsilon_0 \frac{A}{L}$$



Relative Dielectric Constant (K), or permittivity

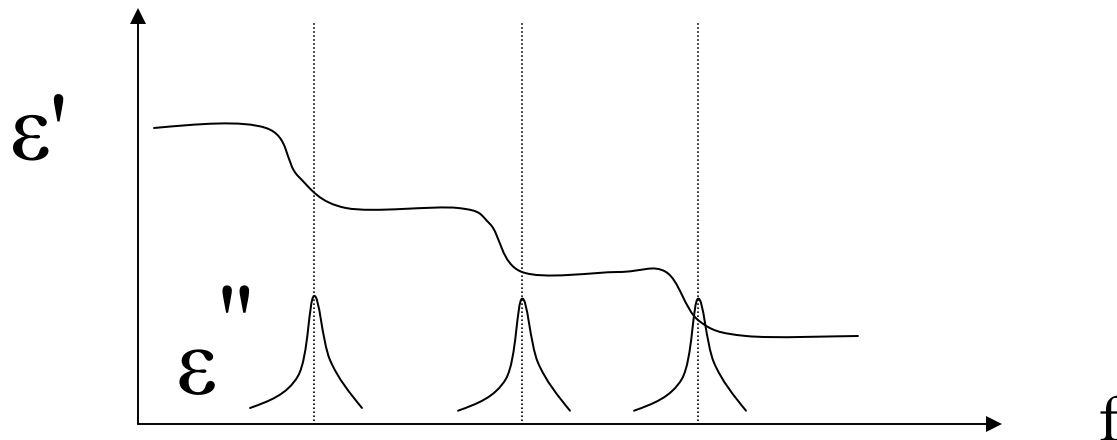
$$\epsilon = \frac{C}{C_{Vac}}$$

Dielectric Constants

• Water	81.1	• BaTiO ₃	6000
• Silicon	11.8	• KNbO ₃	700
• Glass	6.9	• Rochelle salt	170
• Epoxy	4.0	• PZT	1200
• Ice	3.0		
• Polyethylene	2.3		
• Air	1.000576		

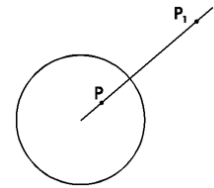
Dielectric Loss

- Frequency dependency of polarization
- When τ and f are in the same order, energy absorbed and phase lag occurs.
- Dielectric Loss, $\tan\delta = \epsilon'' / \epsilon'$
- Dielectric breakdown: 60kV/cm for PZT



Ferroelectricity

- Ionic and electronic polarization
- S^2P or d^0 cations
- Crystal structure with no inversion center
- Ferroelectricity;
 - Spontaneous polarization wrt external electric field
 - Reversible, Remanent polarization, hysteresis
- Pyroelectricity; strong variation in polarization with temperature
- Piezoelectricity; large mechanical strain response to applied electrical field



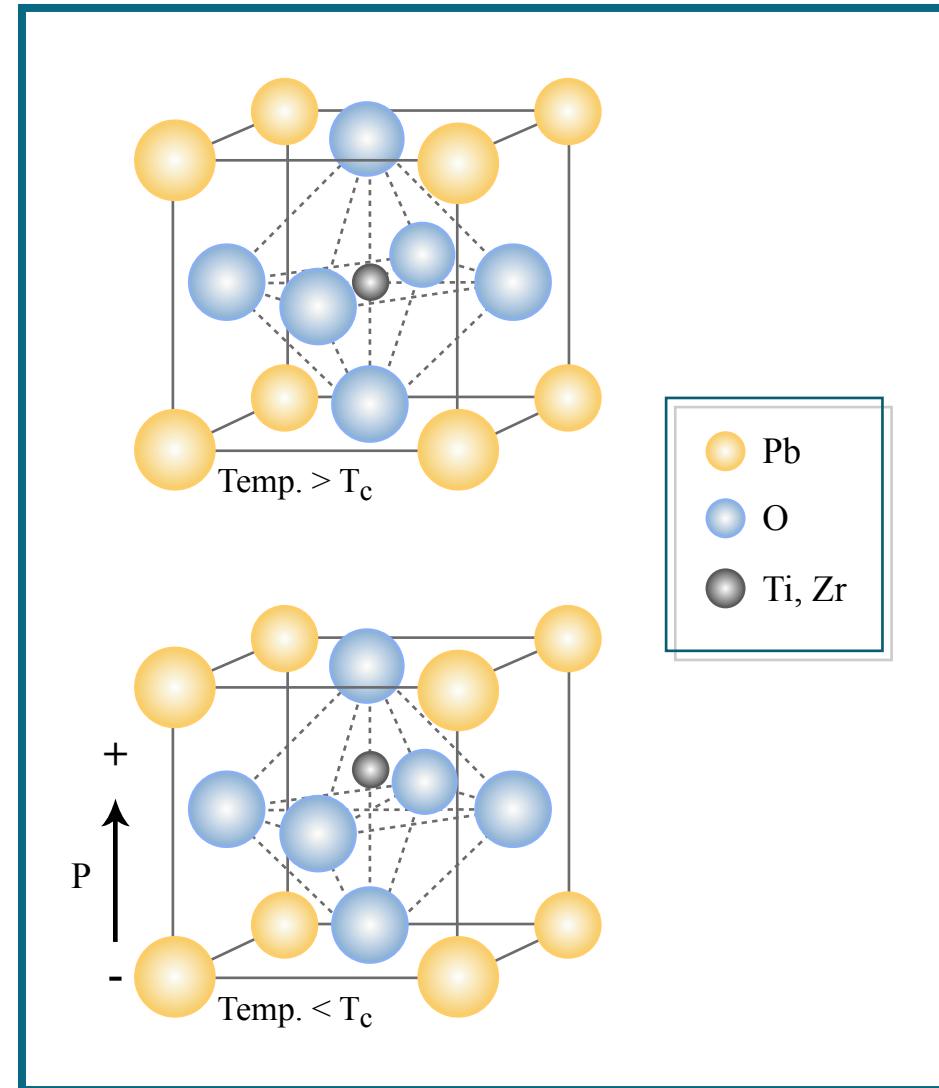
Perovskite Phase

- PZT, $(\text{Pb}(\text{Zr}_{1-x}\text{Ti}_x)\text{O}_3)$, the most important piezoelectric material.

$\text{PbZrO}_3:\text{PbTiO}_3 \rightarrow 52:48$

rhombohedral $\rightarrow$ cubic $\rightarrow$ tetrahedral

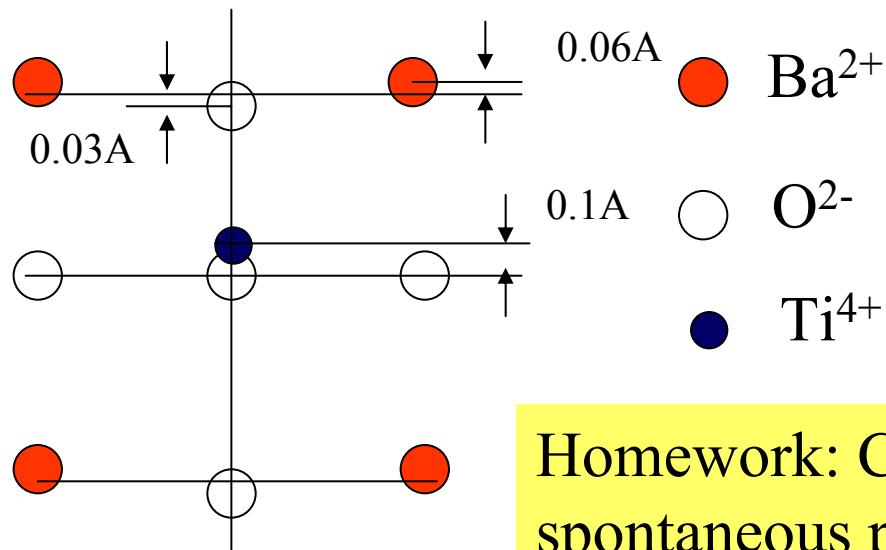
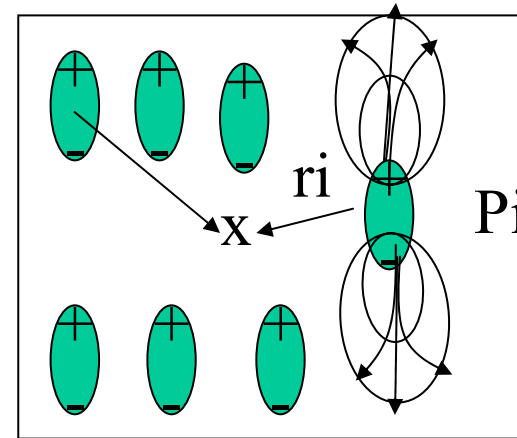
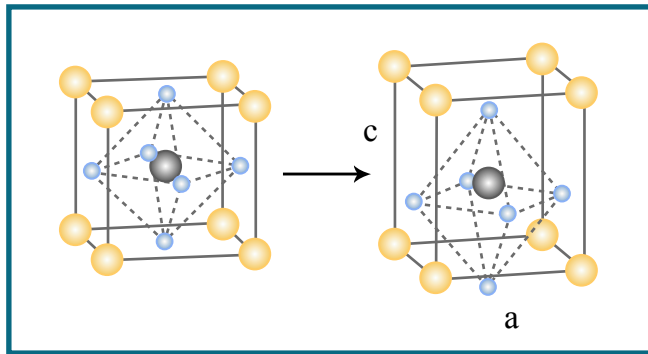
- Curie Temperature
- Pyrochlore phase



Spontaneous polarization

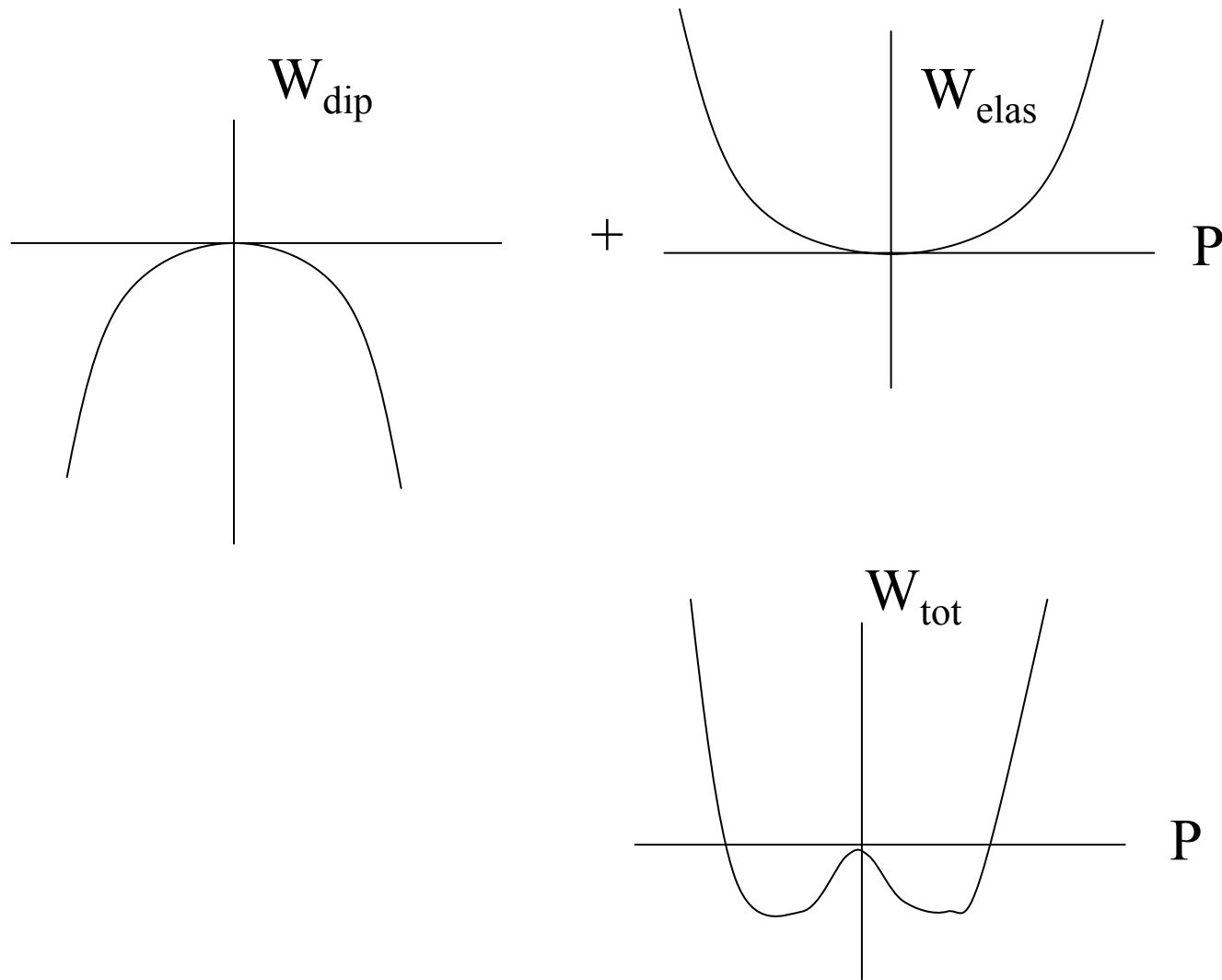
$$\Delta \vec{P} = \vec{P}(\text{polar}) - \vec{P}(\text{nonpolar}) / a^2 c$$

: Polarization per unit cell volume



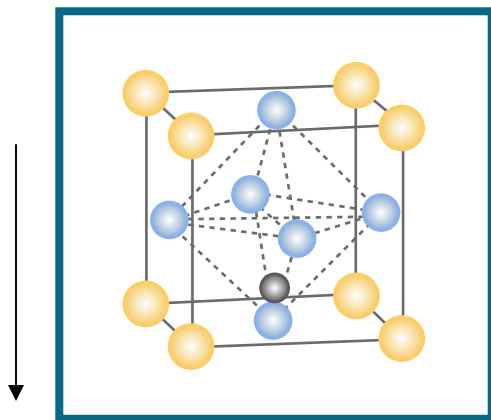
Homework: Calculate the magnitude of spontaneous polarization. $a=3.992 \text{ \AA}$, $c=4.036a$
 $1e=1.602 \times 10^{-19} \text{ C}$

Energy of polarization

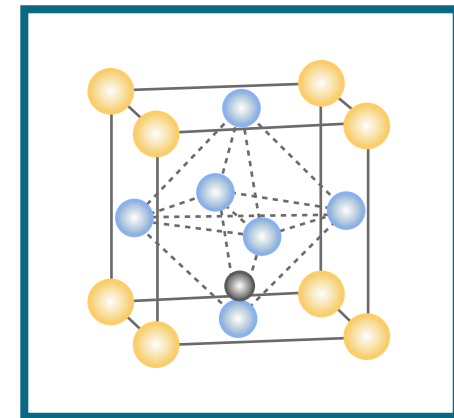
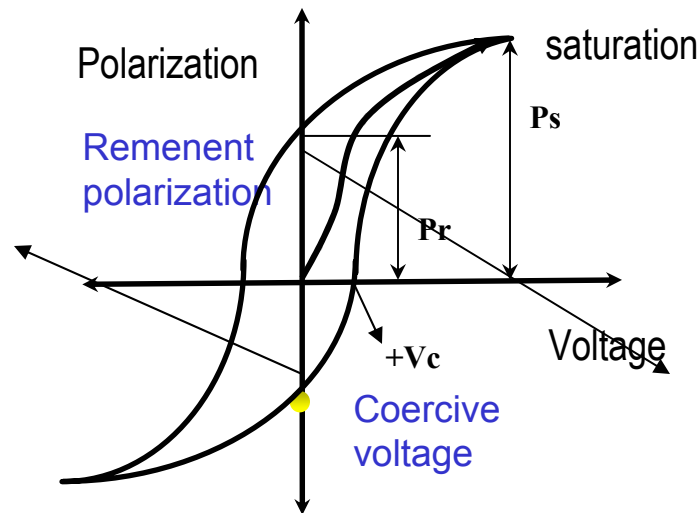


Piezoelectricity

- Polarization does not disappear when the electric field removed.
- The direction of polarization is reversible.

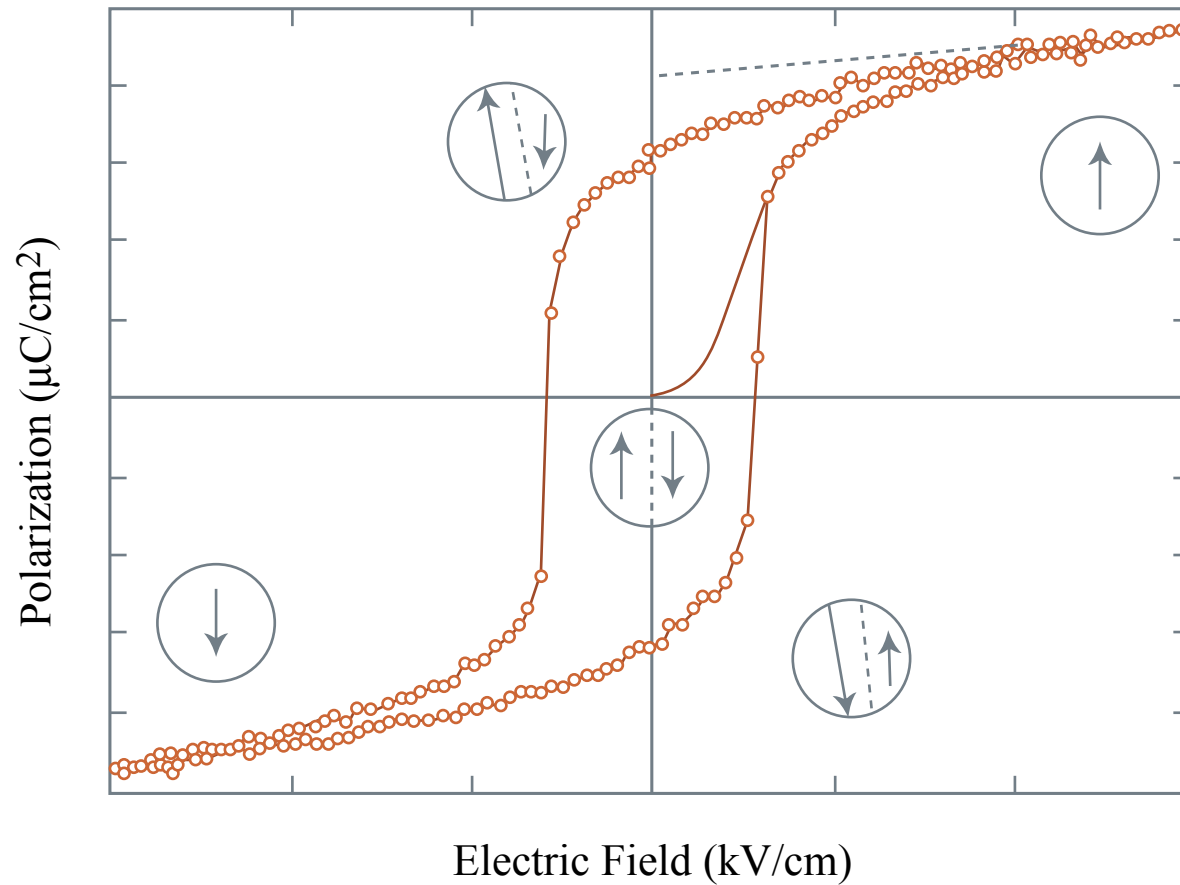


Sang-Gook Kim, MIT



FRAM utilize two stable positions.

Hysteresis



Ferroelectric (P-E) hysteresis loop. The circles with arrows indicate the polarization state of the material for different fields.

Domain Polarization

- Poling: 100 C, 60kV/cm, PZT
- Breakdown: 600kV/cm, PZT
- Unimorph cantilever

Piezoelectricity

Direct effect

$$D = Q/A = dT$$

$$E = -gT$$

$$T = -eE$$

Converse effect

$$S = dE$$

$$g = d/\epsilon = d/K\epsilon_0$$

$$E = -hS$$

- D: dielectric displacement, electric flux density/unit area
- T: stress, S: strain, E: electric field
- d: Piezoelectric constant, [Coulomb/Newton]

Boundary
Conditions

Free $\longrightarrow$ T

$$d = (\partial S / \partial E)_T = (\partial D / \partial T)_E$$

Short circuit $\rightarrow$ E

$$g = (-\partial E / \partial T)_D = (\partial S / \partial D)_T$$

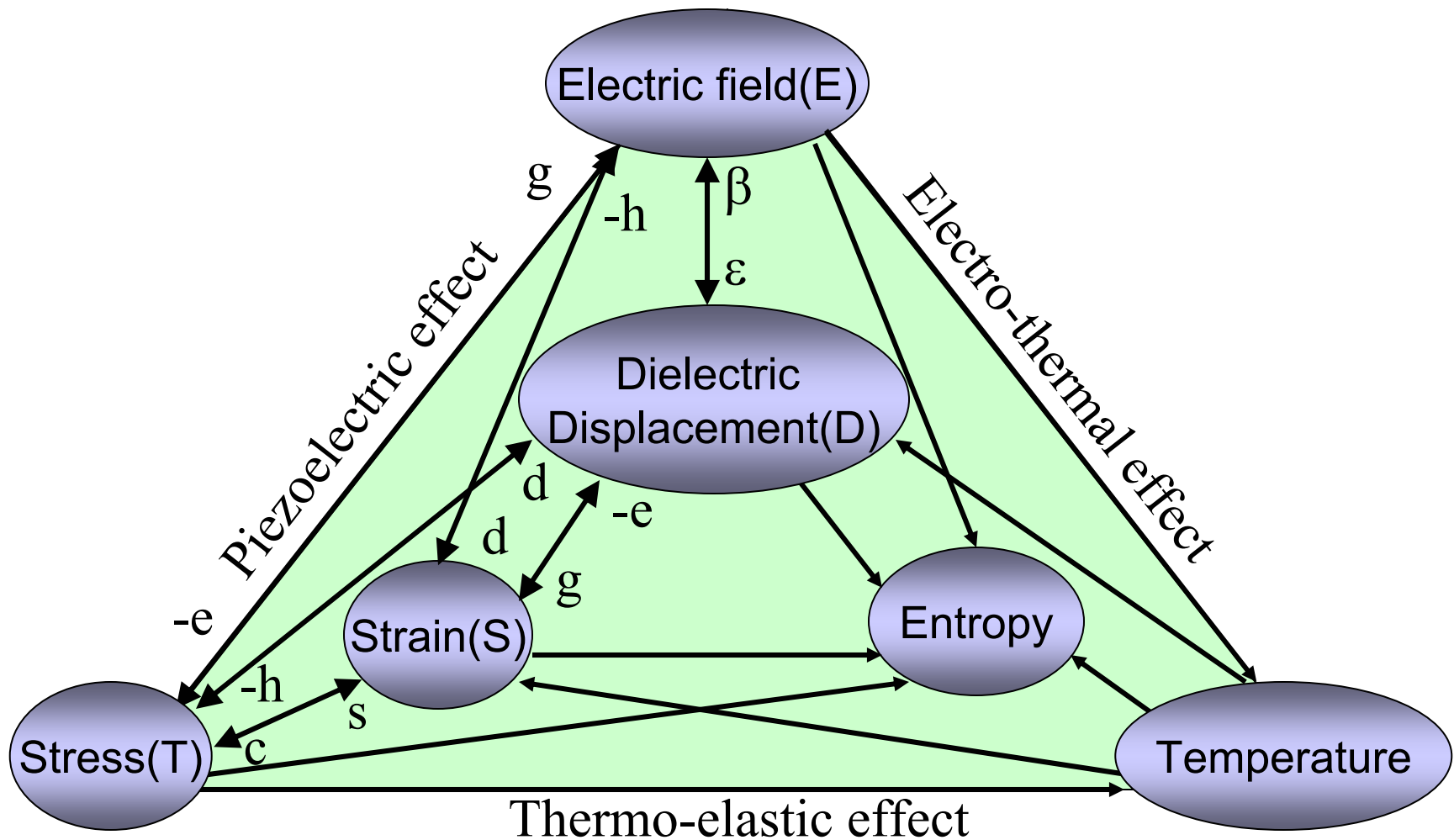
Open circuit $\rightarrow$ D

$$e = (-\partial T / \partial E)_S = (\partial D / \partial S)_E$$

Clamped $\longrightarrow$ S

$$h = (-\partial T / \partial D)_S = (-\partial E / \partial S)_D$$

Principles of piezoelectric



Equation of State

Basic equation

d-form $S_{ij} = s_{ijkl}^E T_{kl} + d_{kij} E_k$

$$D_i = d_{ikl} T_{kl} + \varepsilon_{ik}^T E_k$$

g-form $S = s^D T + g D$

$$E = -g T + \beta^T D$$

e-form $T_{ij} = c_{ijkl}^E S_{kl} - e_{kij} E_k$

$$D_i = e_{kij} S_{kl} + \varepsilon_{ik}^S E_k$$

h-form $T = c^D S - h D$

$$E = -h S + \beta^S D$$

$$c^E = 1/s^E$$

$$e = d c^E$$

$$\varepsilon^E = \varepsilon^T - d c^E d_t$$

$$\beta^T = 1/\varepsilon^T$$

$$g = d/\varepsilon^T$$

$$s^D = s^E - d_t (\varepsilon^T)^{-1} d$$

$$D = Q/A$$

$$S = F/A$$

Equation of states

$$\mathbf{D} = \mathbf{d}\mathbf{T} + \boldsymbol{\varepsilon}^T \mathbf{E}$$

direct

$$\mathbf{S} = \mathbf{s}^E \mathbf{T} + \mathbf{d}\mathbf{E}$$

converse

Tensor to Matrix notation

For cylindrical symmetry, and poling in axis 3,

$$D_1 = \varepsilon_1 E_1 + d_{15} T_5$$

$$D_2 = \varepsilon_1 E_2 + d_{15} T_4$$

$$D_3 = \varepsilon_3 E_3 + d_{31} (T_1 + T_2) + d_{33} T_3$$

$$S_1 = s_{11} T_1 + s_{12} T_2 + s_{13} T_3 + d_{31} E_3$$

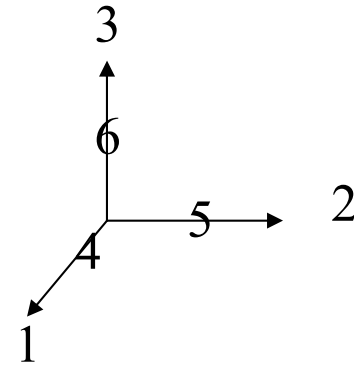
$$S_2 = s_{11} T_2 + s_{12} T_1 + s_{13} T_3 + d_{31} E_3$$

$$S_3 = s_{13} (T_1 + T_2) + s_{33} T_3 + d_{33} E_3$$

$$S_4 = s_{44} T_4 + d_{15} E_2$$

$$S_5 = s_{44} T_5 + d_{15} E_1$$

$$S_6 = s_{66} T_6$$



Applications of piezoelectric

Sensors

Pressure sensors
Accelerometers
Gyroscopes
Power generators

Actuators

Vibrators
Ultrasonic transducers
Resonators / Filters / Switches
Surface Acoustic wave(SAW) devices
Transformers
Actuators
Ultrasonic motors

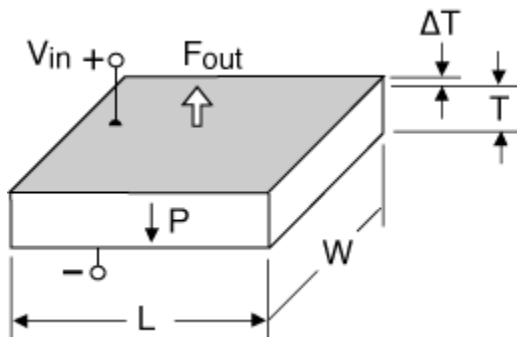
Piezoelectric Charge Constants

Electrical energy

Actuator

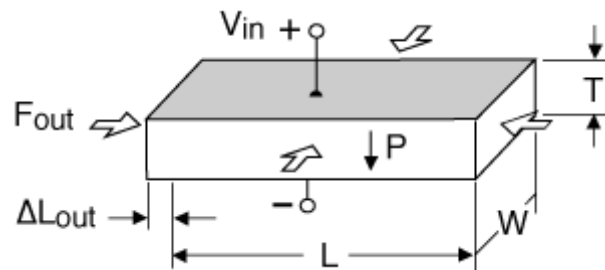
Mechanical energy

Longitudinal (d_{33})



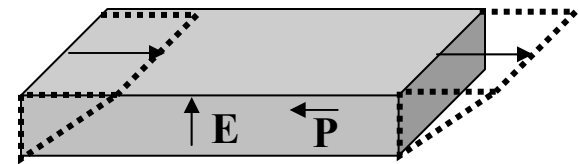
$$\Delta T/T = d_{33} \cdot E$$

Transverse (d_{31})



$$\Delta L/L = d_{31} \cdot E$$

Shear (d_{15})



$$\text{Shear strain} = d_{15} E$$

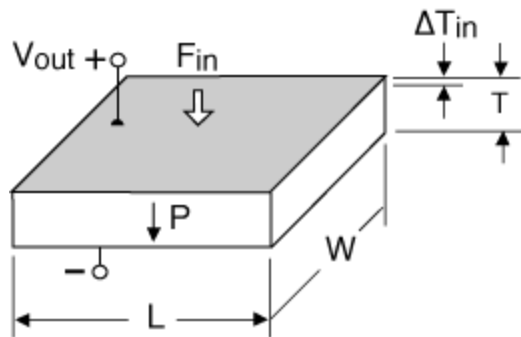
Piezoelectric Charge Constants

Mechanical energy

Sensor

Electrical energy

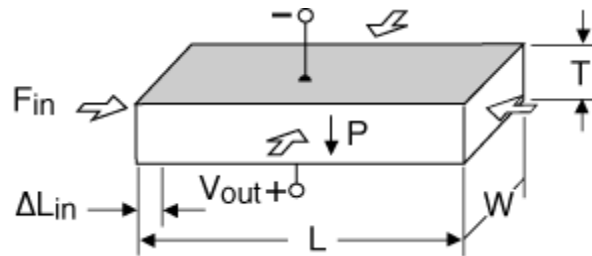
Longitudinal (d_{33})



$$Q = d_{33} \cdot F_{in}$$

$$V_{out}/T = g_{33} \cdot F_{in} / (L \cdot W)$$

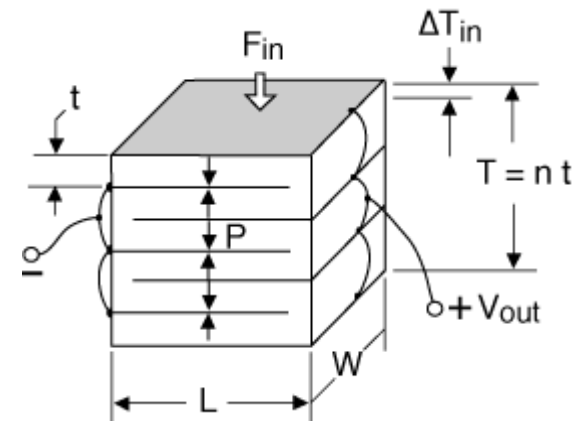
Transverse (d_{31})



$$Q = d_{31} \cdot F_{in}$$

$$V_{out}/T = g_{31} \cdot F_{in} / (T \cdot W)$$

Multi-layer (d_{33})



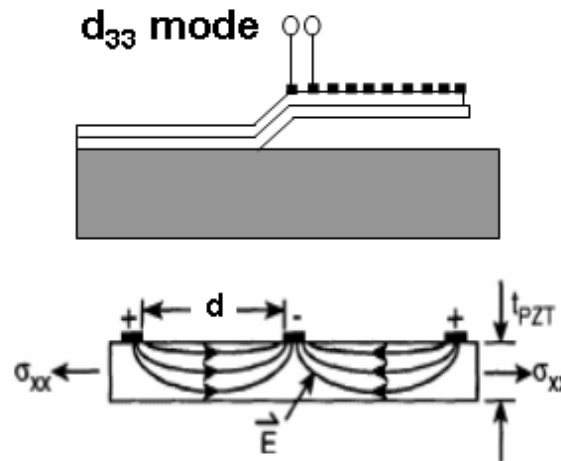
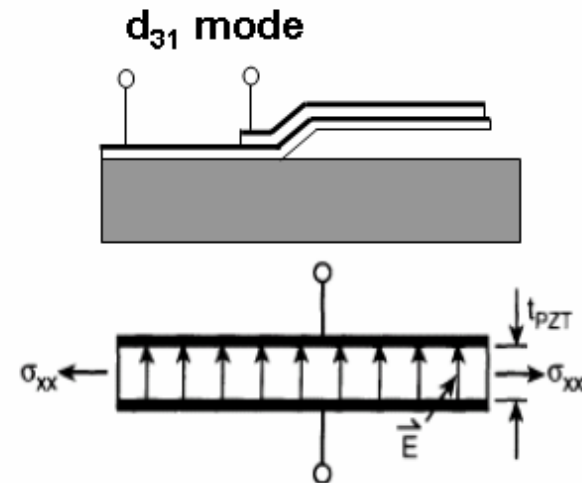
$$Q = n \cdot d_{33} \cdot F_{in}$$

$$V_{out}/T = t/n \cdot g_{33} \cdot F_{in} / (LW)$$

d_{31} vs d_{33}

Homework 2:

Compare generated voltages V_{31} (from d_{31} mode), V_{33} (d_{33} mode). Both have same cantilever dimension, but different electrodes.



$d_{33}=200$ pC/n
 $K=1000$

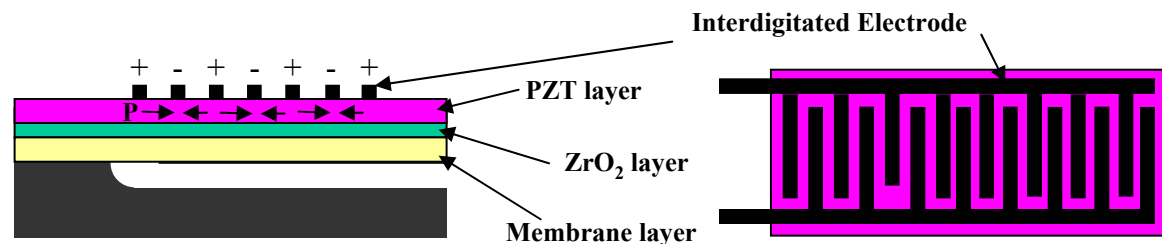
Assume, $g_{33}=2g_{31}$

$t_{pzt}=0.5$ μ

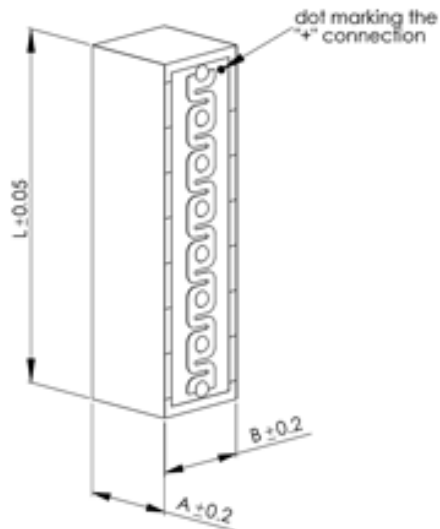
$d=5$ μ

length=100 μ , width=50 μ

Young's modulus of the beam=
65 Gpa, max. strain = 0.1%

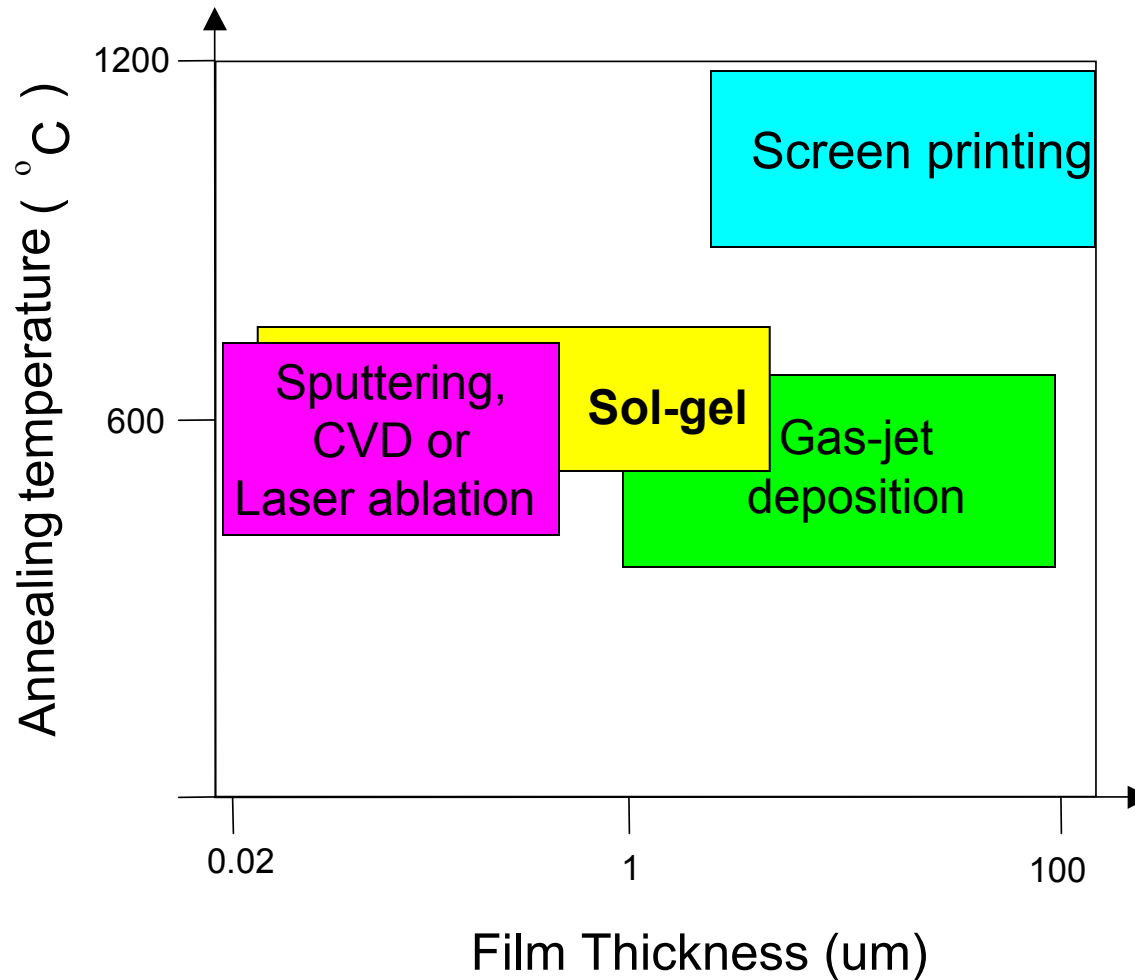


Design of a Z-positioner



Ordering Number*	Dimensions A x B x L [mm]	Nominal Displacement [μm @ 100 V] (±10%)	Max. Displacement [μm @ 120 V] (±10%)	Blocking Force [N @ 120 V]	Stiffness [N/μm]	Electrical Capacitance [μF] (±20%)	Resonant Frequency [kHz]
P-882.10	2 x 3 x 9	7	9	215	26	0.13	135

Fabrication Methods for PZT thin Films



Sol-Gel spin coating

Advantages

- Vacuum chamber not necessary (simple)
- Easy composition control
- Deposition on large flat substrate

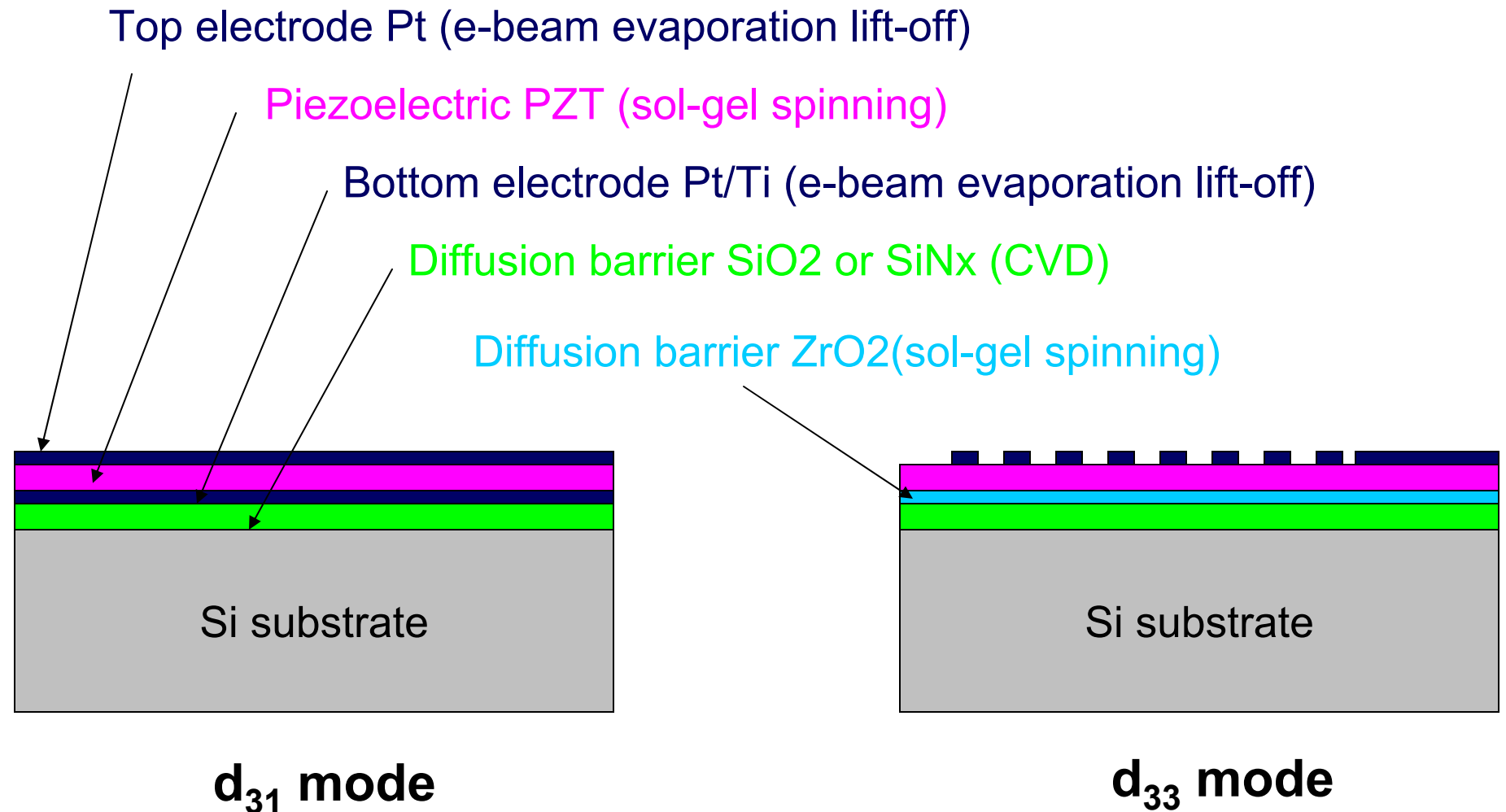
Disadvantages

- Difficult to deposit on deep trenched surface
- Higher raw material consumption

Advantage and disadvantage of PZT film

Advantage	Disadvantage
Unlimited resolution Large force generation Fast expansion No magnetic fields (low cross talk) Low power consumption No wear and tear for actuation Vacuum and clean room compatible Operation at cryogenic temperature	Complex fabrication Hysteresis Life cycle (10^{12} cycles) ; Fatigue, retention...

Typical Layer Structures for Sol-Gel PZT



Thermal Oxide Growth and Bottom Electrode Evaporation

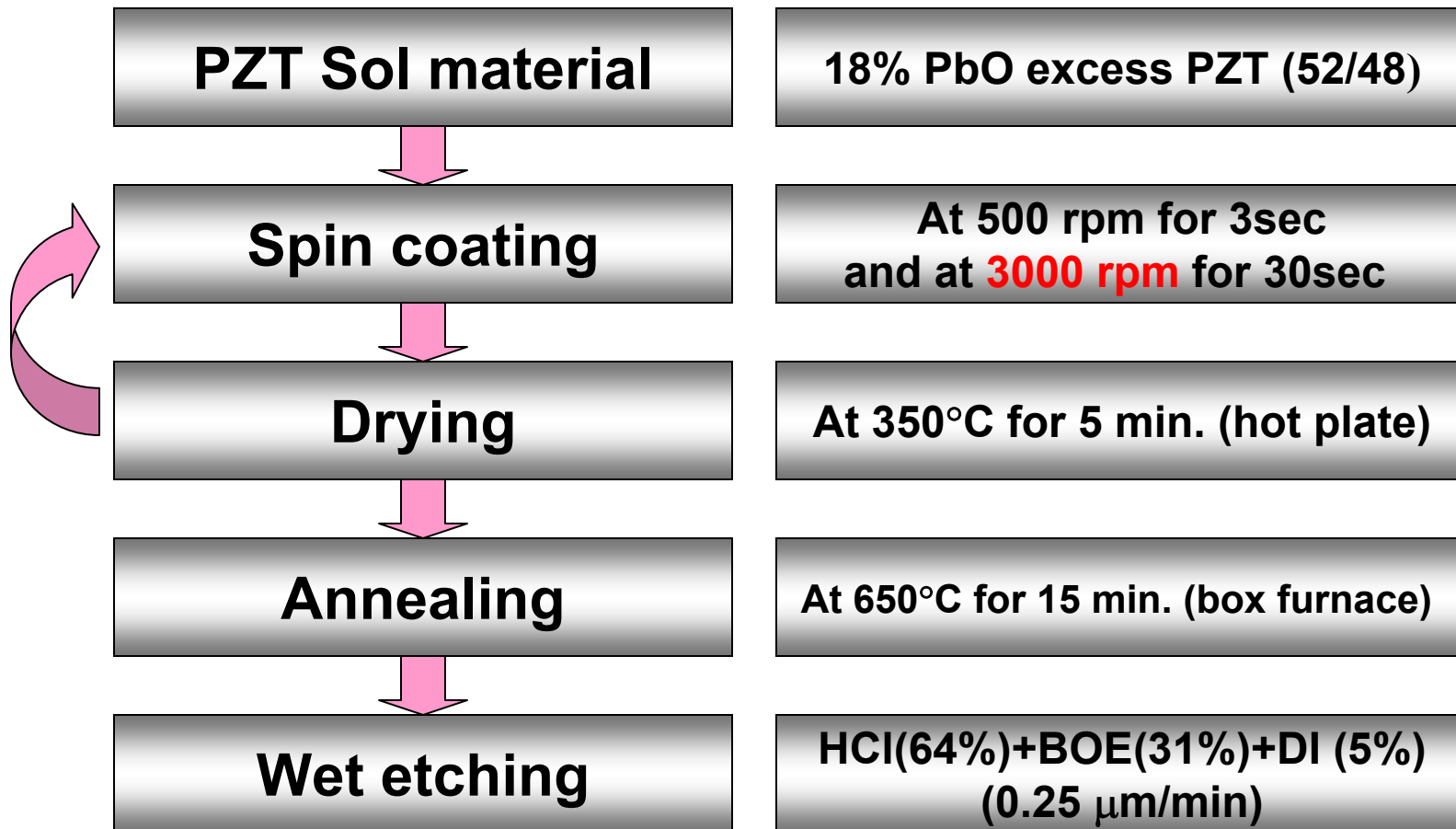


Tubes for growing of
device diffusion barrier

Evaporation of
device electrodes

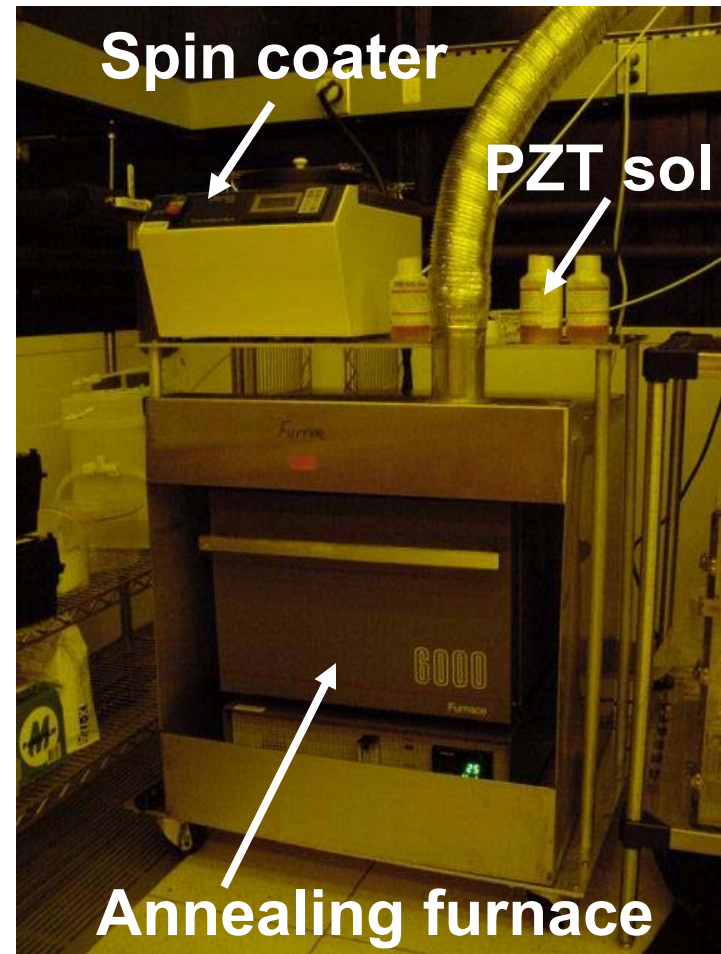
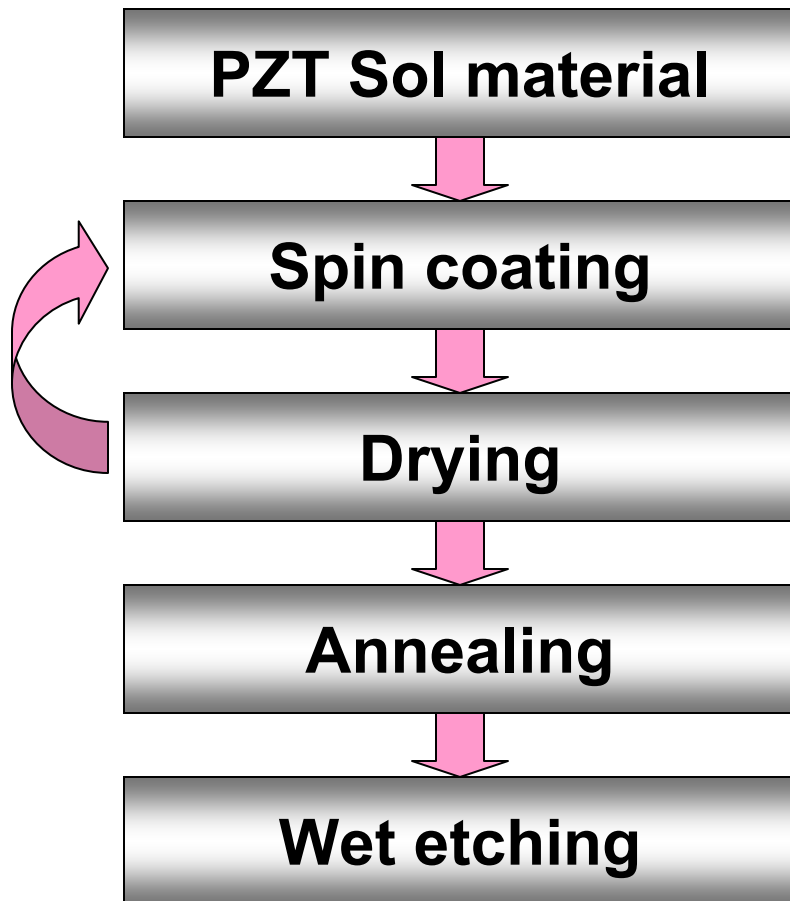


Fabrication of the PZT Film



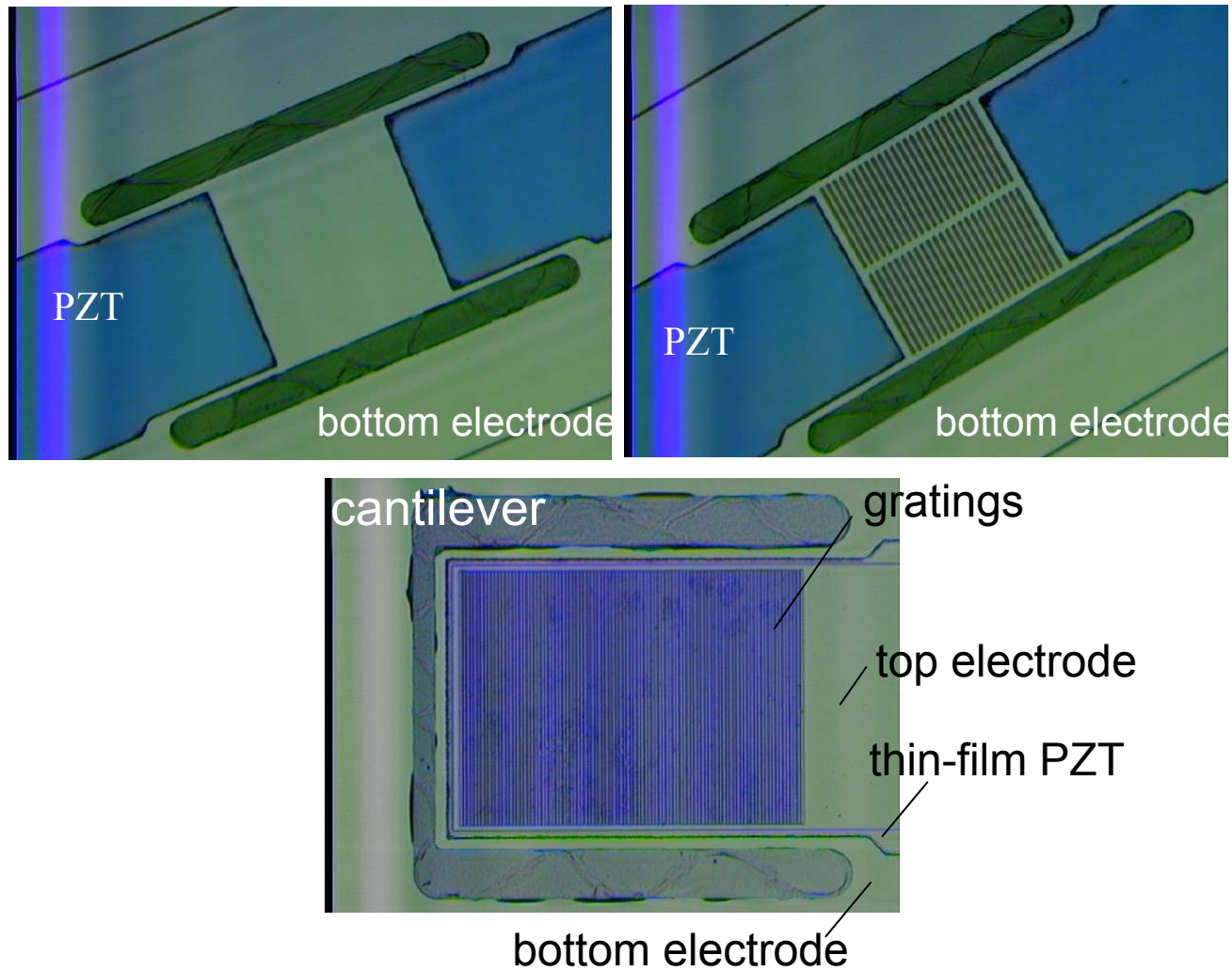
Spin-coat Mitsubishi PZT sol-gel: **15% PZT(118/52/48) A6 Type**

Fabrication of the PZT Film



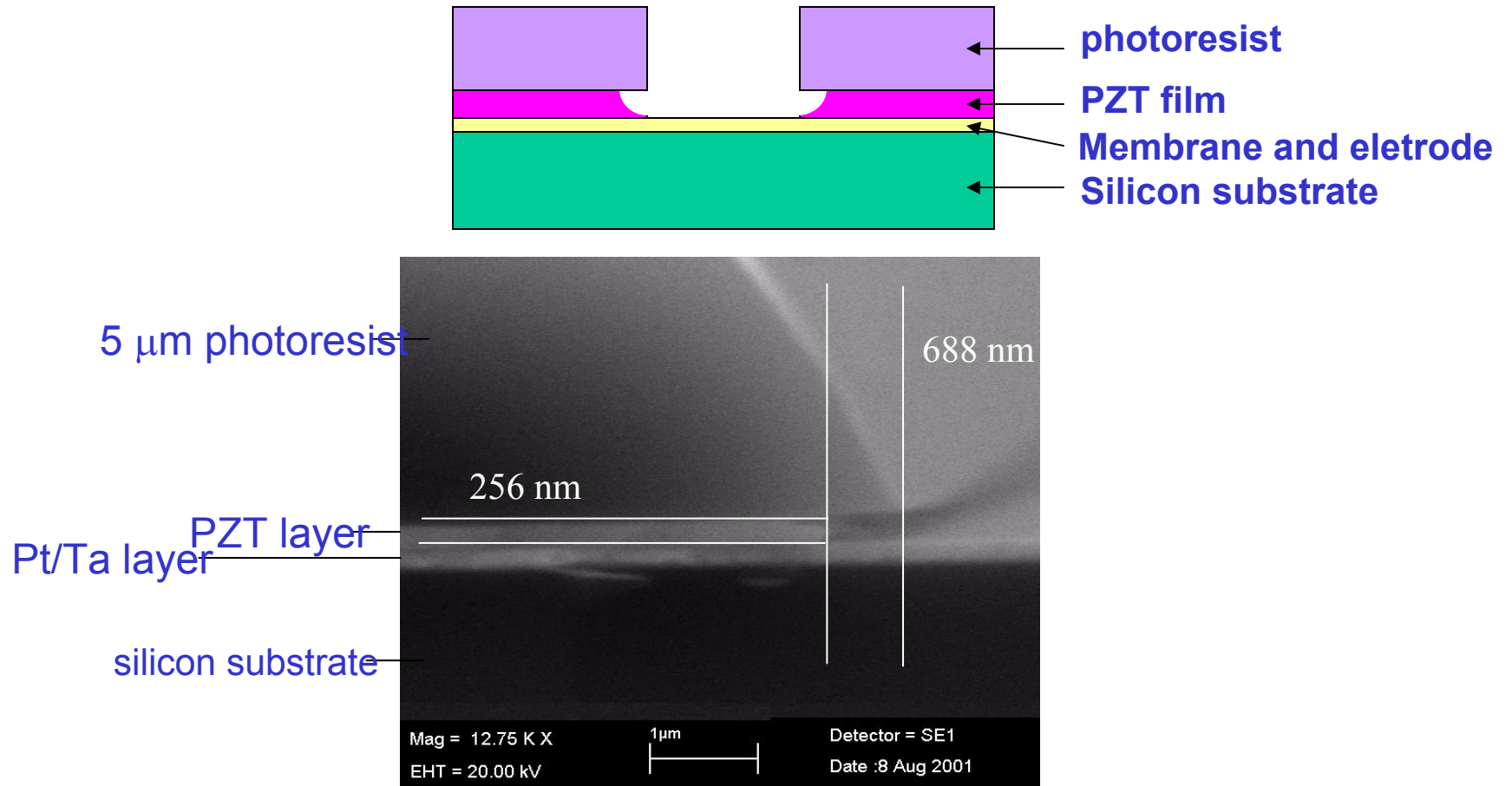
PZT Patterning

Patterned PZT on device



PZT Patterning (Wet etching)

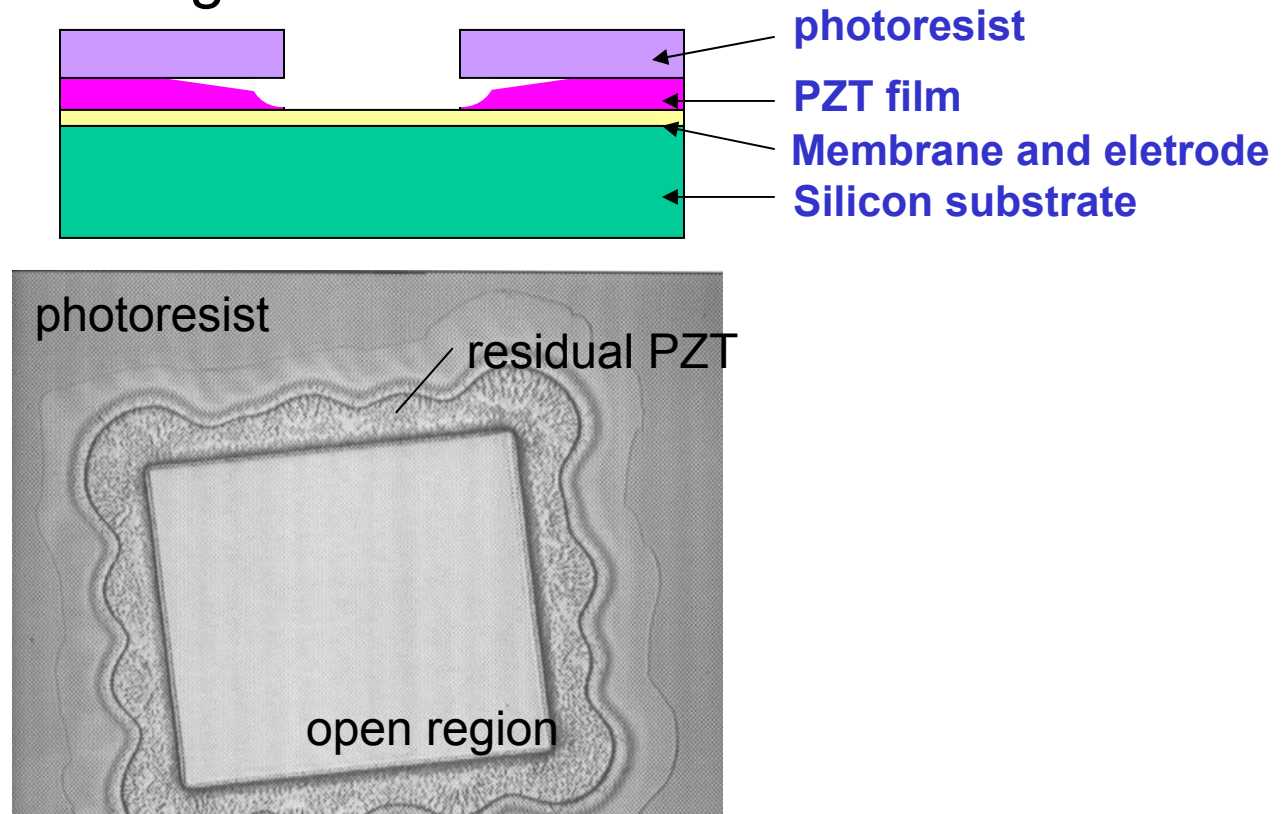
PZT wet-etching with thick photoresist



HCl(64%)+BOE(31%)+DI (5%)
(etch rate: 0.25 $\mu\text{m}/\text{min}$)

PZT Patterning (Wet etching)

PZT wet-etching with thin resist



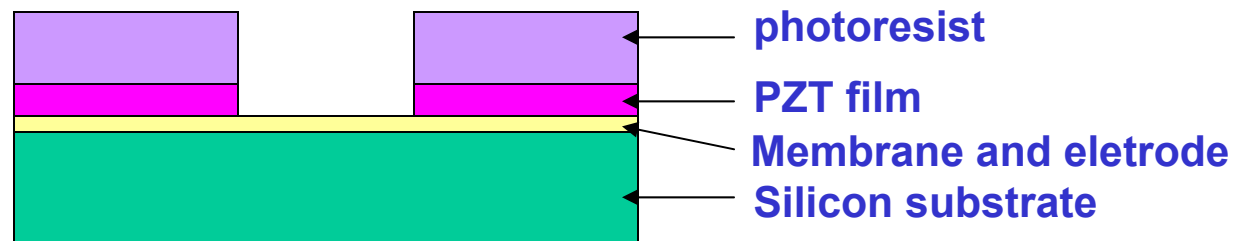
- large undercuts with thin ($1\ \mu\text{m}$) photoresist material

¹ W. Liu *et al*, *Thin Solid Films*, 2000.

² K. Yamashita *et al*, *Transducers '01*, Munich.

PZT Patterning (Dry etching)

PZT dry-etching with thick resist

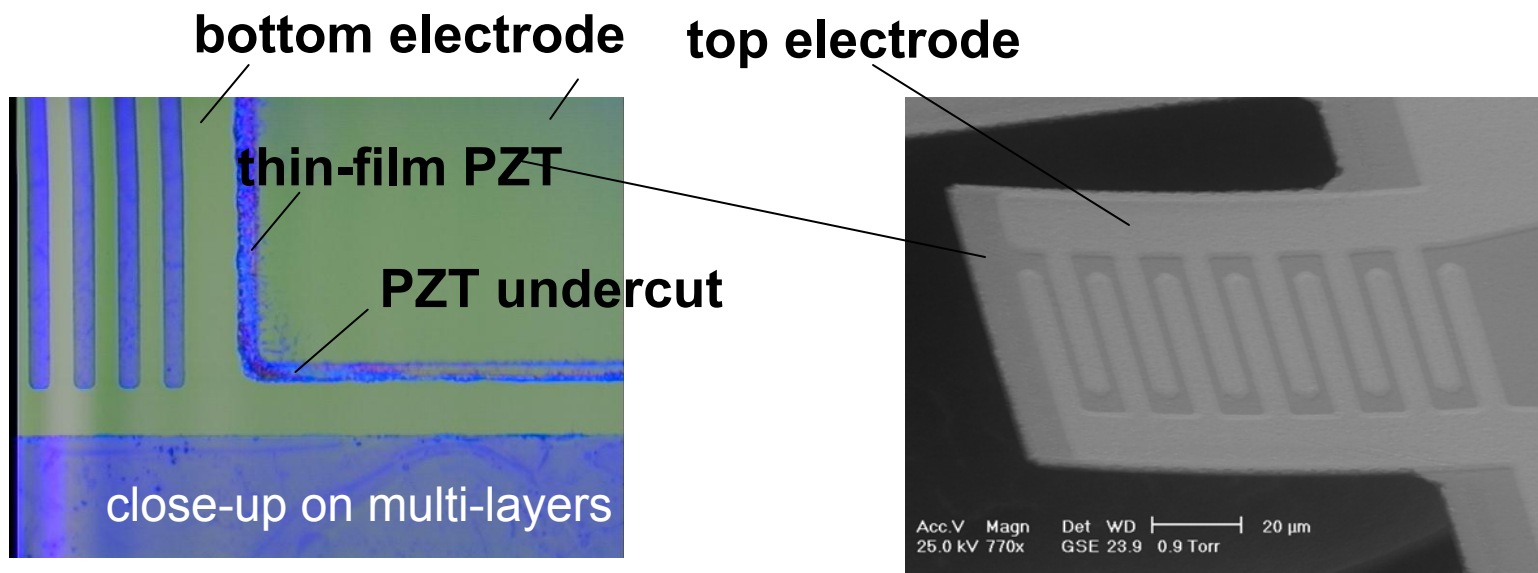


using RIE, Plasmaquest (in TRL) or Plasmatherm (in EML)
with $\text{BCl}_3:\text{Cl}_2$ (30:10)

- stiff sidewall with thick ($10\text{ }\mu\text{m}$) photoresist material

Top Electrode Lift-Off

d33 mode interdigitated structure

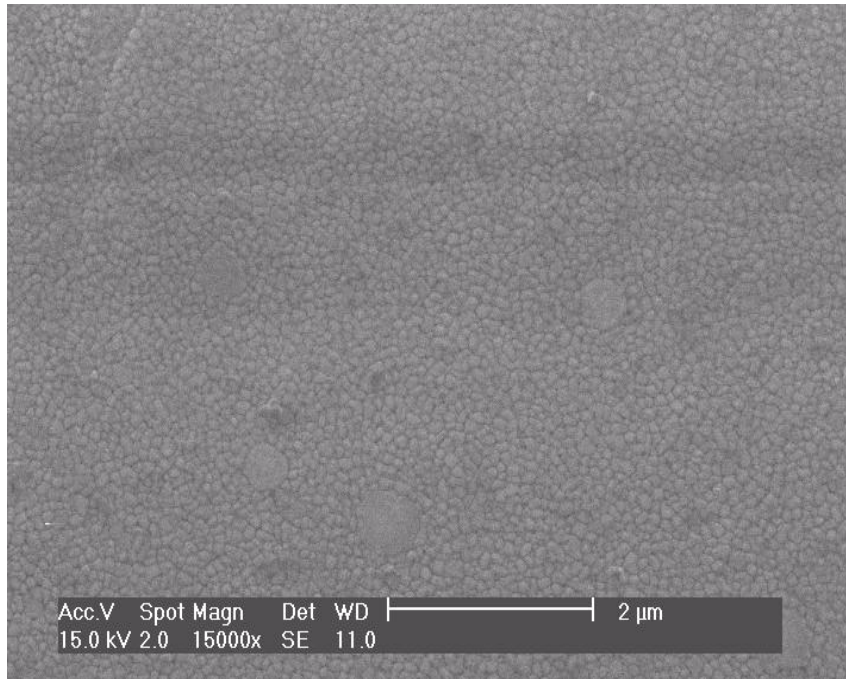


d31 mode sandwich structure

Pt/Ti top electrode pattern by lift-off, 220 nm thick.

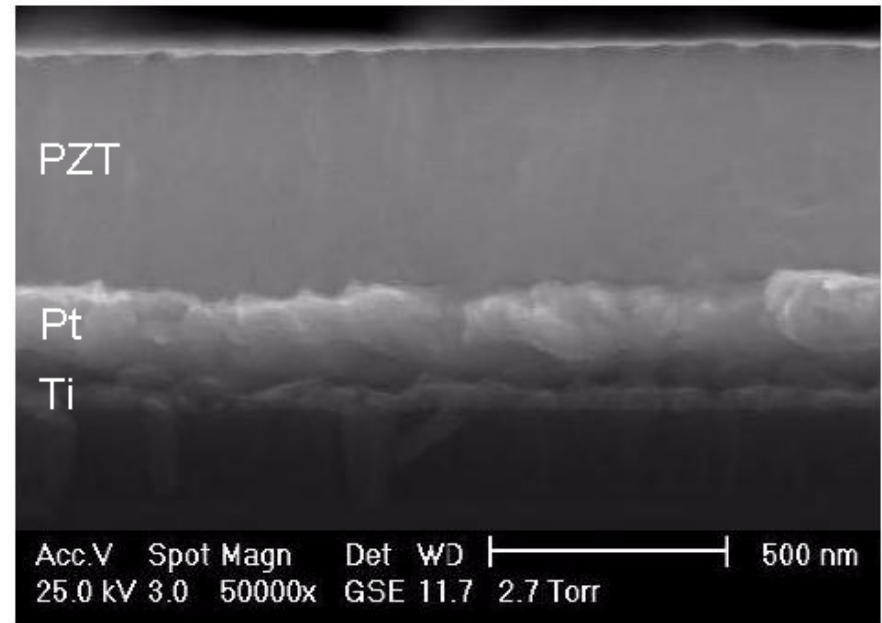
Micro-structure of PZT Thin Film

SEM of PZT film surface



Average grain size : 0.1 μm

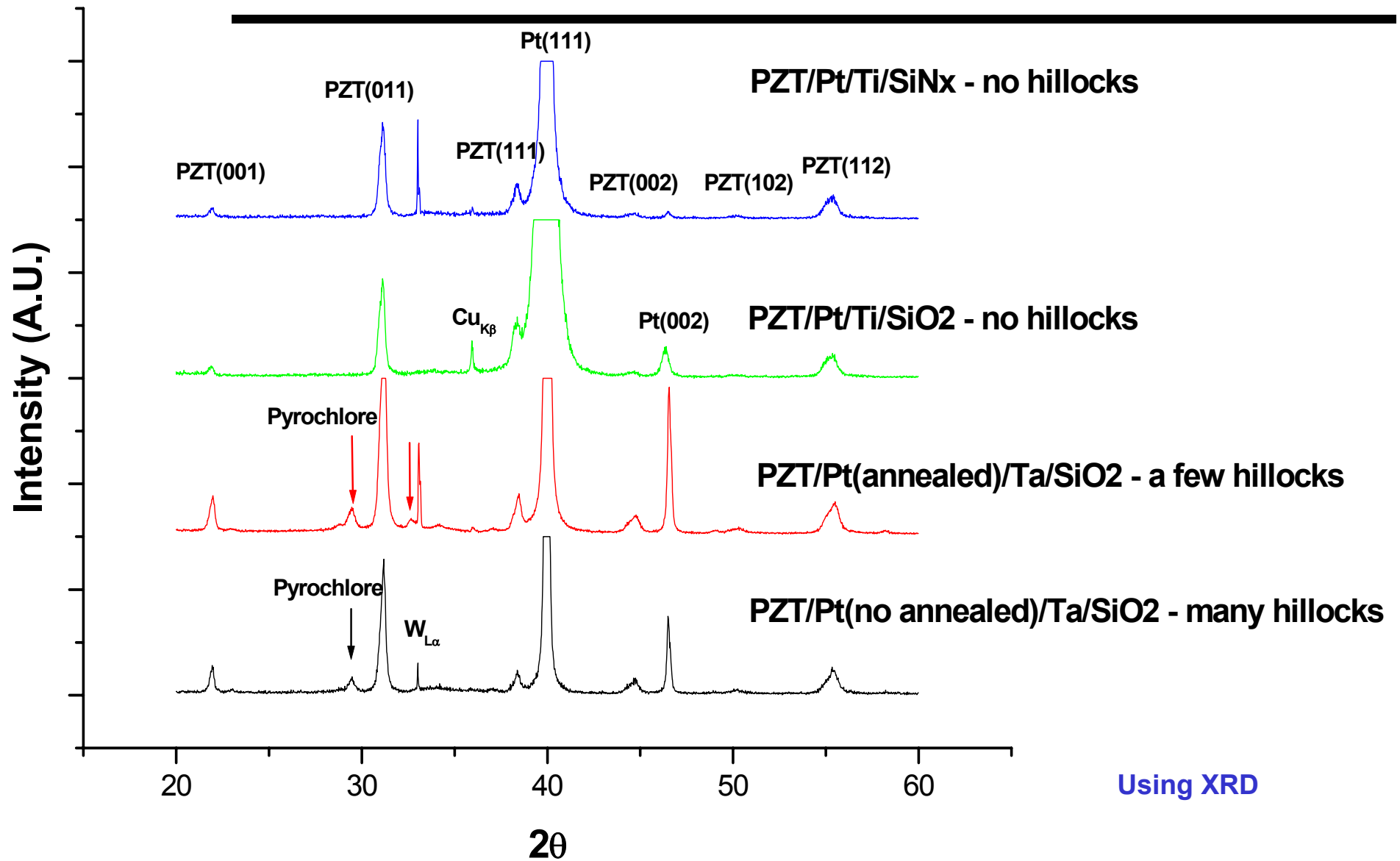
Cross sectional image of PZT film



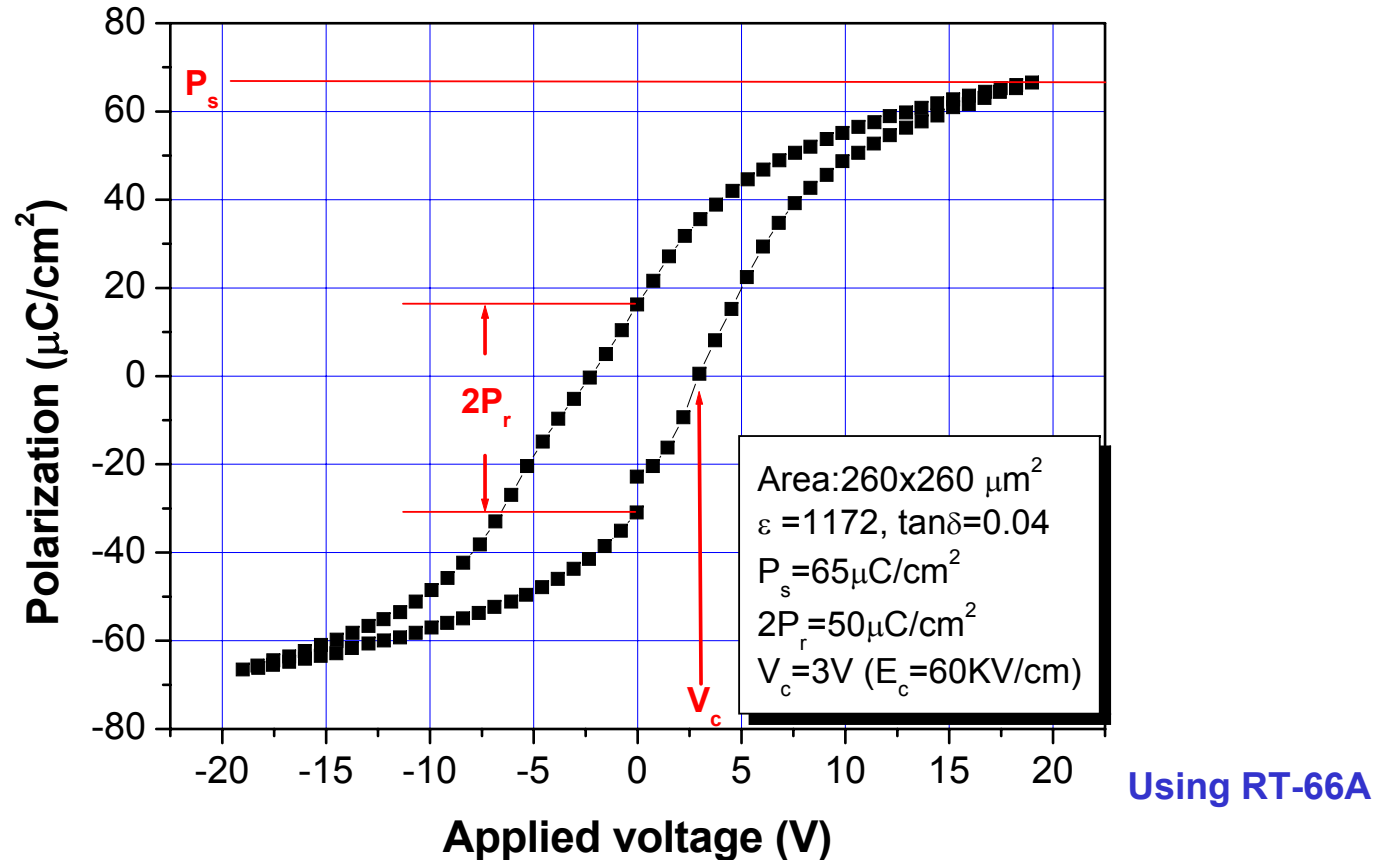
PZT thickness = 510 ± 40 nm;
Pt thickness = 200 nm.

Using SEM

PZT XRD On Various Bottom Electrode Combinations

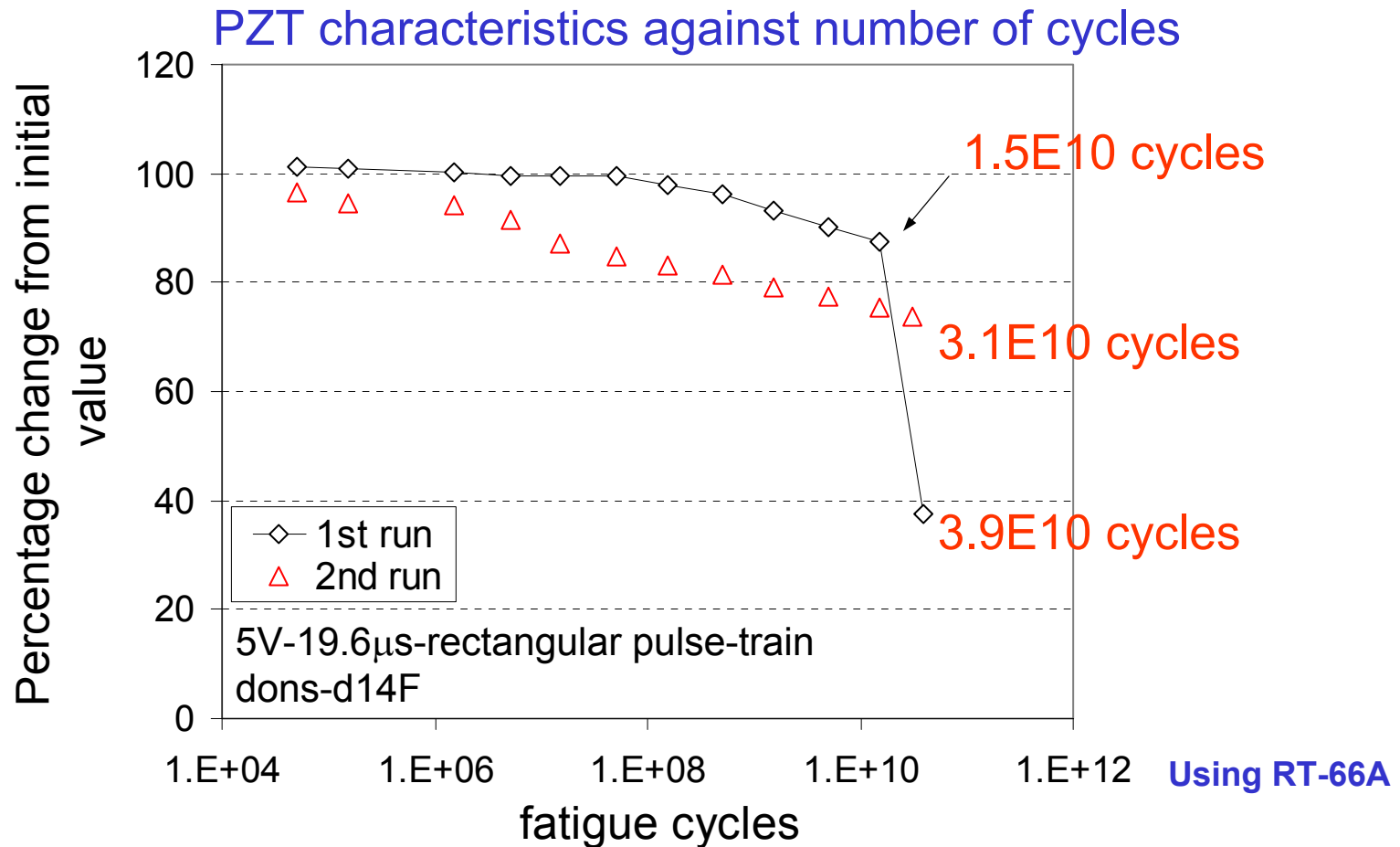


Electrical Measurements - PZT Ferroelectric Characterization



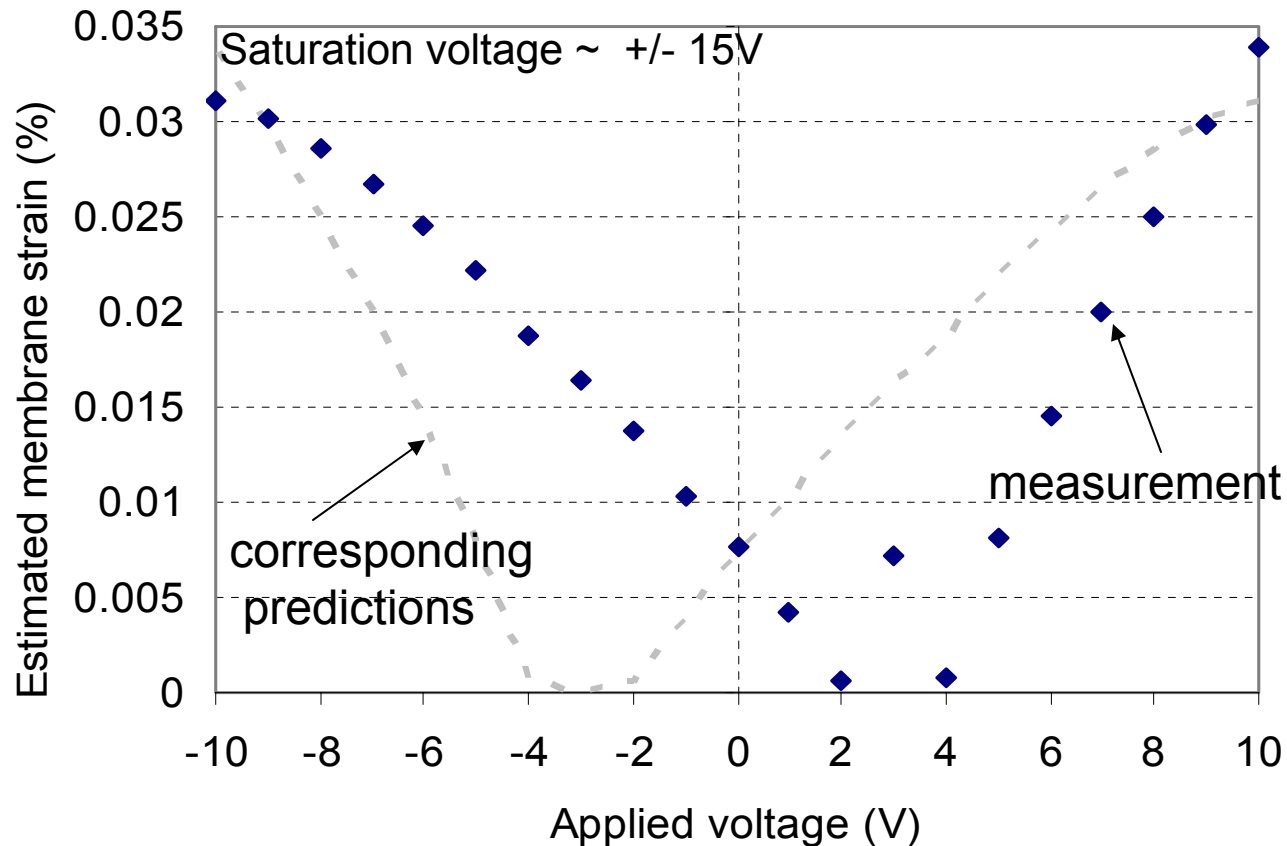
- hysteresis due to domain reorientation - growth, merging and shrinkage
- saturation polarization, P_s at $65 \mu\text{C}/\text{cm}^2$
- remnant polarization, $2P_r$ at $50 \mu\text{C}/\text{cm}^2$

Piezoelectric Fatigue Analysis



- PZT electrical fatigue up to more than 1E10 cycles
- characteristics recovered on 2nd run with same device

Piezoelectric Displacement Analysis



$$\text{strain} = d_{31} V/t$$

$$(d_{33}=275\text{pC/N}^1, d_{31}=-115\text{pC/N}^2)$$

¹ direct measurement

² inferred from mechanical motion